



NORAD supported project in MRRD covering  
Capacity Building and Institutional Cooperation in the  
field of Hydrogeology for Faryab Province  
Afghanistan

# **Geophysics Course**

## **Introduction to DC Resistivity**

By Andreas de Jong  
June 2013

# Surface Geophysical Methods



# On-Line Courses & References

1. Colorado School of Mines
2. University of Berkeley
3. Ecole Polytechnique Montreal
4. University of Lausanne
5. University of Montana
6. United States Geological Survey (USGS)
7. Tomoquest

# PART 1 – Introduction

1. Passive and Active Geophysical Methods
2. Electrical Methods Overview
  - History
  - DC Resistivity
  - Induced Polarisation (IP)
  - Self Potential (SP)
  - Electromagnetic (EM)
  - Magnetotelluric (MT)

# Passive Geophysical Methods

- Passive geophysical surveys incorporate measurements of naturally occurring fields or properties of the earth.
- Examples: gravity, magnetic, radiometric surveys.





# Active Geophysical Methods

- In active geophysical surveys a signal is injected into the earth and we then measure how the earth responds to this signal. Signals include displacement, an electrical current, or an active radiometric source.
- Examples: DC Resistivity, TDEM, EM & Seismic surveys.

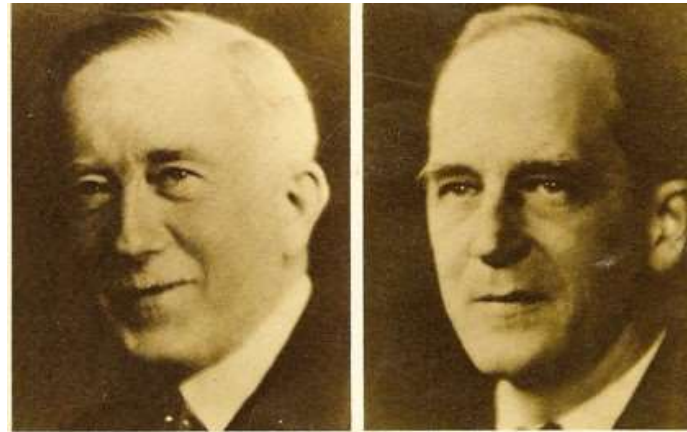


# Electrical Methods: History

- SP method dates back to the 1830's when it was used in Cornwall, England by Robert Fox to find extensions of known copper deposits.
- Telluric currents (natural electrical currents in the Earth), were first identified by Peter Barlow in 1847.
- The EM method was developed in the 1920's for the exploration of base-metal deposits.
- The Schlumberger brothers developed Schlumberger Array in 1912.



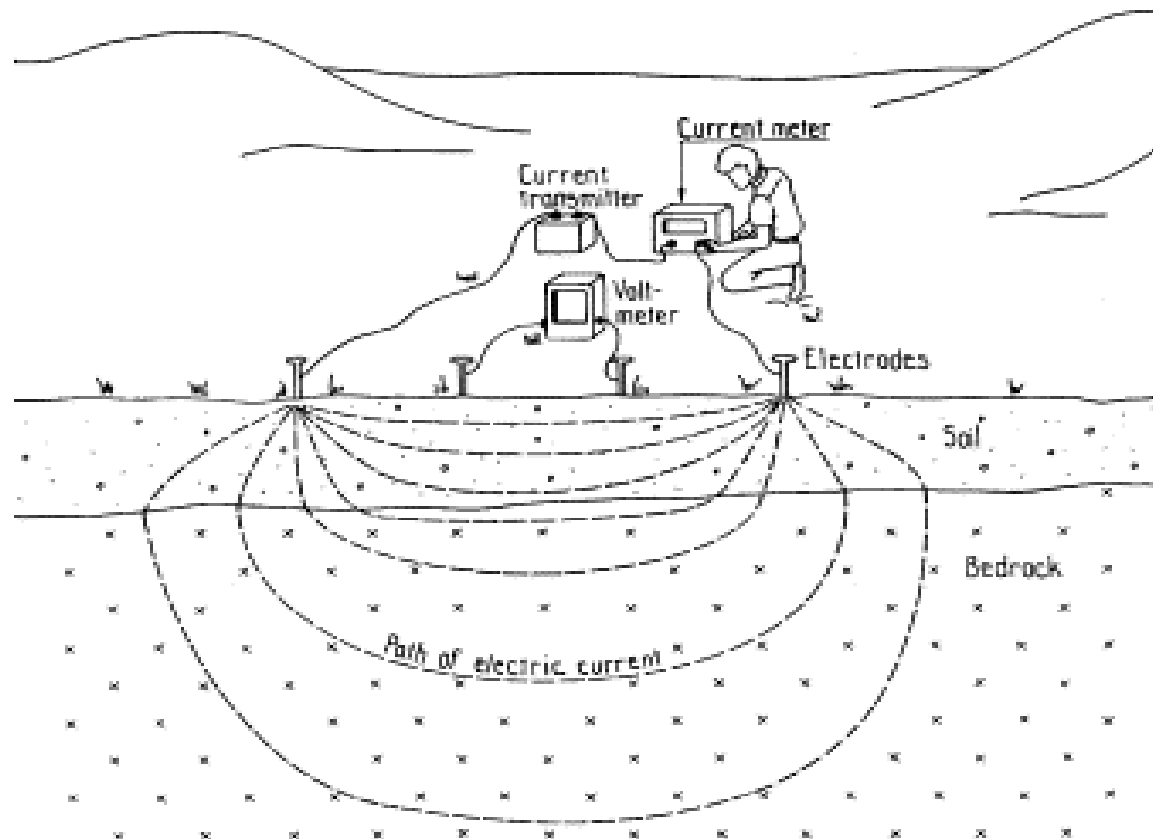
Source: <http://galitzin.mines.edu/INTROGP/>



Conrad and Marcel Schlumberger 1936

# Electrical Methods: DC Resistivity

- Active method that employs measurements of electrical potential associated with subsurface electrical current flow generated by a DC, or slowly varying AC, source.

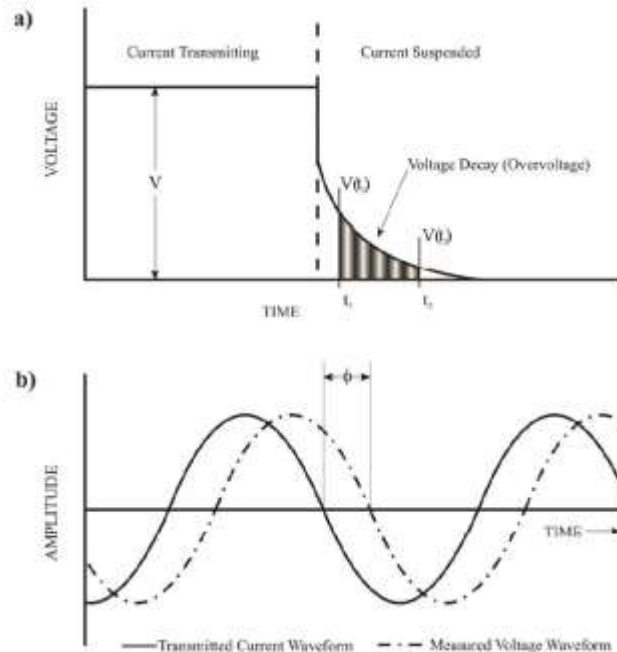


Source: <http://ars.els-cdn.com/content/image/1-s2.0-S0098300400001606-gr1.gif>



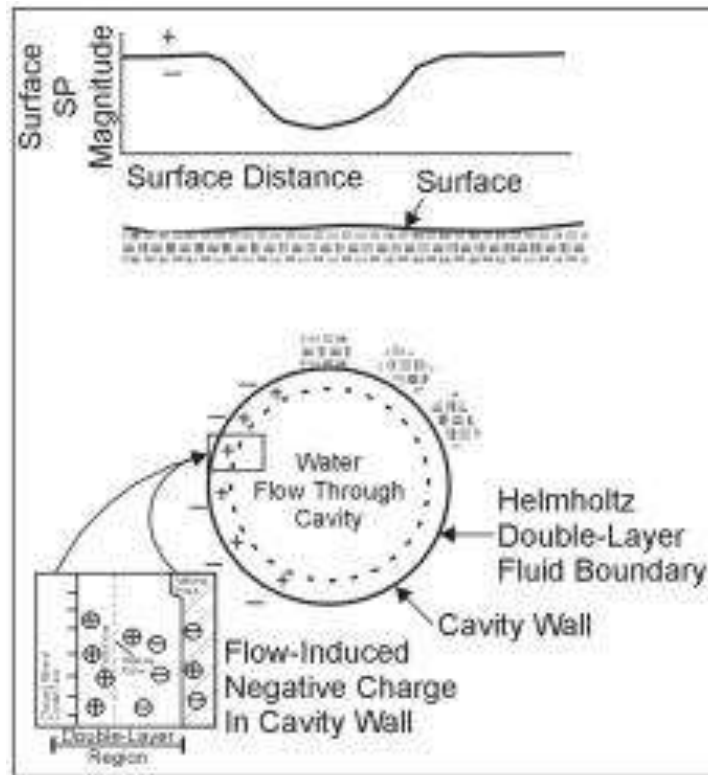
# Electrical Methods: Induced Polarization (IP)

- Active method that is commonly done in conjunction with DC Resistivity. It employs measurements of the transient (short-term) variations in potential as the current is initially applied or removed from the ground.
- IP is commonly used to detect concentrations of clay and electrically conductive metallic mineral grains.



# Electrical Methods: Self Potential (SP)

- Passive method that employs measurements of naturally occurring electrical potentials commonly associated with the weathering of sulphide ore bodies, or groundwater flow.

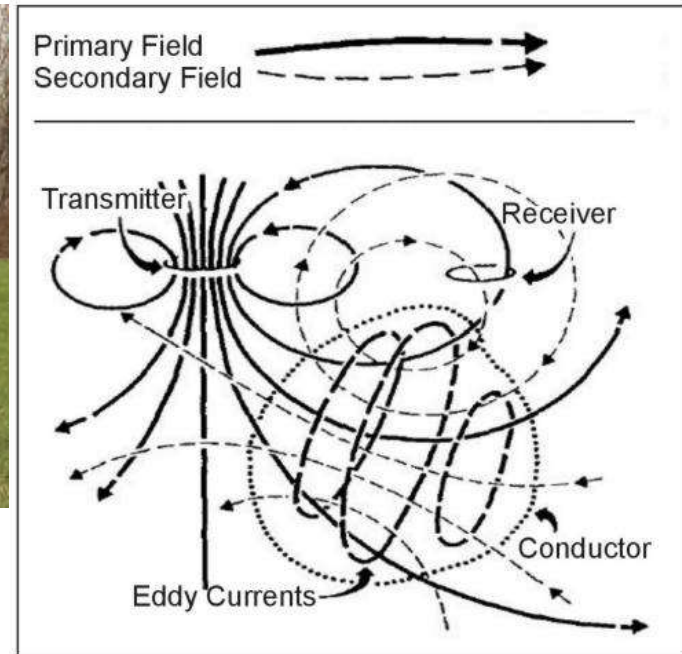


# Electrical Methods: Electromagnetic (EM)

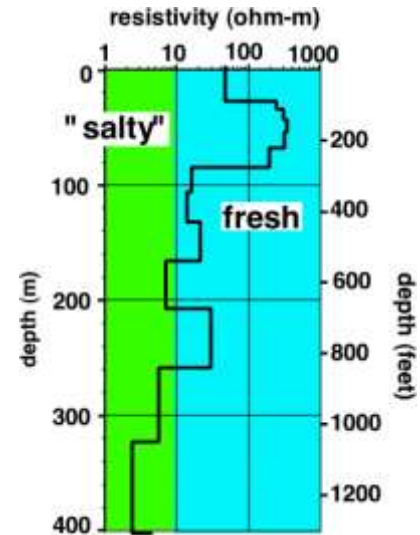
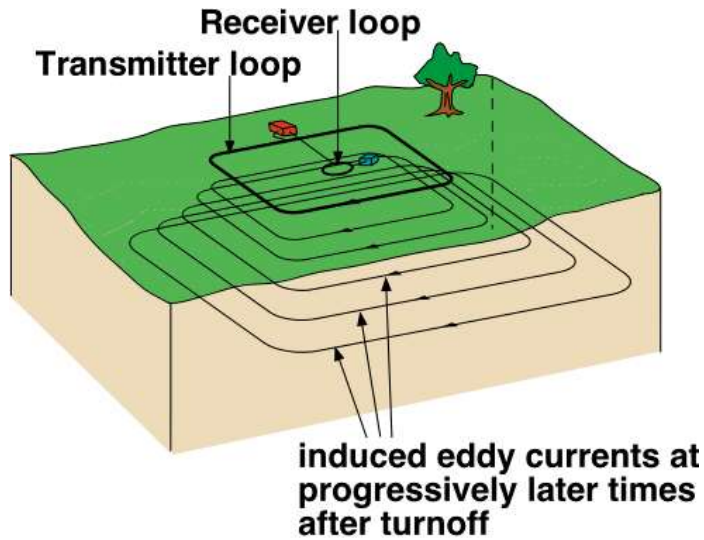
- Active method that employs measurements of a time-varying magnetic field generated by induction through current flow within the earth.



Geonics EM-34



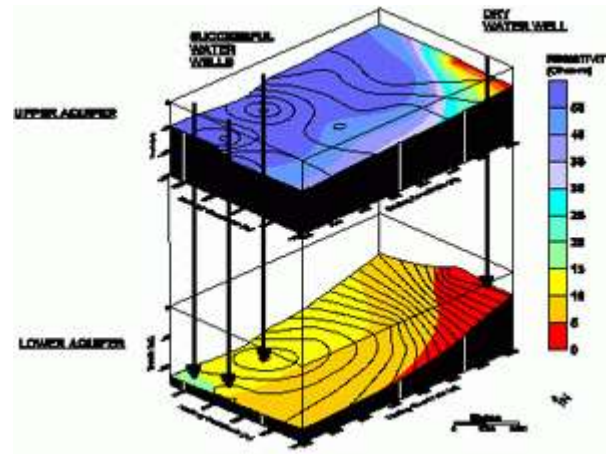
# Electrical Methods: TDEM



Source: [http://www.ncwater.org/Education\\_and\\_Technical\\_Assistance/Ground\\_Water/TDEM/](http://www.ncwater.org/Education_and_Technical_Assistance/Ground_Water/TDEM/)

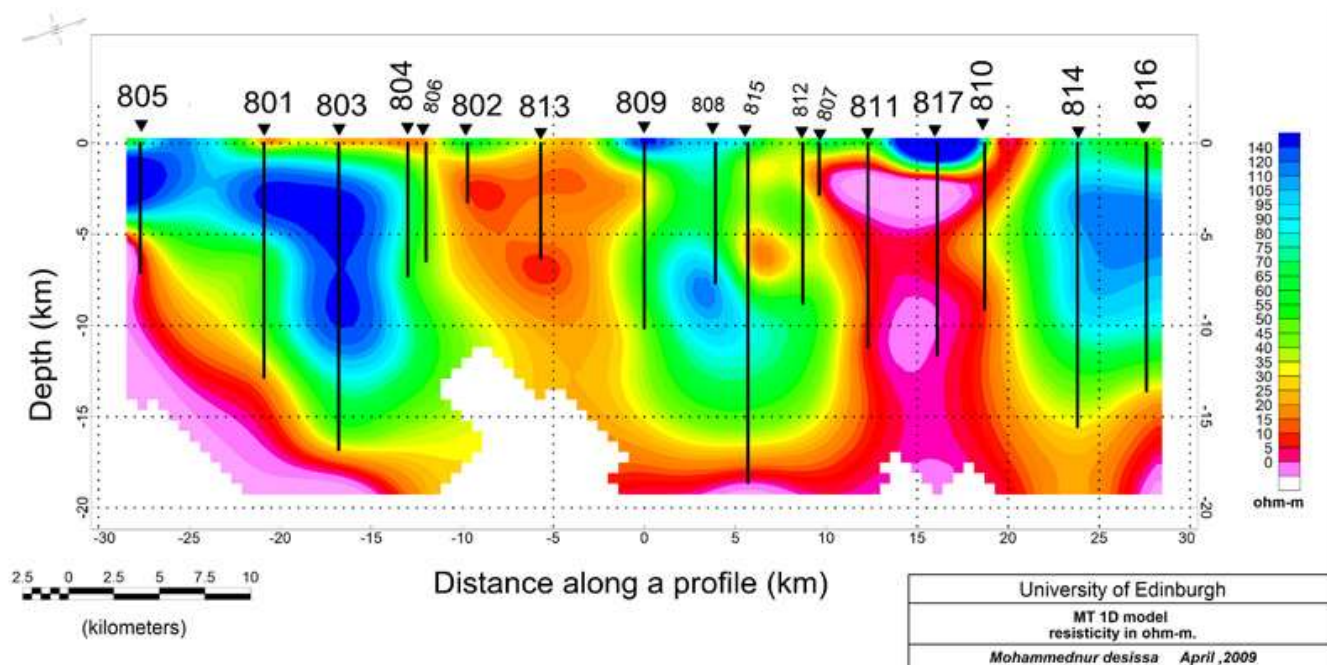


Geonics Protem 57



# Electrical Methods: Magnetotelluric (MT)

- Passive method that employs measurements of naturally occurring electrical currents, or telluric currents, generated by magnetic induction of electrical currents in the ionosphere.
- This method can be used to determine electrical properties of materials at relatively great depths (down to and including the mantle) inside the Earth.



Source: [http://www.earthexplorer.com/2009-07/Steamy\\_Prospects\\_in\\_Ethiopia.asp](http://www.earthexplorer.com/2009-07/Steamy_Prospects_in_Ethiopia.asp)

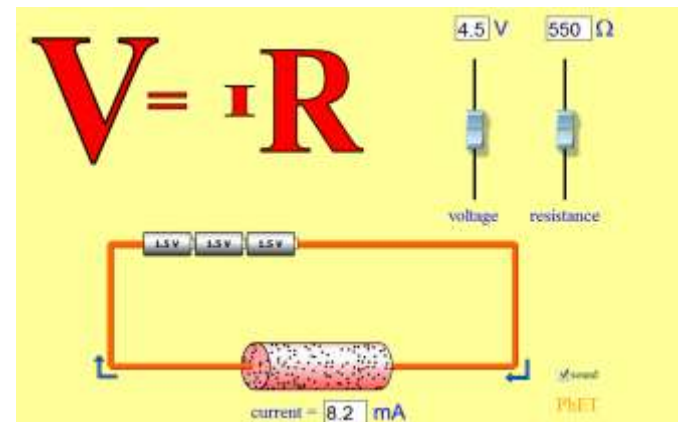
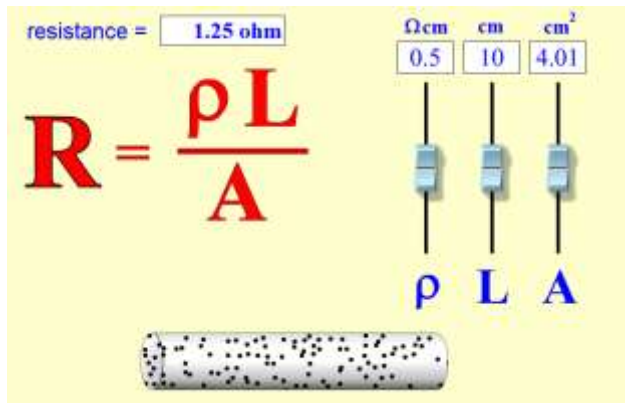
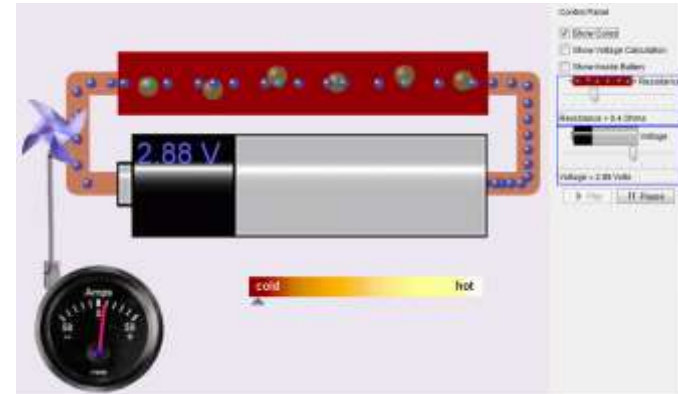
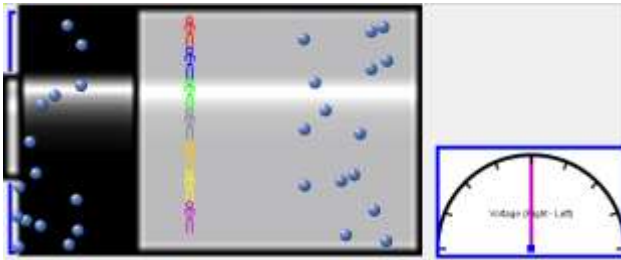


# PART 2 – Resistivity Basics

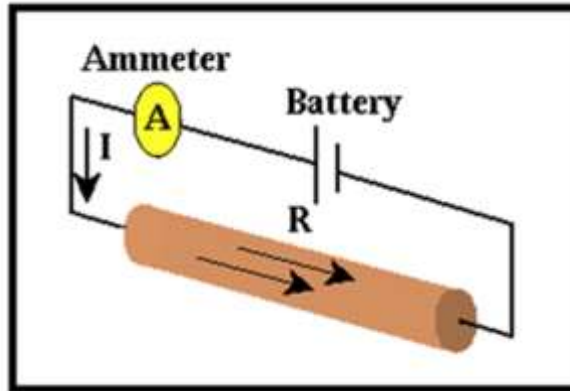
1. Current Flow and Ohm's Law
2. Resistivity & Resistance
3. Conductivity
4. Factors Affecting Resistivity
5. Archie's Law
6. Resistivities for Common Earth Materials
7. Current Density and Electric Field
8. A First Estimate of Resistivity
9. Current Flow From Two Closely Spaced Electrodes
10. A Practical Way of Measuring Resistivity



# Practical 1 - Electricity



# Current Flow & Ohm's Law



$$V = IR$$

Ohm's Law (1827)

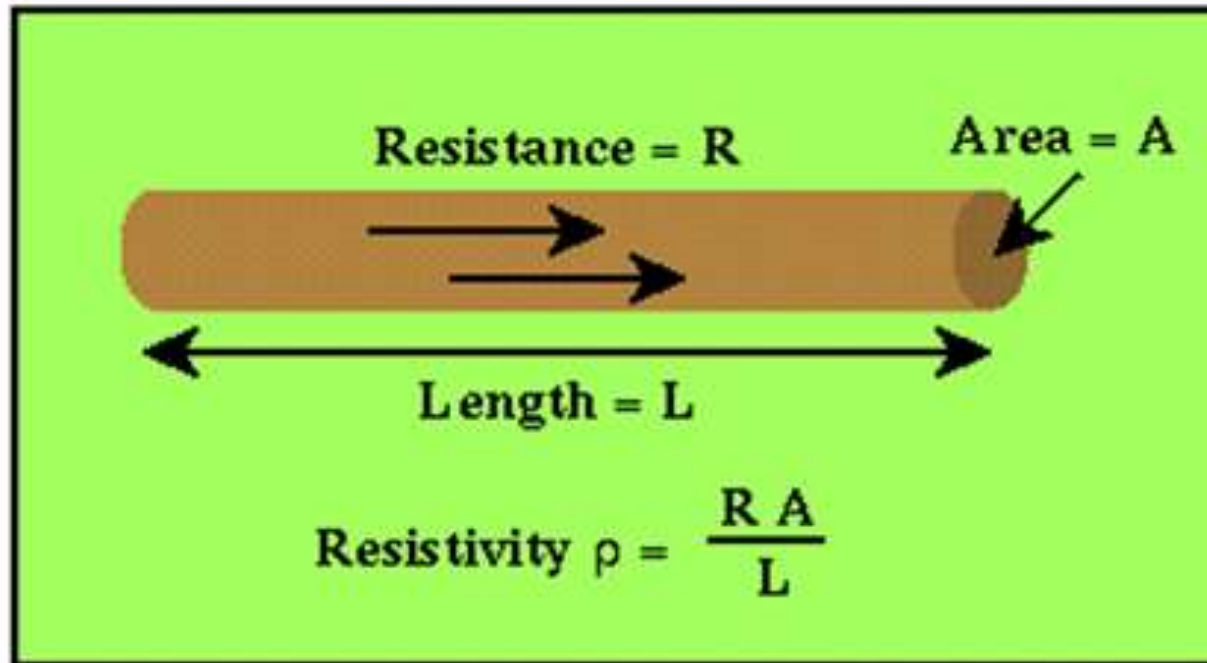
- V = voltage (volts)
- I = Current (amperes)
- R = Resistance (ohms)



# Problems with Resistance

## Resistance:

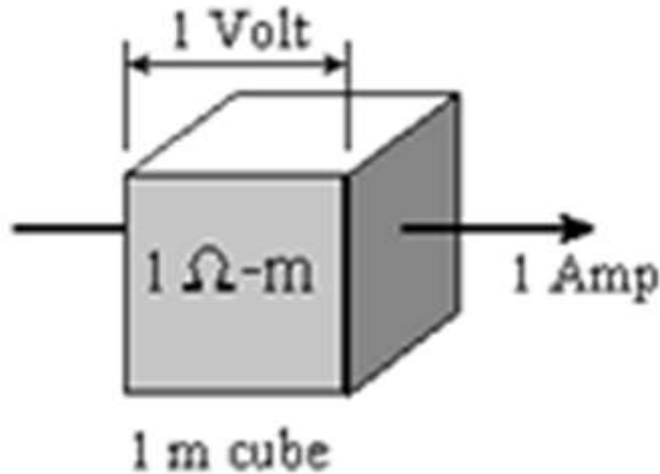
- depends not only on the material from which the wire is made, but also the geometry of the wire. i.e. the length and thickness of the wire affects the reading.
- How can we apply this relatively simple experiment to determine electrical properties of earth materials?



# Use Resistivity, NOT Resistance

Resistivity = resistance per unit volume

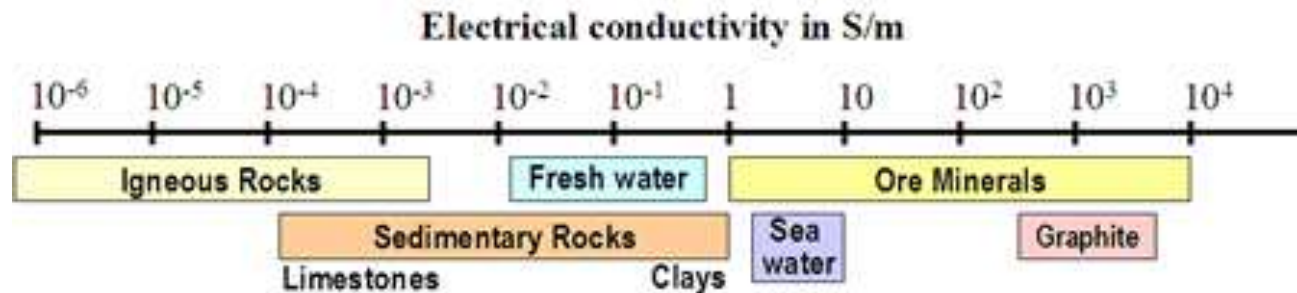
- Resistivity is a geometrically-independent quantity that is usually indicated by the Greek symbol  $\rho$ .
- Units are ohm-m (ohm-meters).



# Conductivity

Conductivity = inverse of resistivity:  $1/\rho$

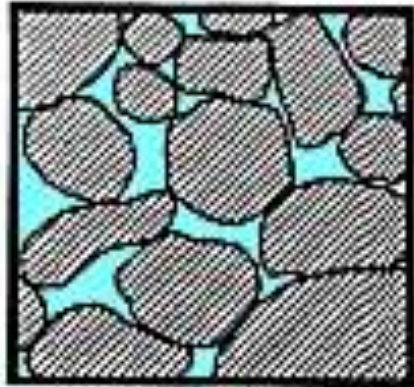
- Conductivity is often represented using sigma,  $\sigma$
- Conductivity is given in units of Siemens per metre, or S/m.
- Units of millisiemens per metre (mS/m) are often used for small conductivity values.
- $1000\text{mS/m} = 1\text{S/m}$ . So  $1\text{mS/m} = 1000\text{ Ohm-m}$ , since resistivity and conductivity are inversely related.



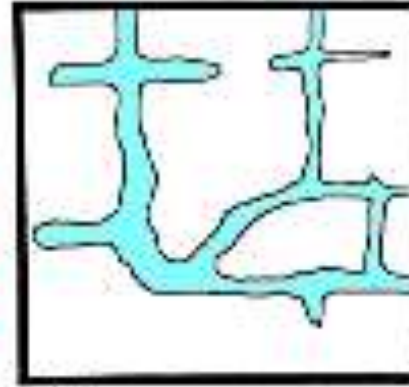
Source; <http://www.eos.ubc.ca/ubcgif/iag/foundations/properties/resistivity.htm>



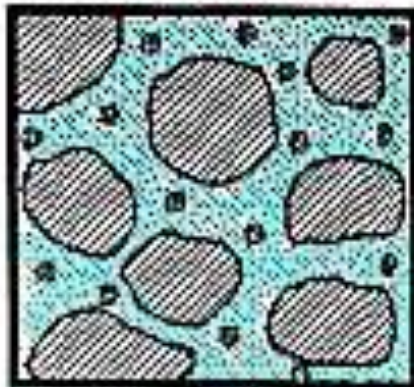
# Factors Affecting Resistivity - Porosity



Two textures of sandstone



Vuggy limestone



Sandstone clay mixture



Fractured granite

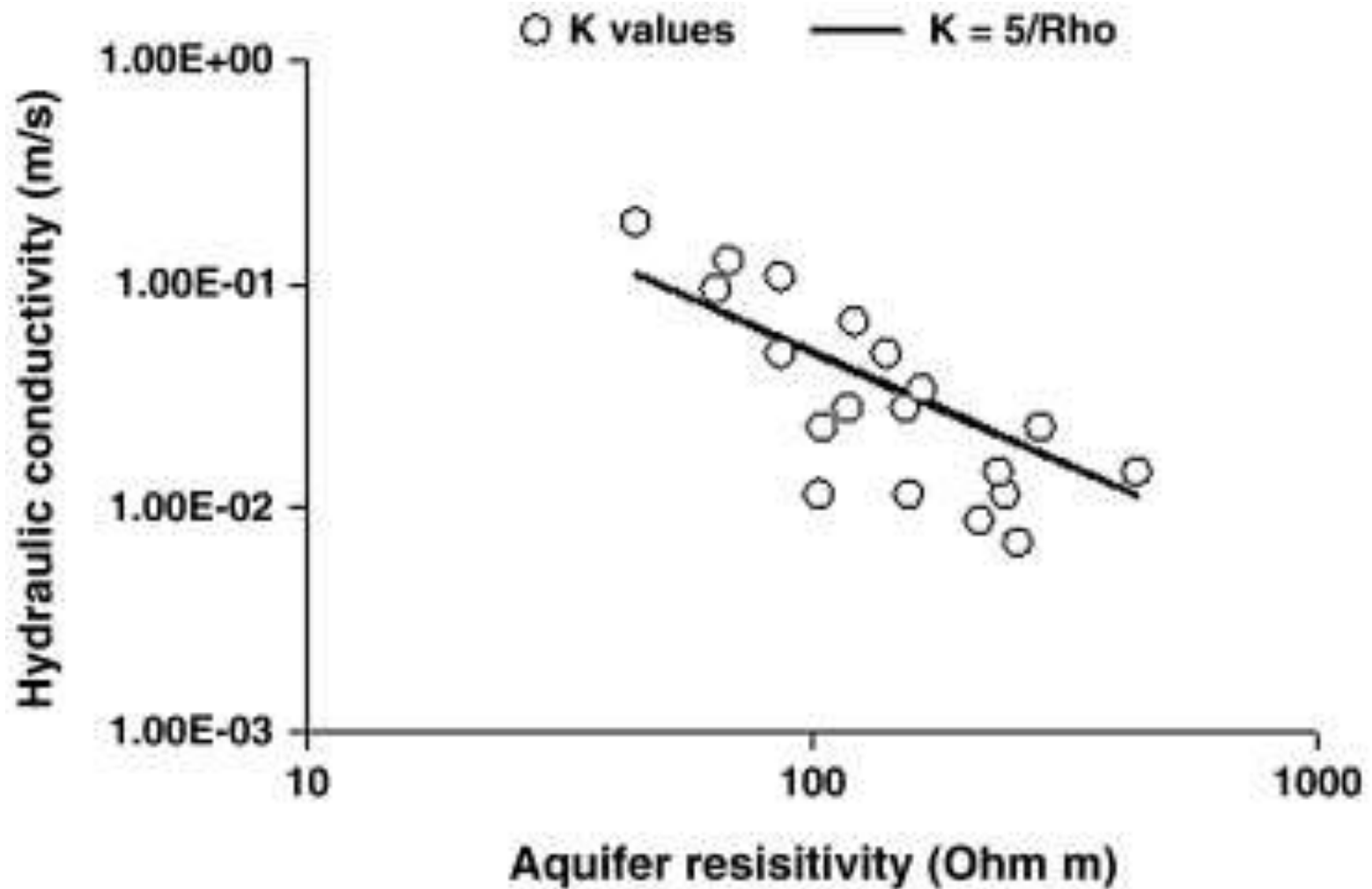


Basalt with vuggy pores

Source; <http://www.eos.ubc.ca/ubcgif/iag/foundations/properties/resistivity.htm>

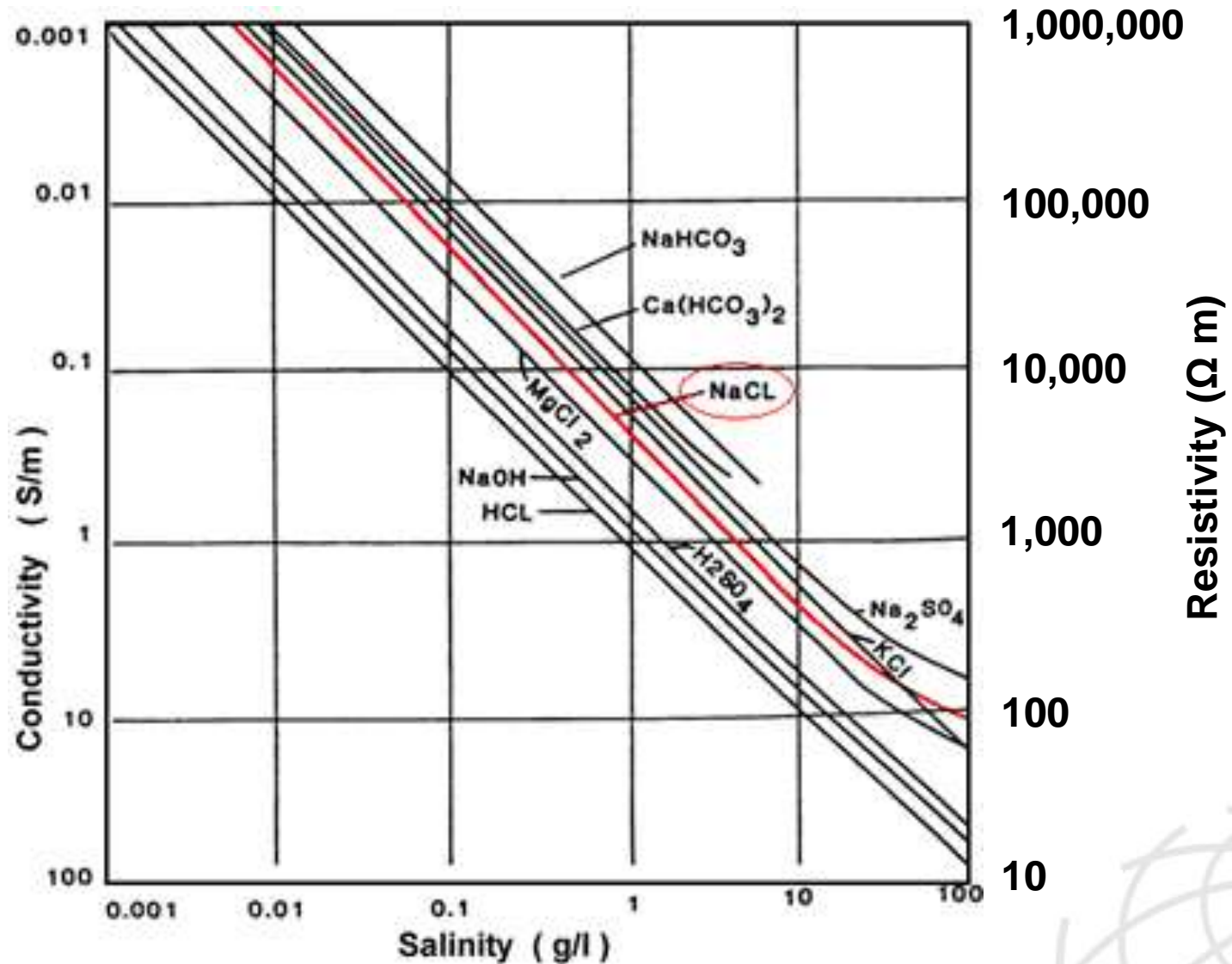


# Factors Affecting Resistivity - Permeability



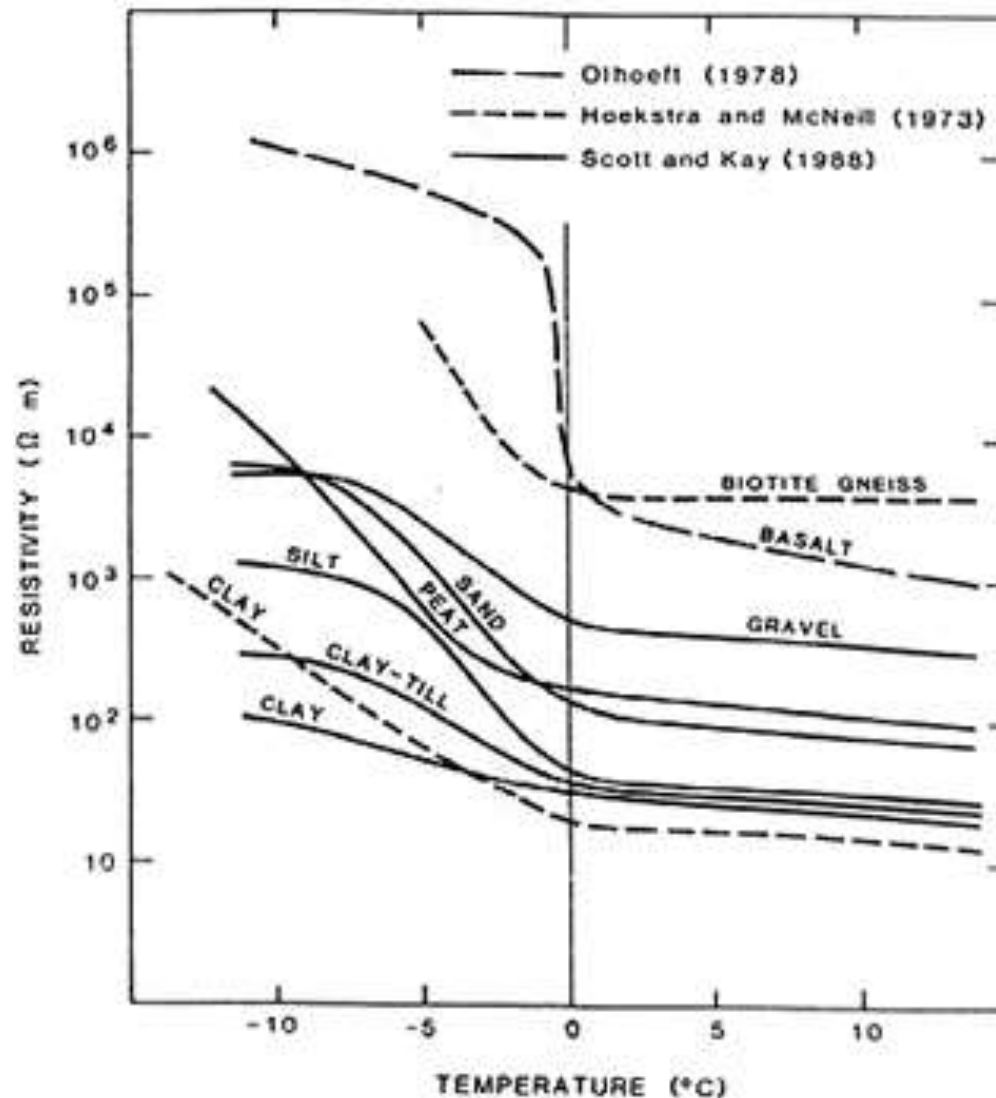
Source: <http://www.sciencedirect.com/science/article/pii/S0926985112000985>

# Factors Affecting Resistivity - Salinity



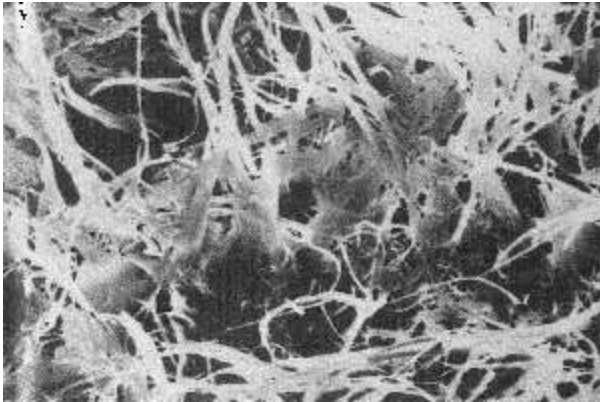
Source: <http://www.eos.ubc.ca/ubcgif/iag/foundations/properties/resistivity.htm>

# Factors Affecting Resistivity - Temperature



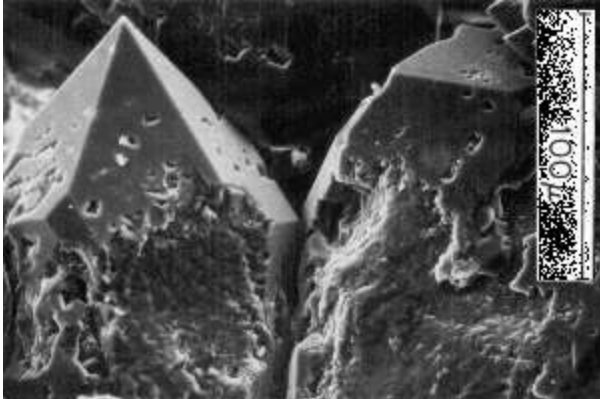
Source: <http://www.eos.ubc.ca/ubcgif/iag/foundations/properties/resistivity.htm>

# Factors Affecting Resistivity – Clay Content



Illite (a clay mineral) with total surface area of  **$100\text{m}^2/\text{gm}$**

(photo Credit: R. Knight.)



Quartz overgrowths in sandstone with total surface area of  **$0.1\text{m}^2/\text{gm}$**

(photo credit: R. Knight.)

# Archie's Law (1942)

$$\frac{\rho_r}{\rho_f} = \alpha \phi^{-m}$$

Where,

$\rho_r$  is the rock resistivity, in ohm-meters

$\rho_f$  is the resistivity of the pore fluid

$\alpha$  is the coefficient of saturation

1 = complete saturation

$\phi$  is the porosity

$m$  is the cementation factor

# Formation Factor

$$F = \alpha \phi^{-m}$$

Where,

$F$  is the formation factor  
 $\alpha$  is the coefficient of saturation  
1 = complete saturation  
 $\phi$  is the porosity  
 $m$  is the cementation factor



# Archie's Law

$$\rho_r = F\rho_f$$

Where,

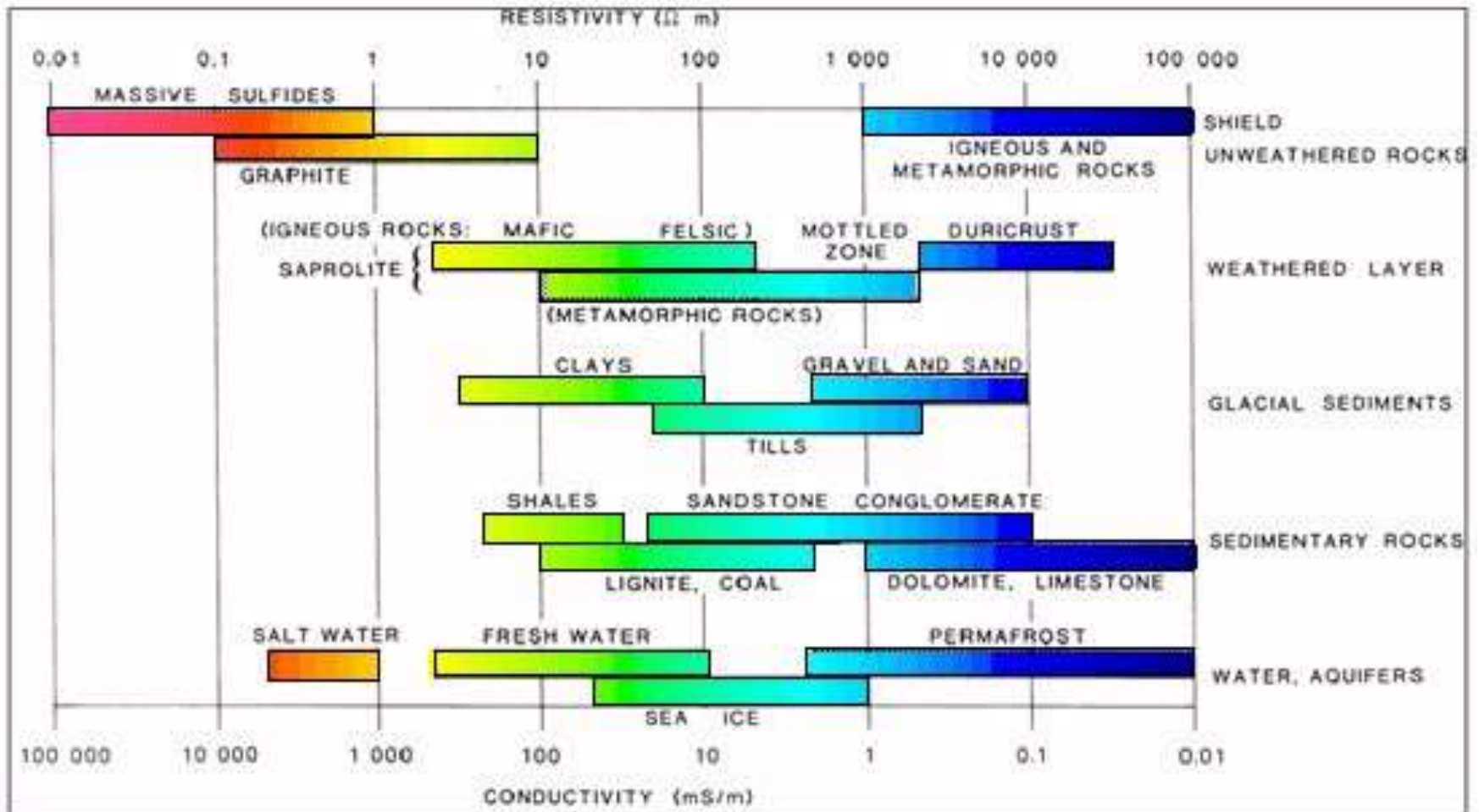
$\rho_r$  is the rock resistivity, in ohm-meters

$F$  is the formation factor

$\rho_f$  is the resistivity of the pore fluid

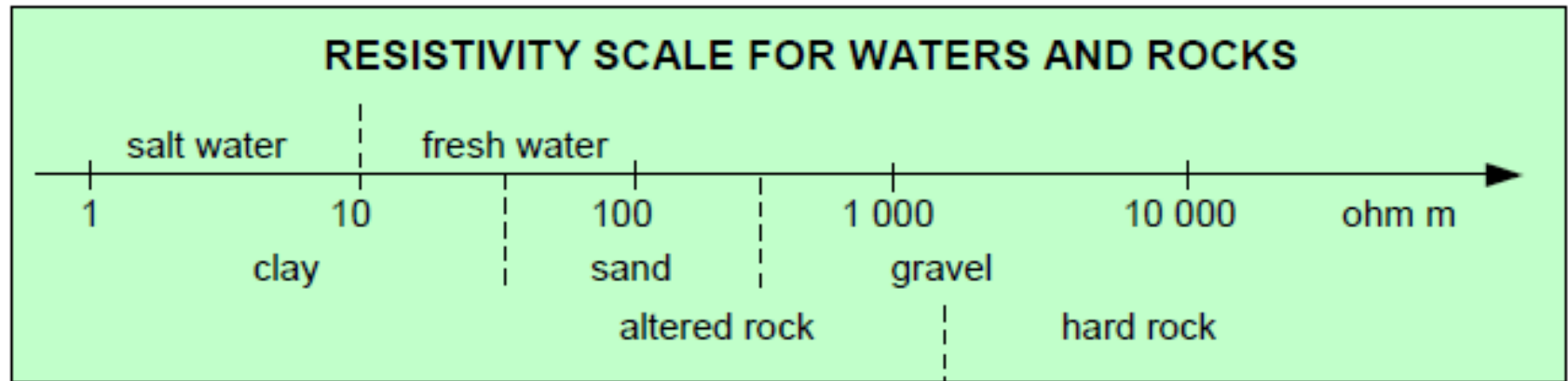
**Note: Archie's Law does not work  
when the rocks contain CLAY!**

# Resistivity of Rock Forming Materials



Source: <http://www.eos.ubc.ca/ubcgif/iag/foundations/properties/resistivity.htm>

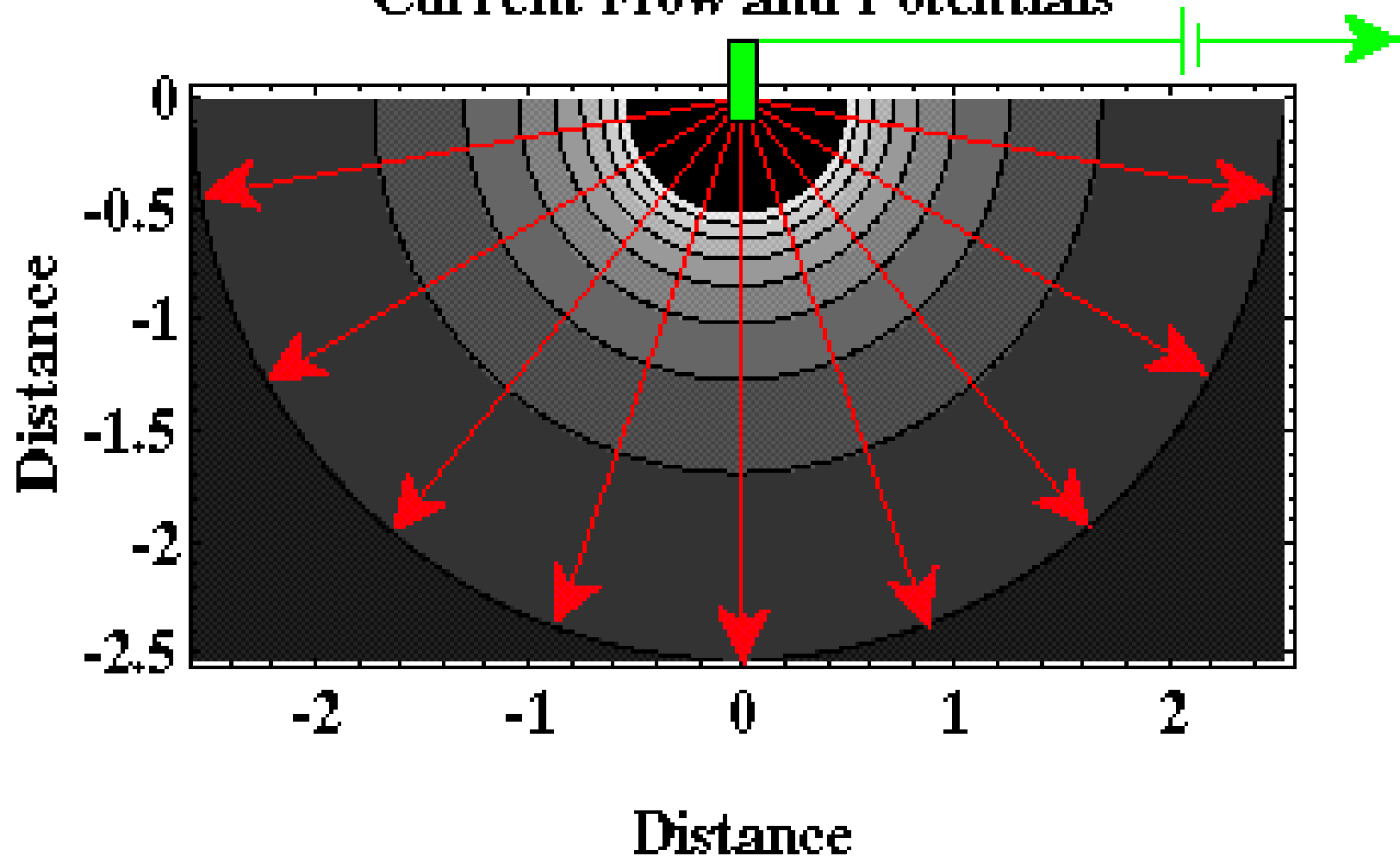
# Resistivity of Rock Forming Materials



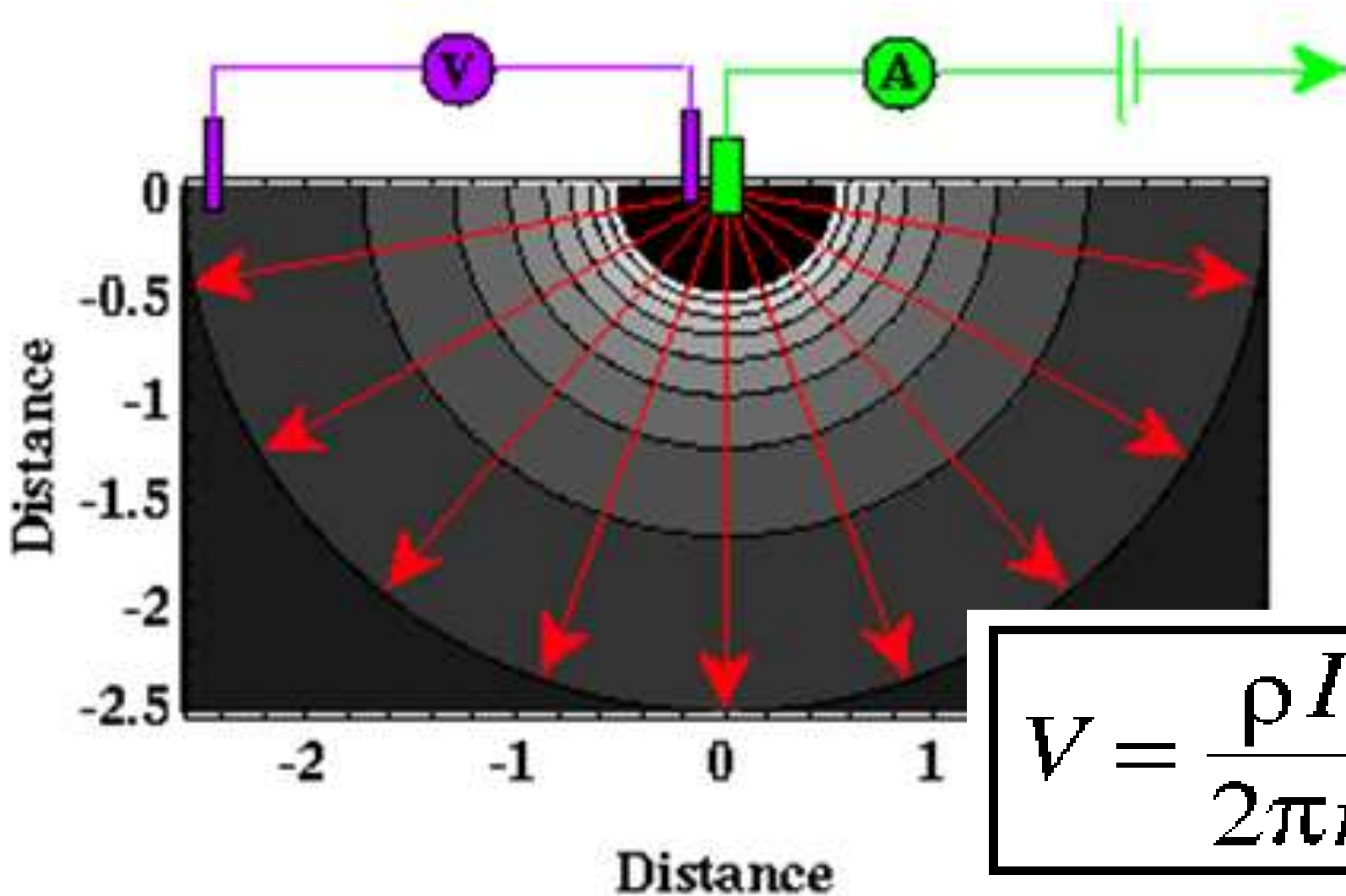
Source: <http://www.iris-instruments.com>

# Current Density and Electric Field

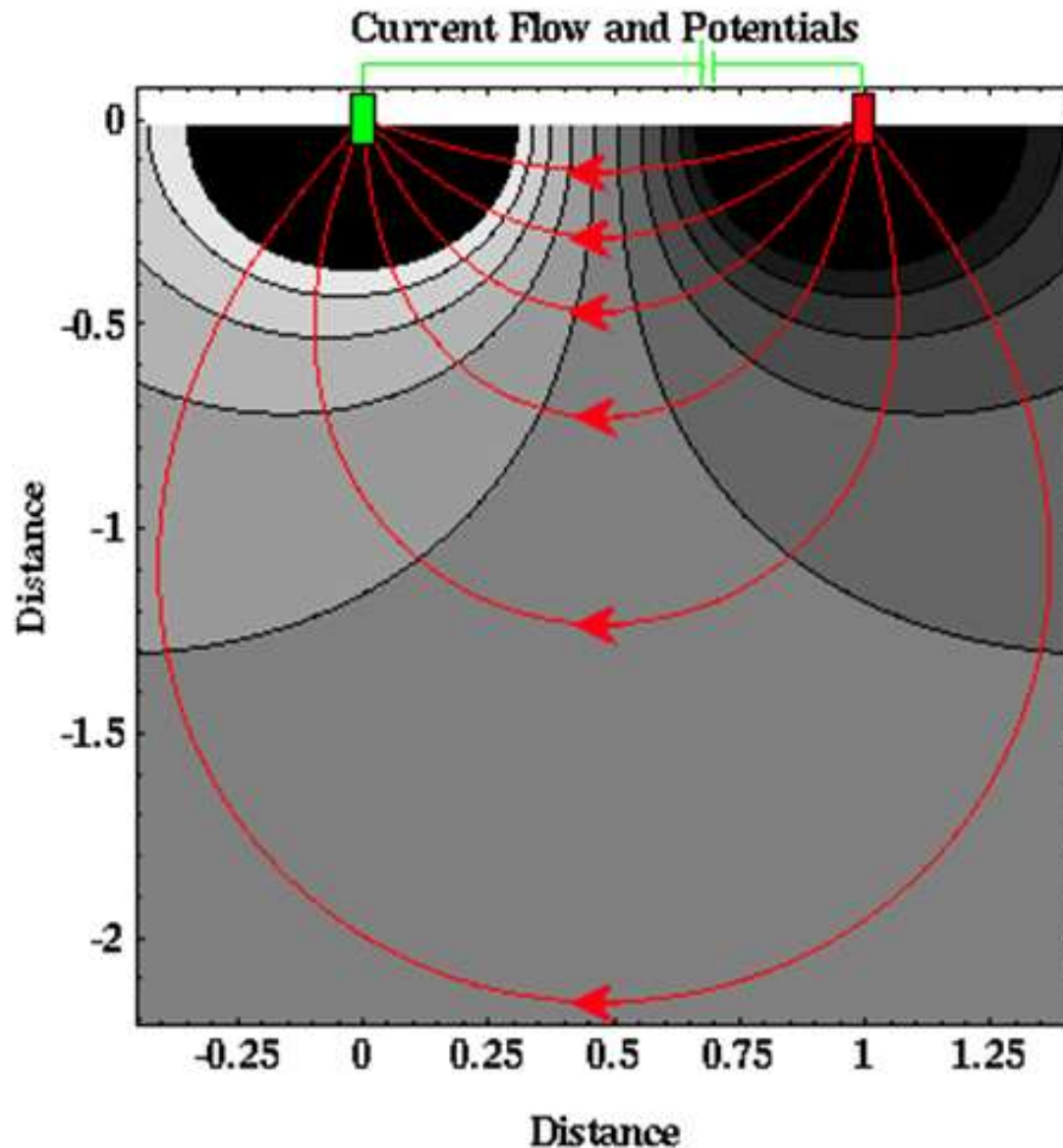
## Current Flow and Potentials



# A First Estimate of Resistivity



# Current Flow - Two Closely Spaced Electrodes

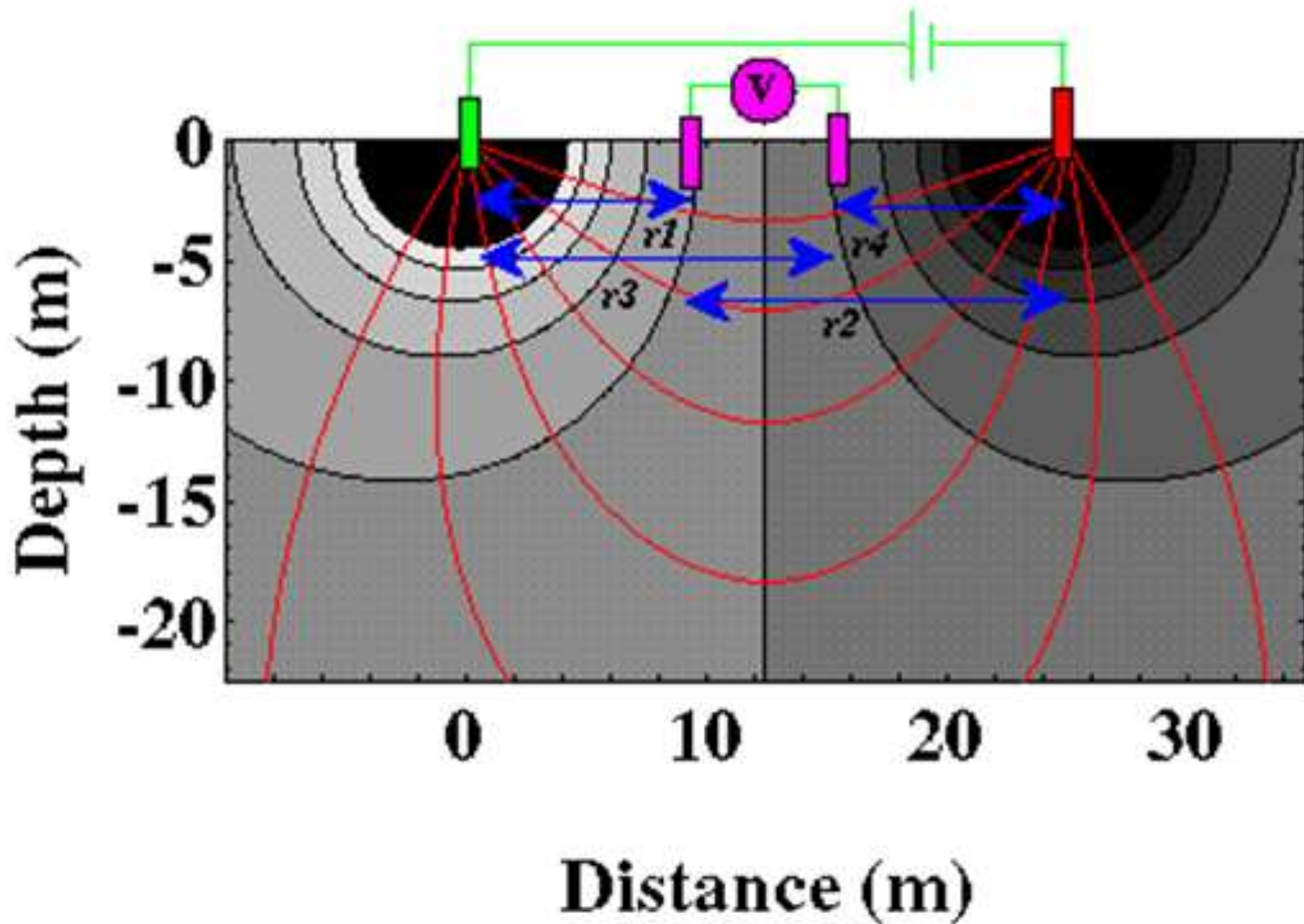


| Current Path | % of Total Current |
|--------------|--------------------|
| 1            | 17                 |
| 2            | 32                 |
| 3            | 43                 |
| 4            | 49                 |
| 5            | 51                 |
| 6            | 57                 |

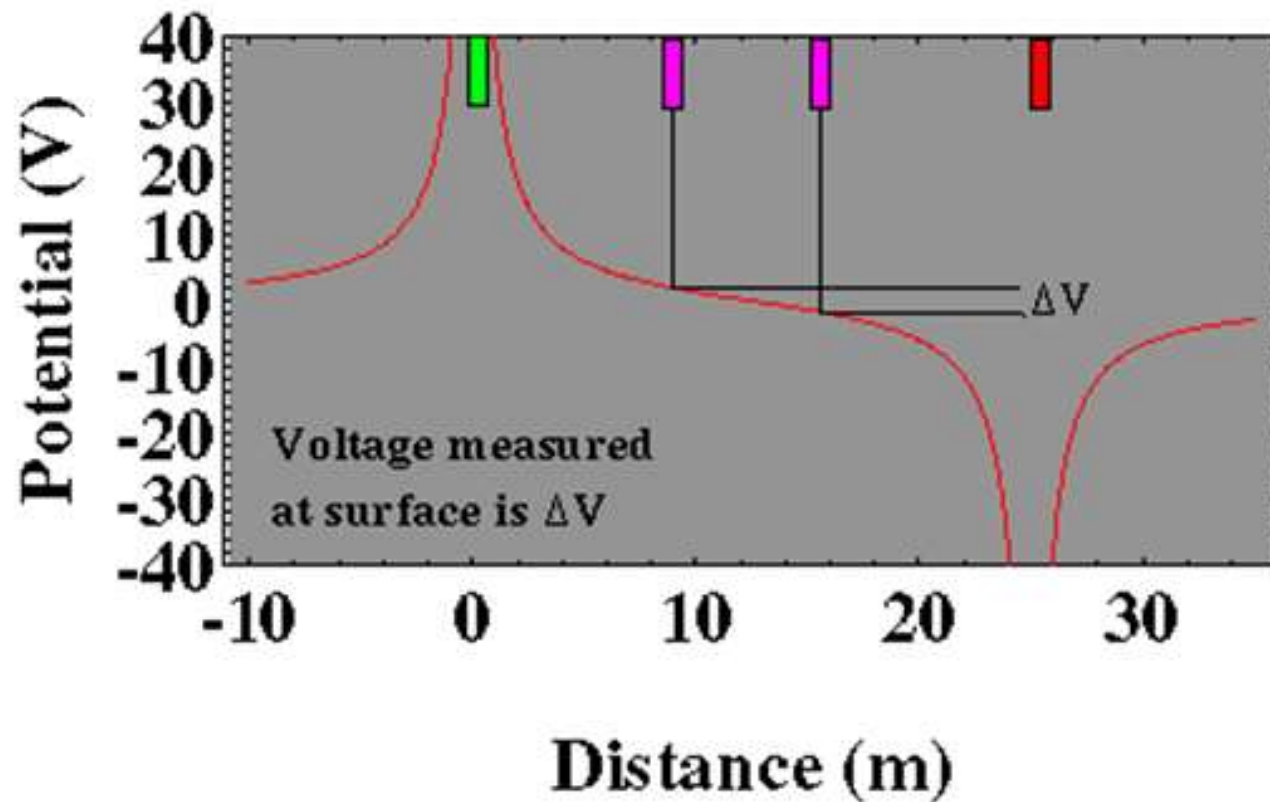
Source: <http://galitzin.mines.edu/INTROGP/>



# A Practical Way of Measuring Resistivity



# A Practical Way of Measuring Resistivity



$$\rho_{\alpha} = \frac{2\pi\Delta V}{i} \left[ \frac{1}{\left( \frac{1}{r_1} - \frac{1}{r_2} - \frac{1}{r_3} + \frac{1}{r_4} \right)} \right]$$

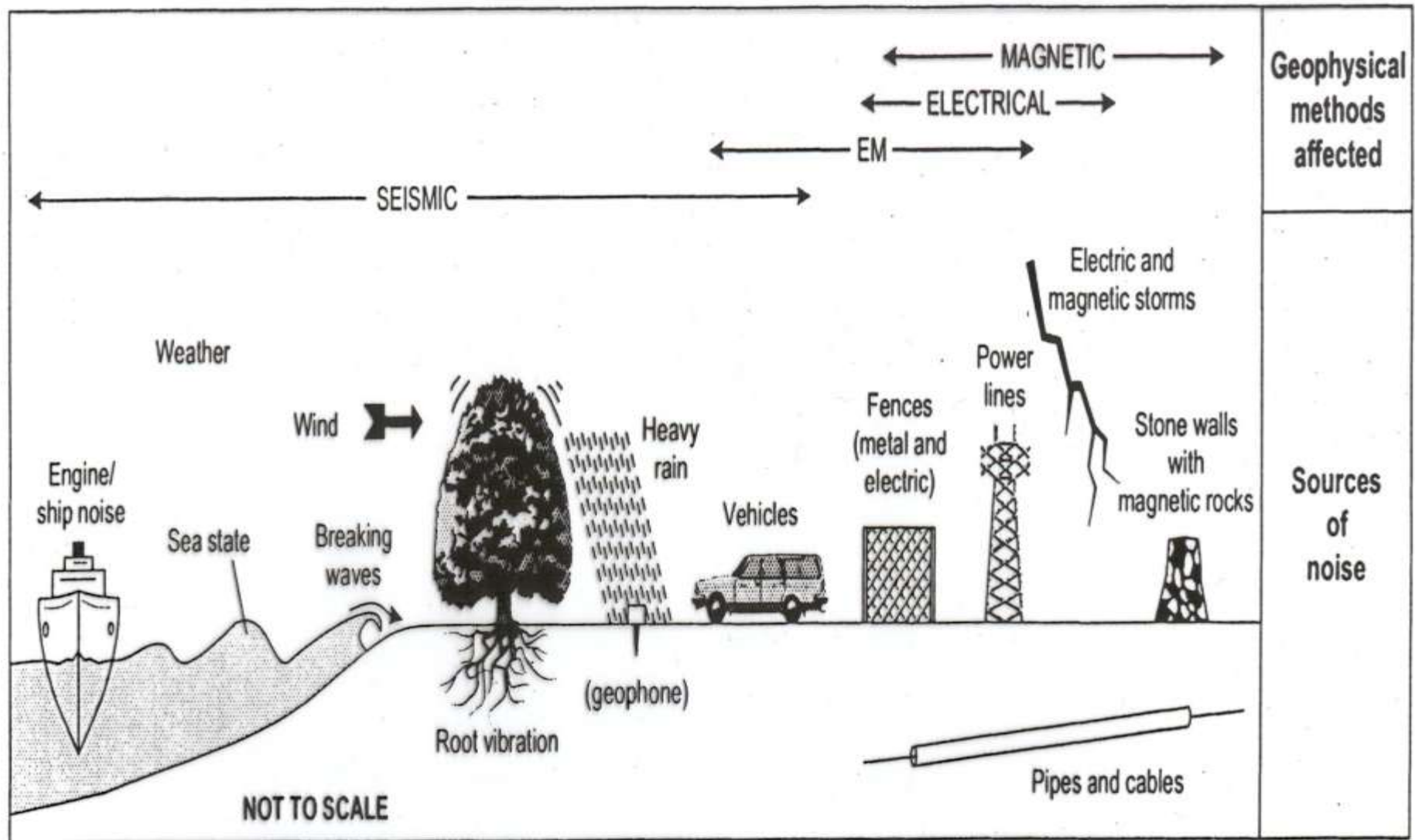
# PART 3 – Resistivity Surveys and Geology

1. Sources of Noise
2. Depth of Current Penetration Versus Current Electrode Spacing
3. Current Flow in Layered Media
4. Variation in Apparent Resistivity: Layered Versus Homogeneous Media
5. Current Flow in Layered Media Versus Electrode Spacing

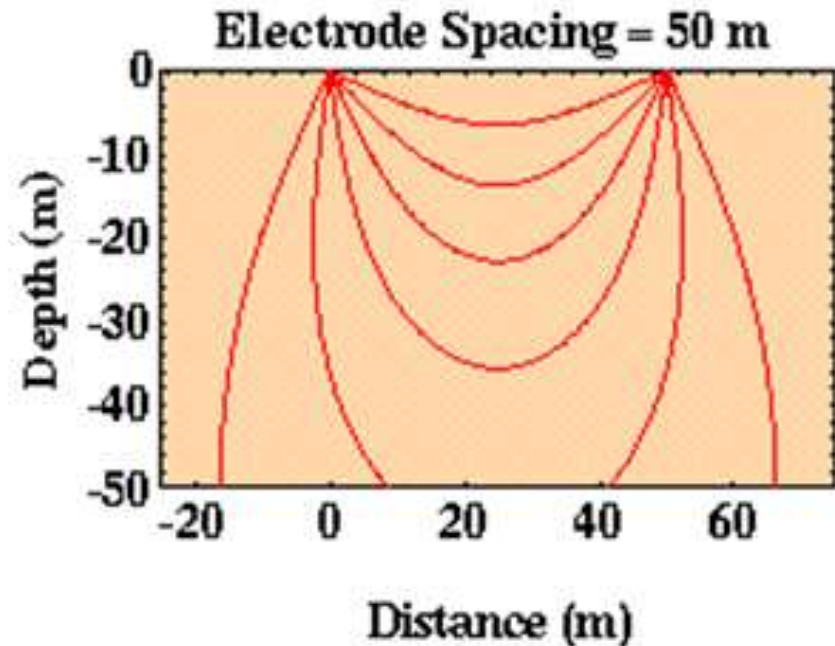
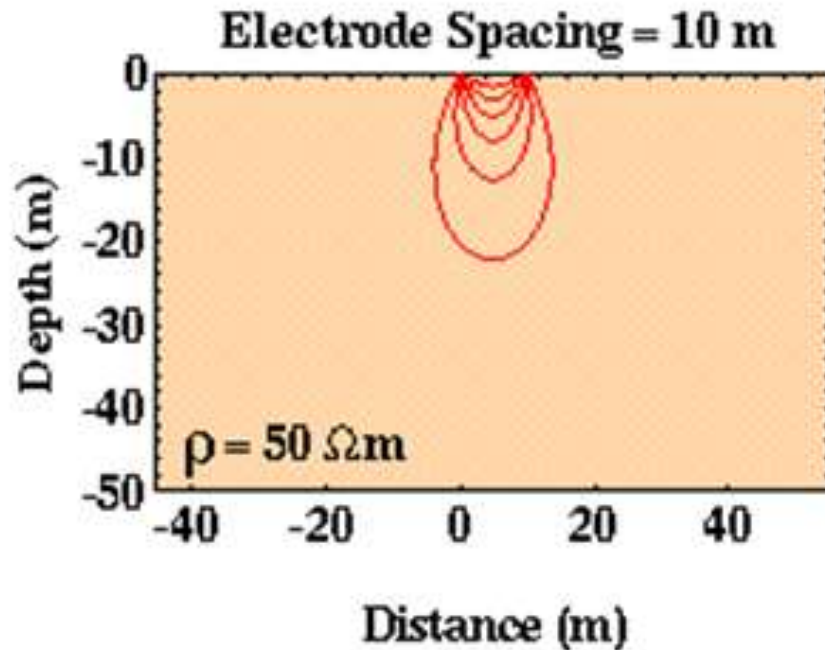
# Sources of Noise

- Electrode Polarization
  - Use non-polarizing electrodes
  - Reverse current flow in the current electrodes
- Telluric Currents
- Presence of Nearby Conductors
- Low Resistivity at the Near Surface
- Near-Electrode Geology and Topography
- Current Induction in Measurement Cables

# Sources of Noise

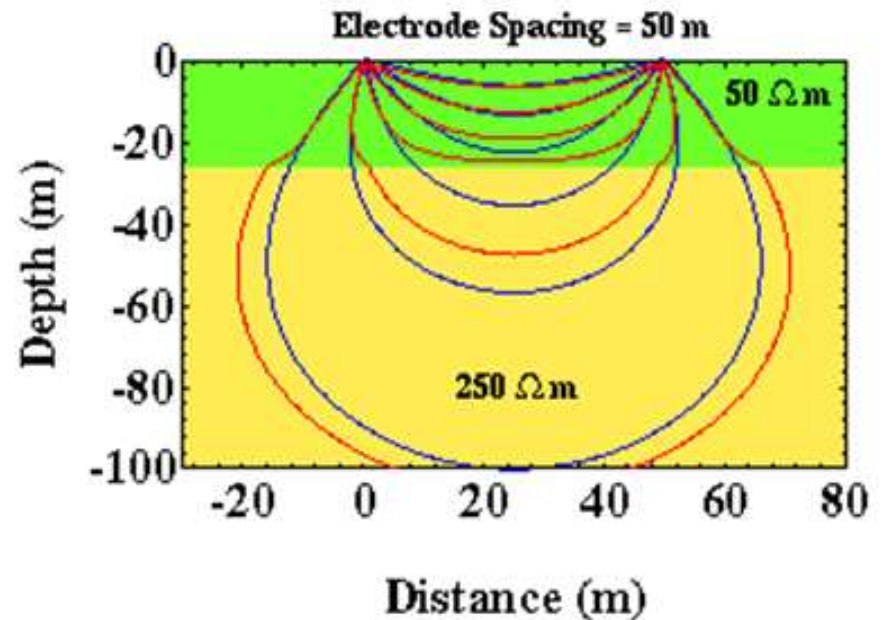
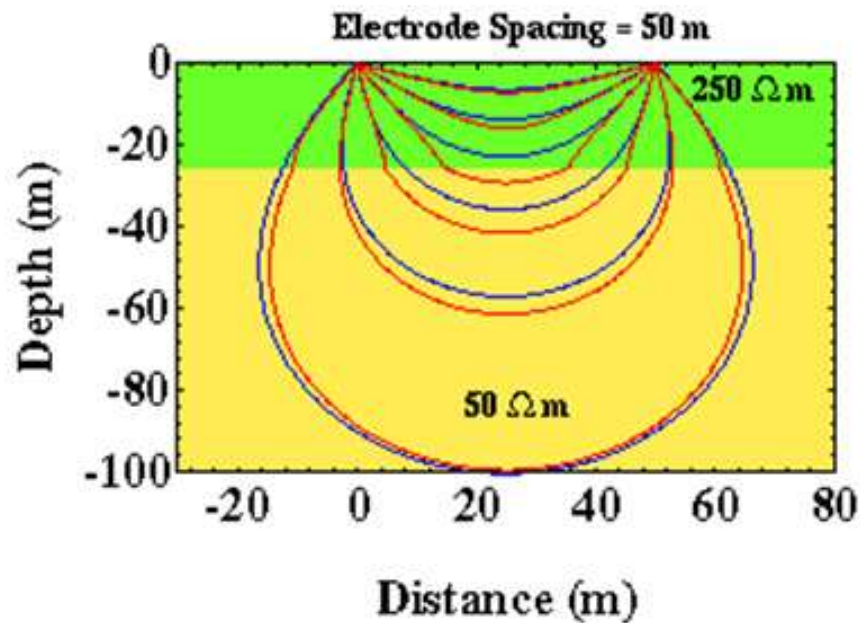


# Depth of Current Penetration Versus Current Electrode Spacing

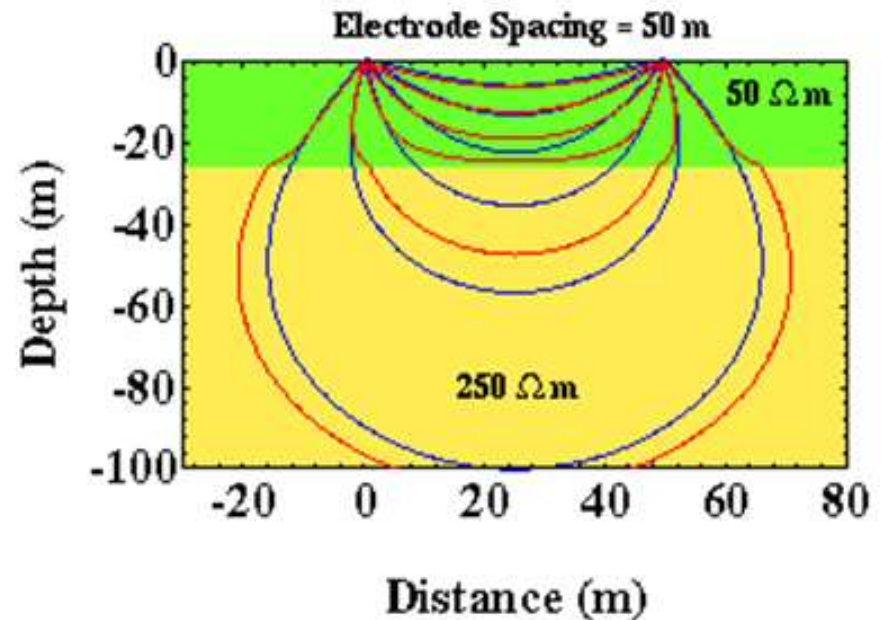
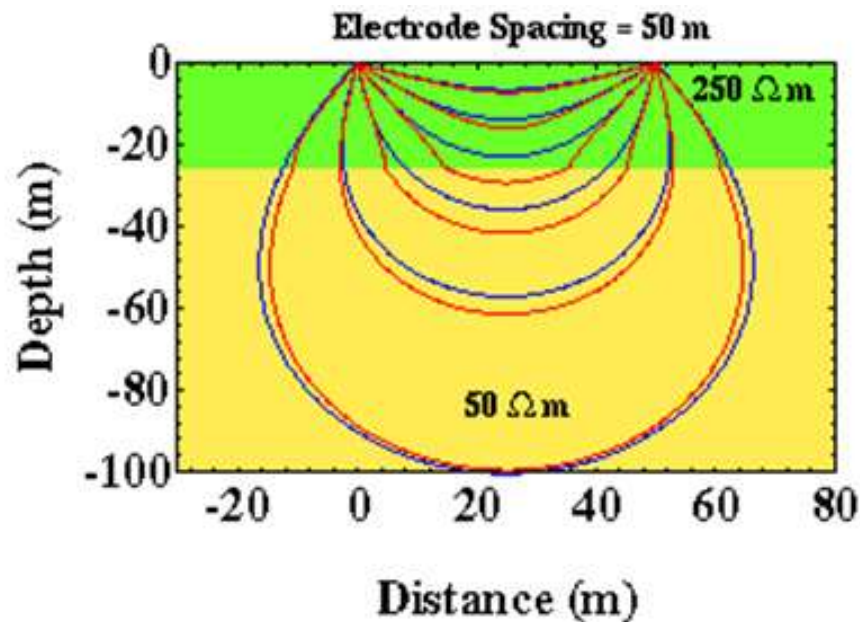




# Current Flow in Layered Media



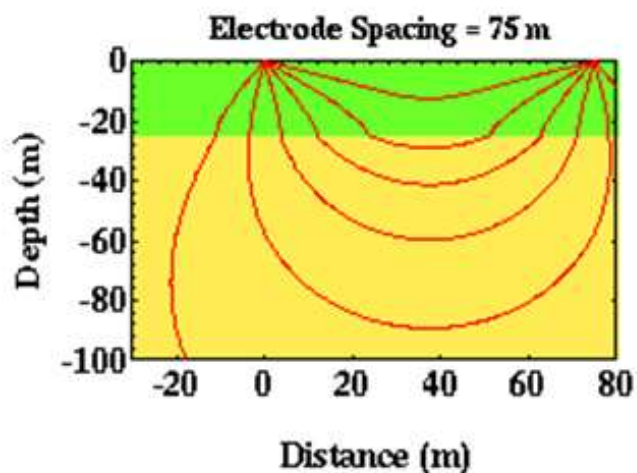
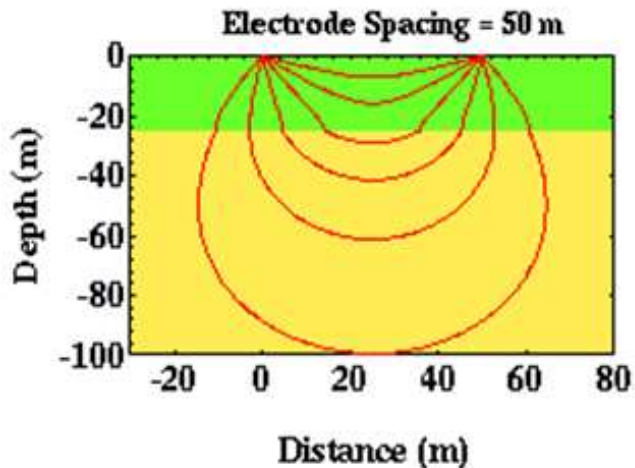
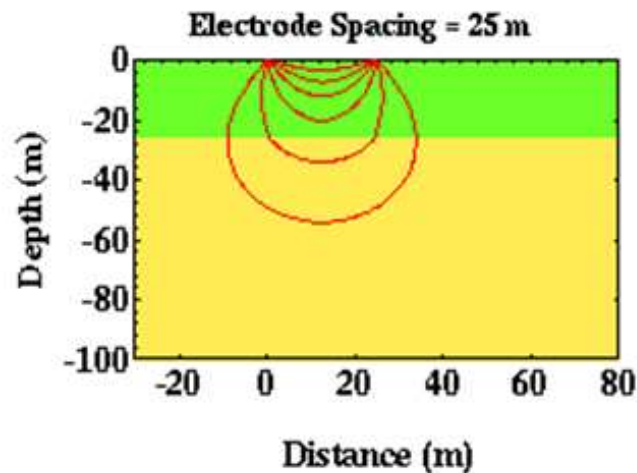
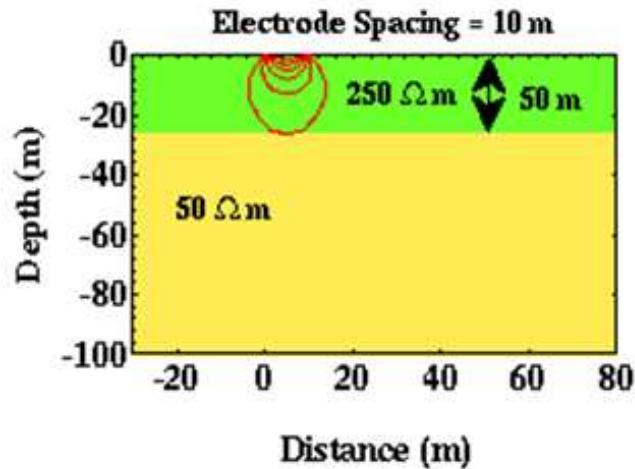
# Variation in Apparent Resistivity: Layered Versus Homogeneous Media



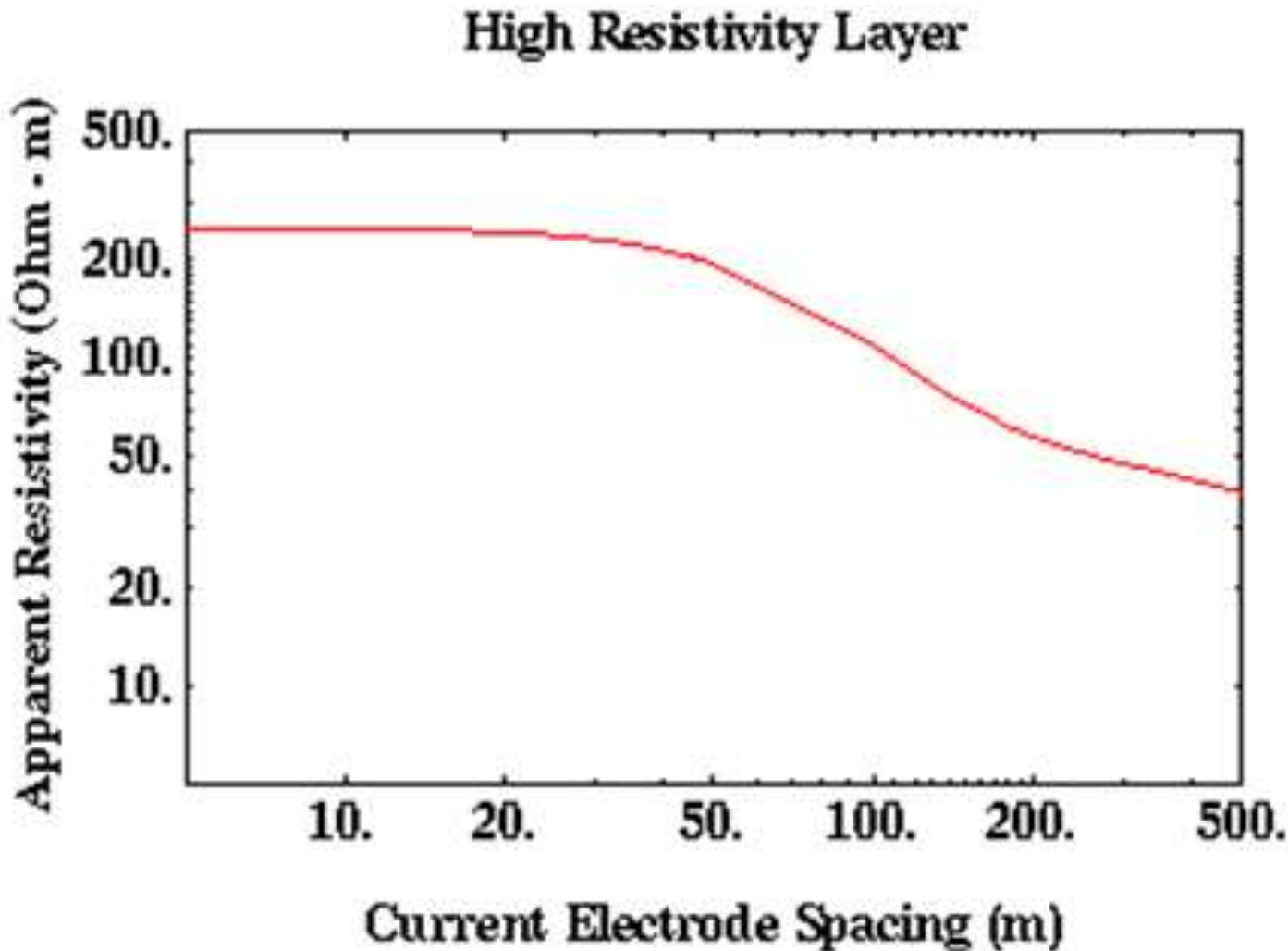
$$\rho_a = \frac{2\pi\Delta V}{i} \left[ \frac{1}{\left( \frac{1}{r_1} - \frac{1}{r_2} - \frac{1}{r_3} + \frac{1}{r_4} \right)} \right]$$

Source: <http://galitzin.mines.edu/INTROGP/>

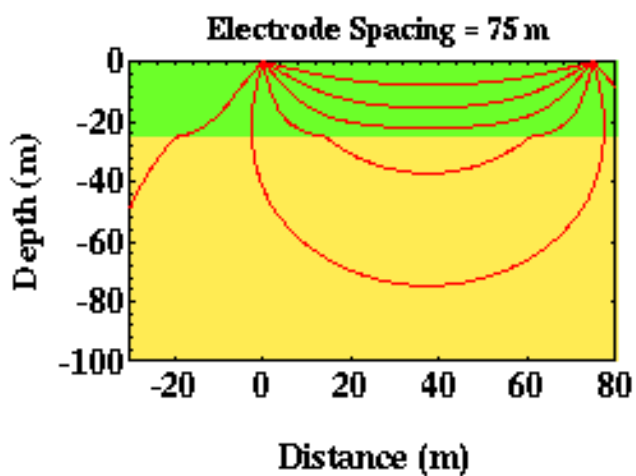
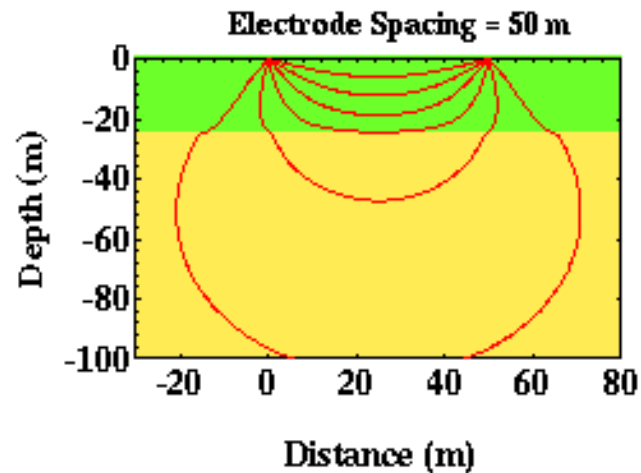
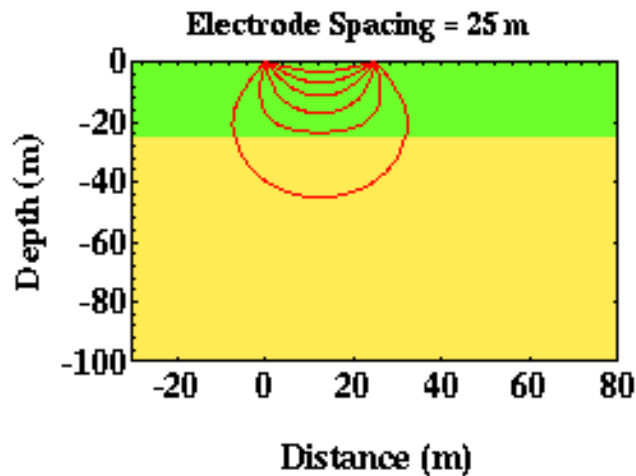
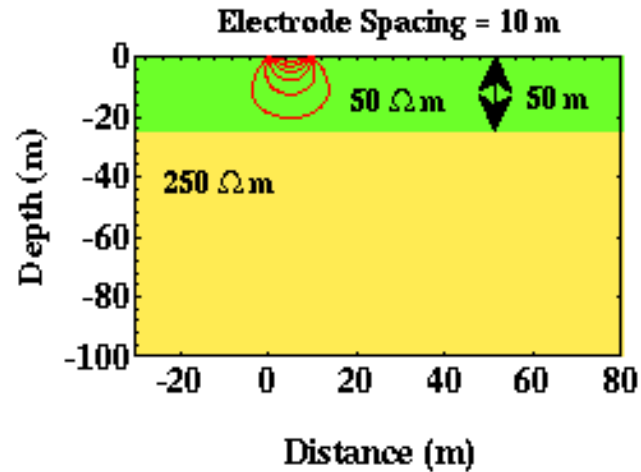
# Current Flow in Layered Media Versus Electrode Spacing: Example 1



# Current Flow in Layered Media Versus Electrode Spacing: Example 1



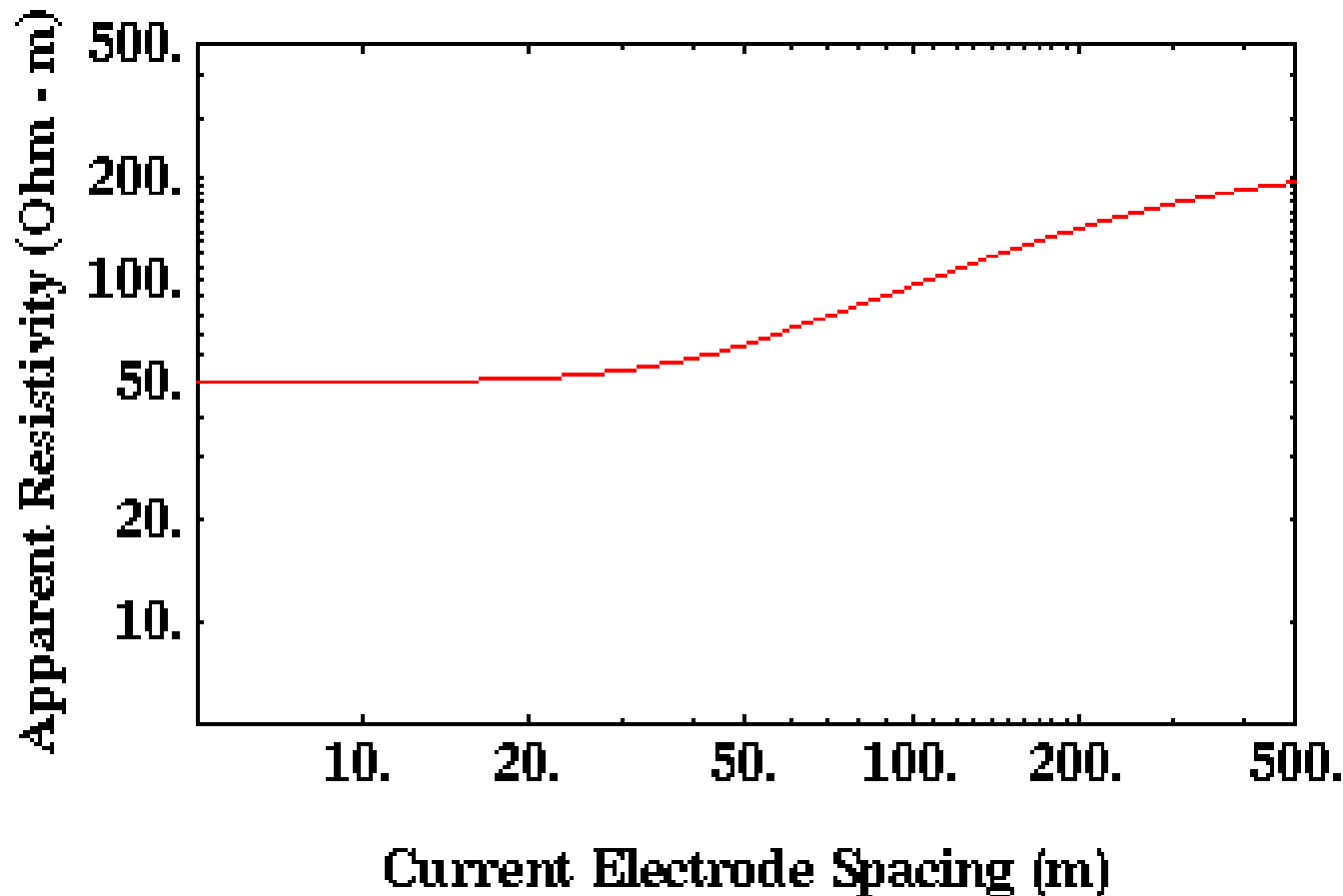
# Current Flow in Layered Media Versus Electrode Spacing: Example 2



Source: <http://galitzin.mines.edu/INTROGP/>

# Current Flow in Layered Media Versus Electrode Spacing: Example 2

Low Resistivity Layer



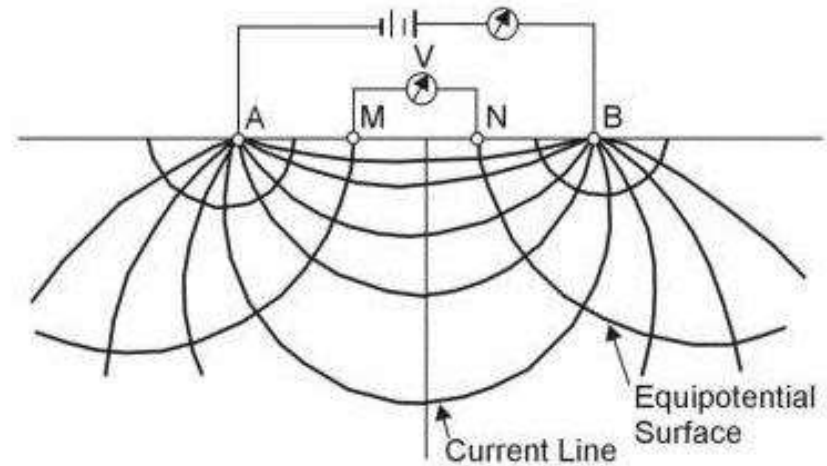


# **PART 4 – Resistivity Equipment and Field Procedures**

1. DC Resistivity Equipment
2. Survey Types Overview: Soundings and Profiles
3. Soundings: Wenner and Schlumberger
4. Electrode Spacings and Apparent Resistivity Plots
5. Advantages and Disadvantages of Wenner and Schlumberger Arrays
6. Resistivity Profiles

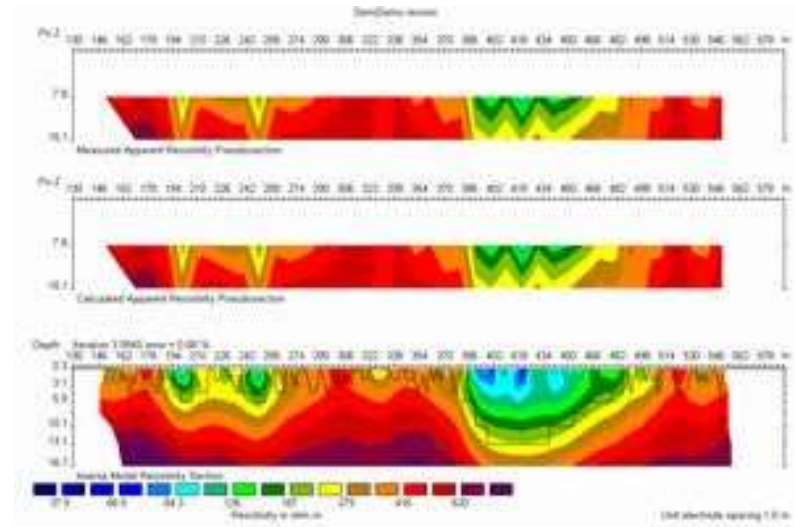
# DC Resistivity Equipment

1. Current Source
2. Ammeter
3. Voltmeter
4. Electrodes
5. Cables



Source: <http://www.iris-instruments.com>

# DC Resistivity Equipment – ABEM Terrameter





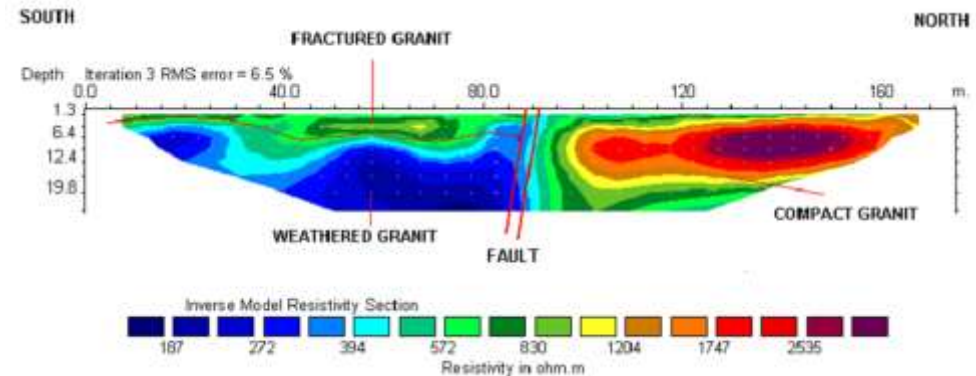
# DC Resistivity Equipment – ABEM Terrameter LS



# DC Resistivity Equipment – IRIS SYSCAL

## SYSCAL Pro

1000V, 250W, 2.5A



| PRODUCT name   | power W | voltage V | current A | power converter | IP windows | receiving dipoles | display   |
|----------------|---------|-----------|-----------|-----------------|------------|-------------------|-----------|
| SYSCAL Kid     | 25      | 200       | 0.5       | internal        | 1          | 1                 | alpha num |
| SYSCAL Junior  | 100     | 400       | 1.2       | internal        | 4          | 1                 | alpha num |
| SYSCAL R1 Plus | 200     | 600       | 2.5       | internal        | 4          | 1                 | alpha num |
| SYSCAL R2      | 250     | 800       | 2.5       | DC/DC ext       | 4          | 1                 | alpha num |
| »              | 1200    | »         | »         | AC/DC ext       | »          | »                 | »         |
| SYSCAL Pro     | 250     | 1000      | 2.5       | internal        | 20         | 10                | graphical |
| »              | 500     | 1500      | »         | DC/DC ext       | »          | »                 | »         |

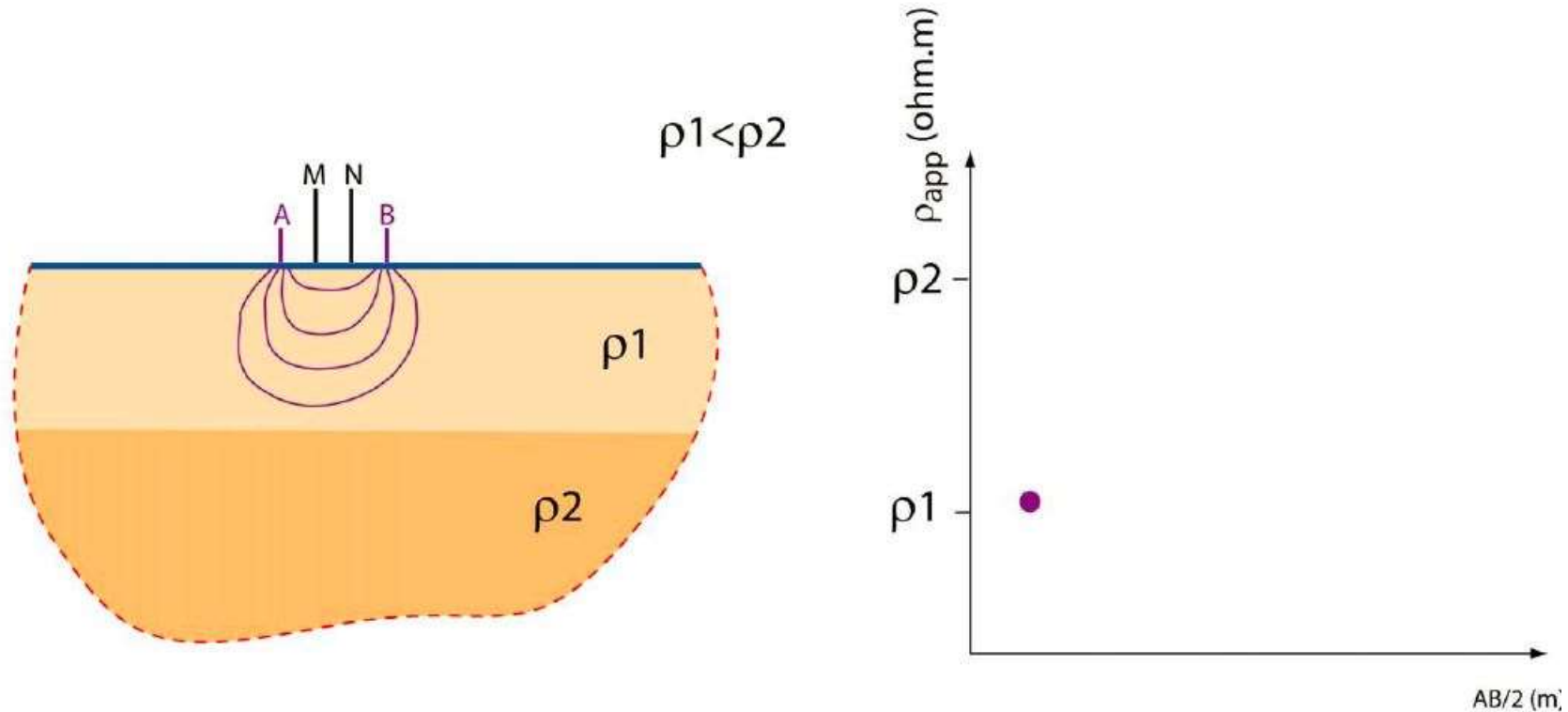
Source: <http://www.iris-instruments.com>

The diagram illustrates a geophysical survey setup. A battery is connected to a galvanometer (represented by a circle with a diagonal arrow) and four electrodes labeled A, M, N, and B. Electrodes A and B are connected to the positive terminal of the battery, while M and N are connected to the negative terminal. The electrodes are placed on the surface of a layered earth model. The layers are represented by different colors and patterns: a top yellow layer, a green layer with dots, a blue layer, and a bottom red layer with crosses. The electrodes are positioned such that A and B are on the surface, while M and N are in the subsurface. The diagram shows the current flow from the battery through the electrodes into the ground.

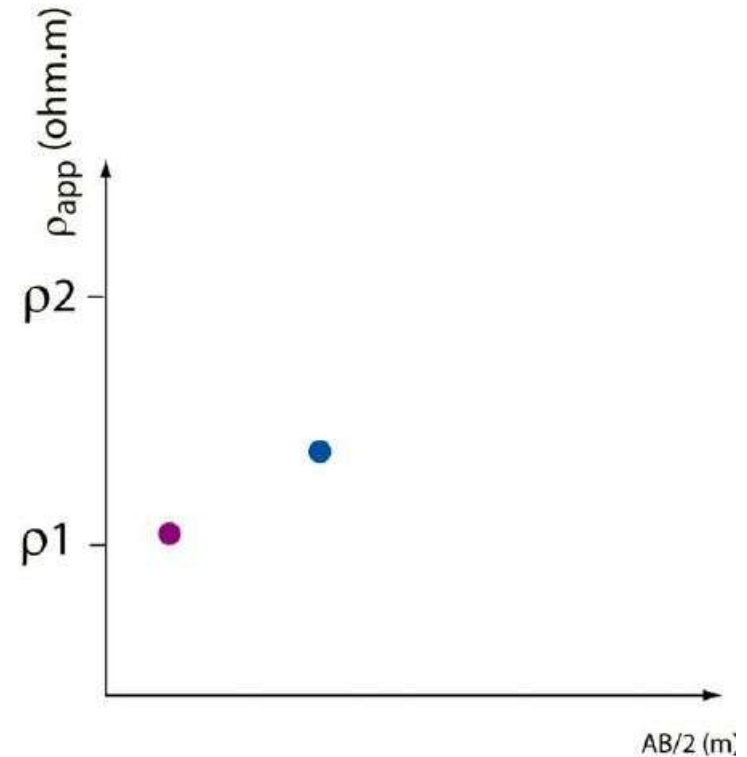
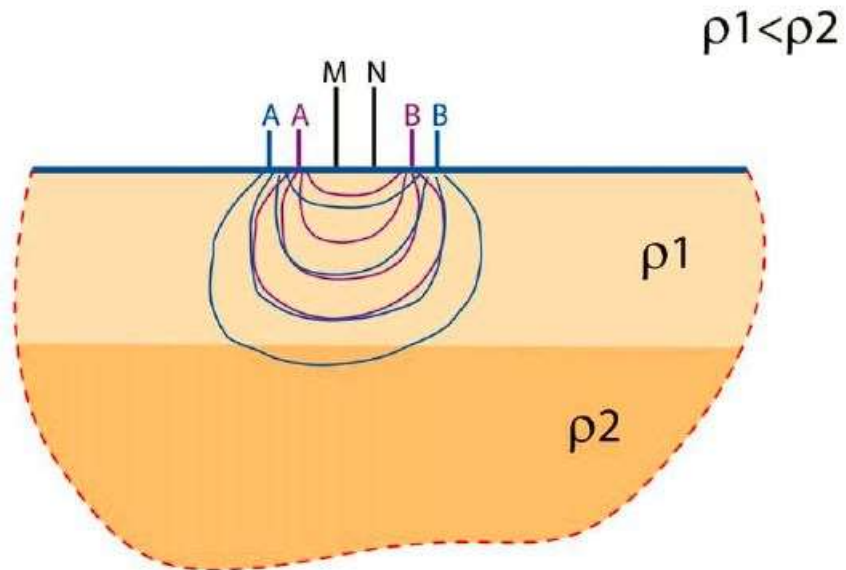




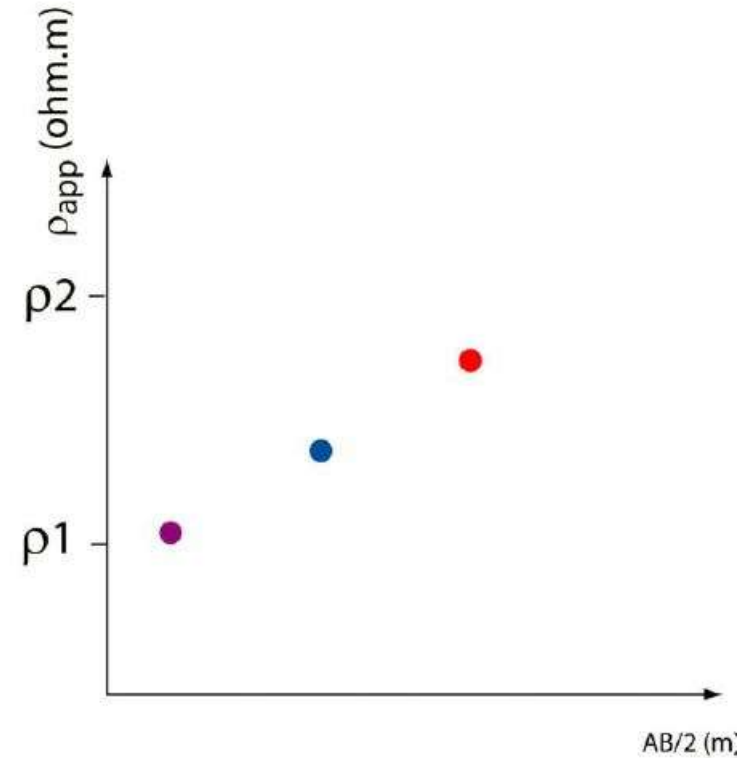
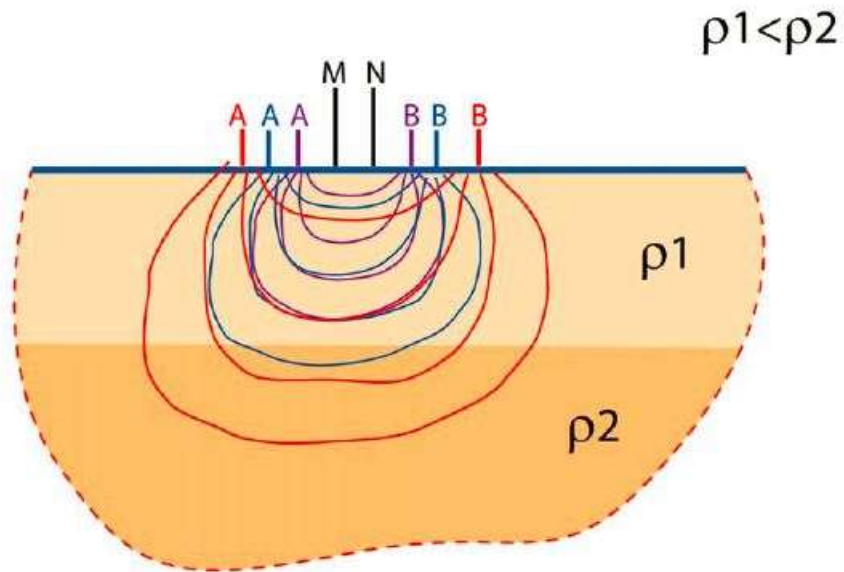
# Vertical Electrical Sounding (VES)



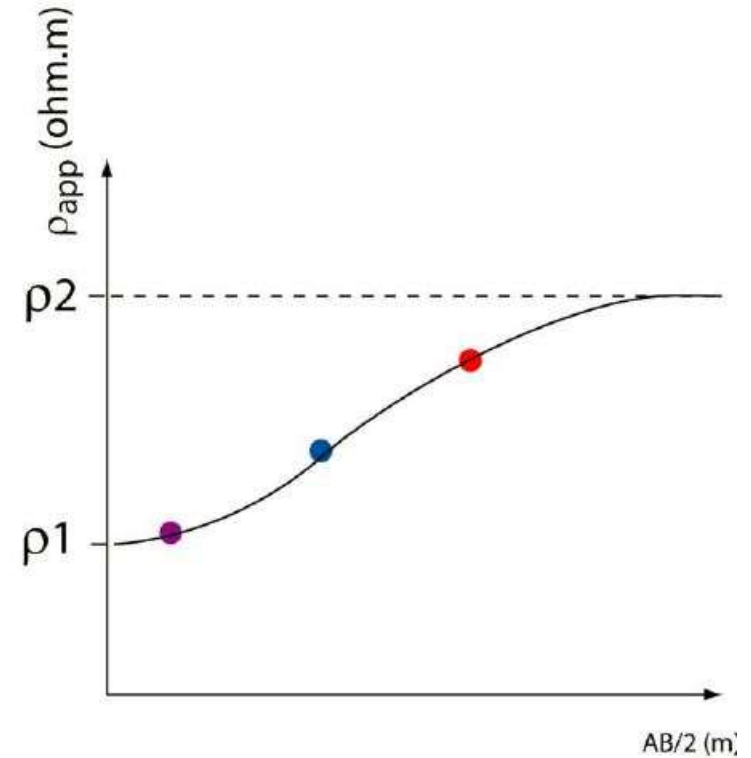
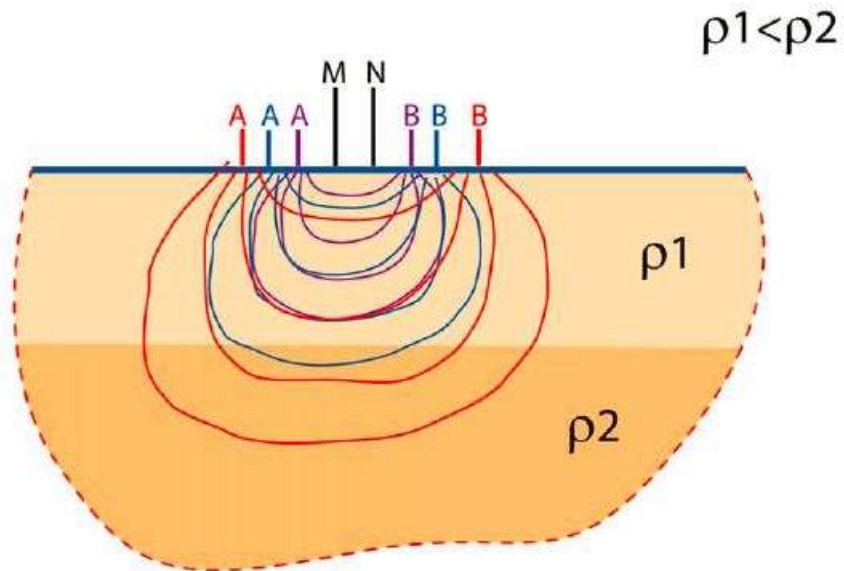
# Vertical Electrical Sounding (VES)



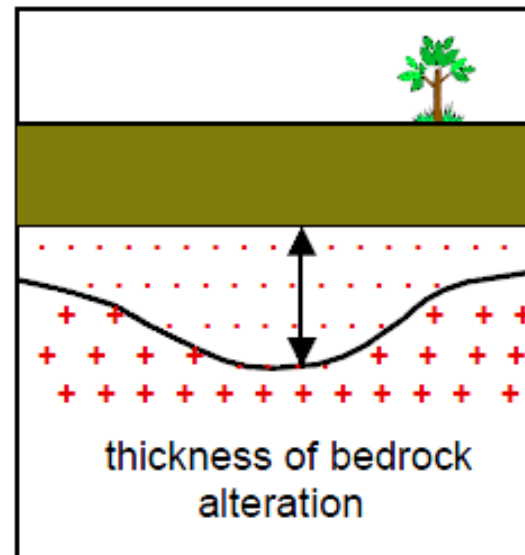
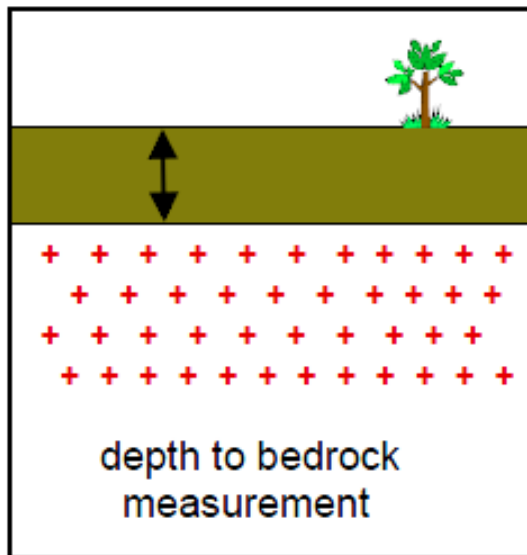
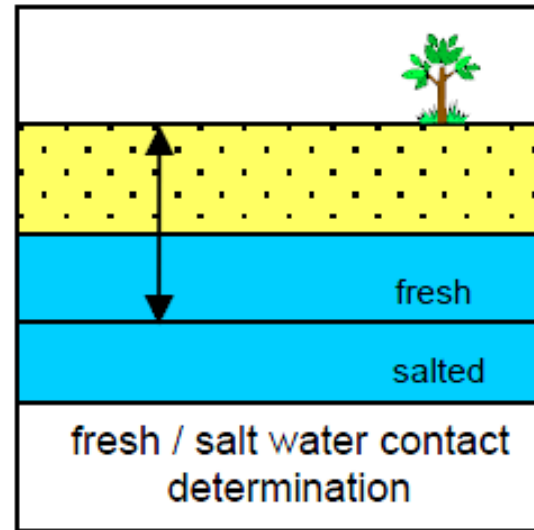
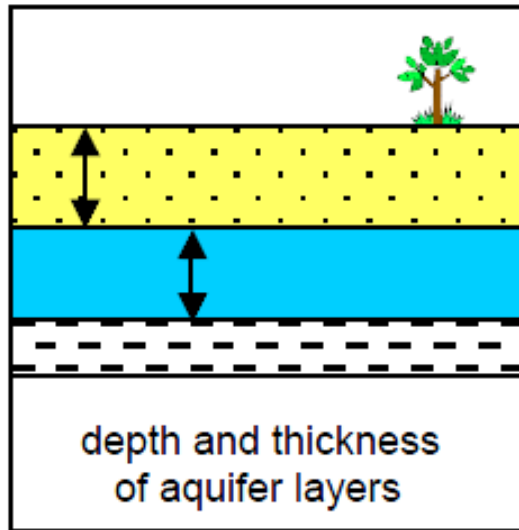
# Vertical Electrical Sounding (VES)



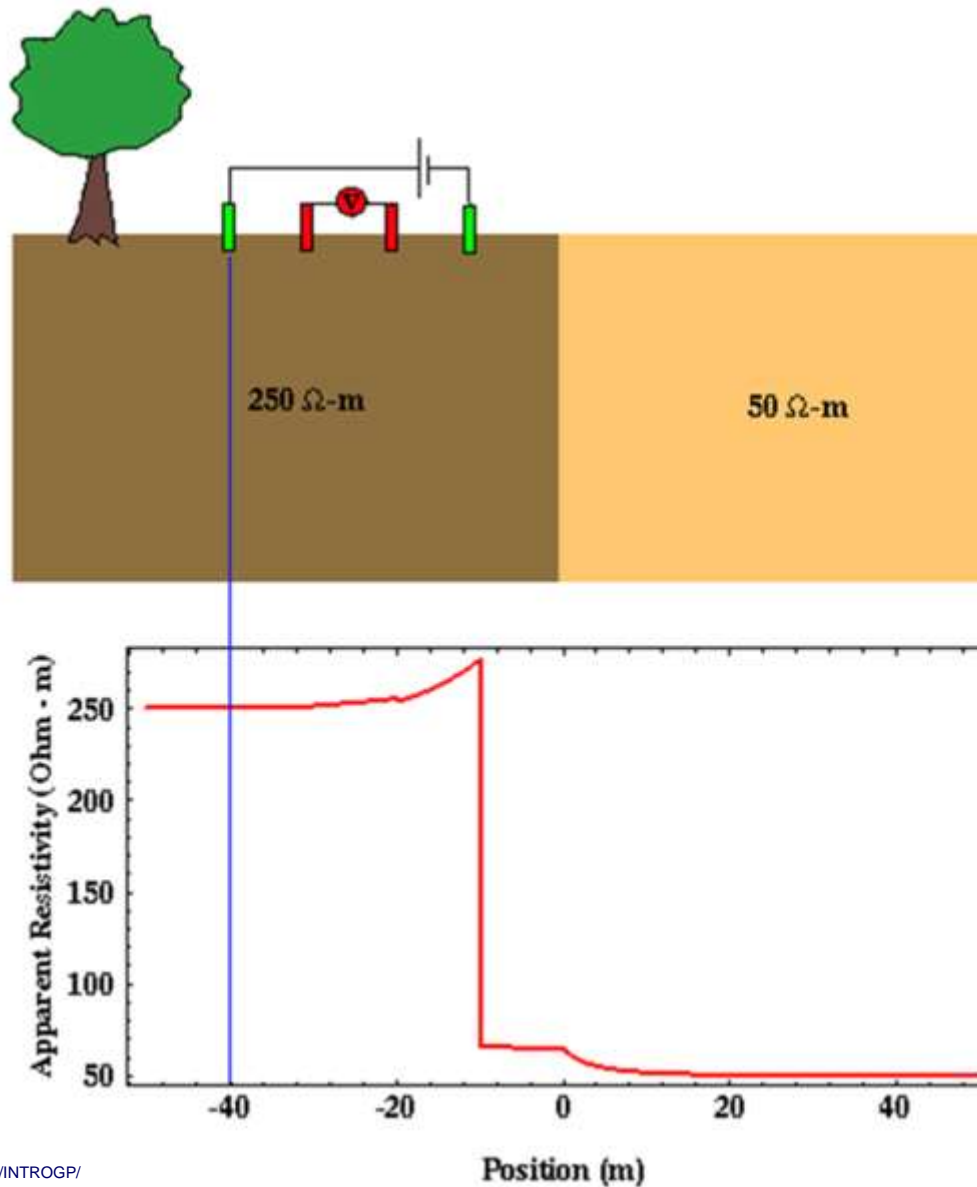
# Vertical Electrical Sounding (VES)



# Applications of Soundings

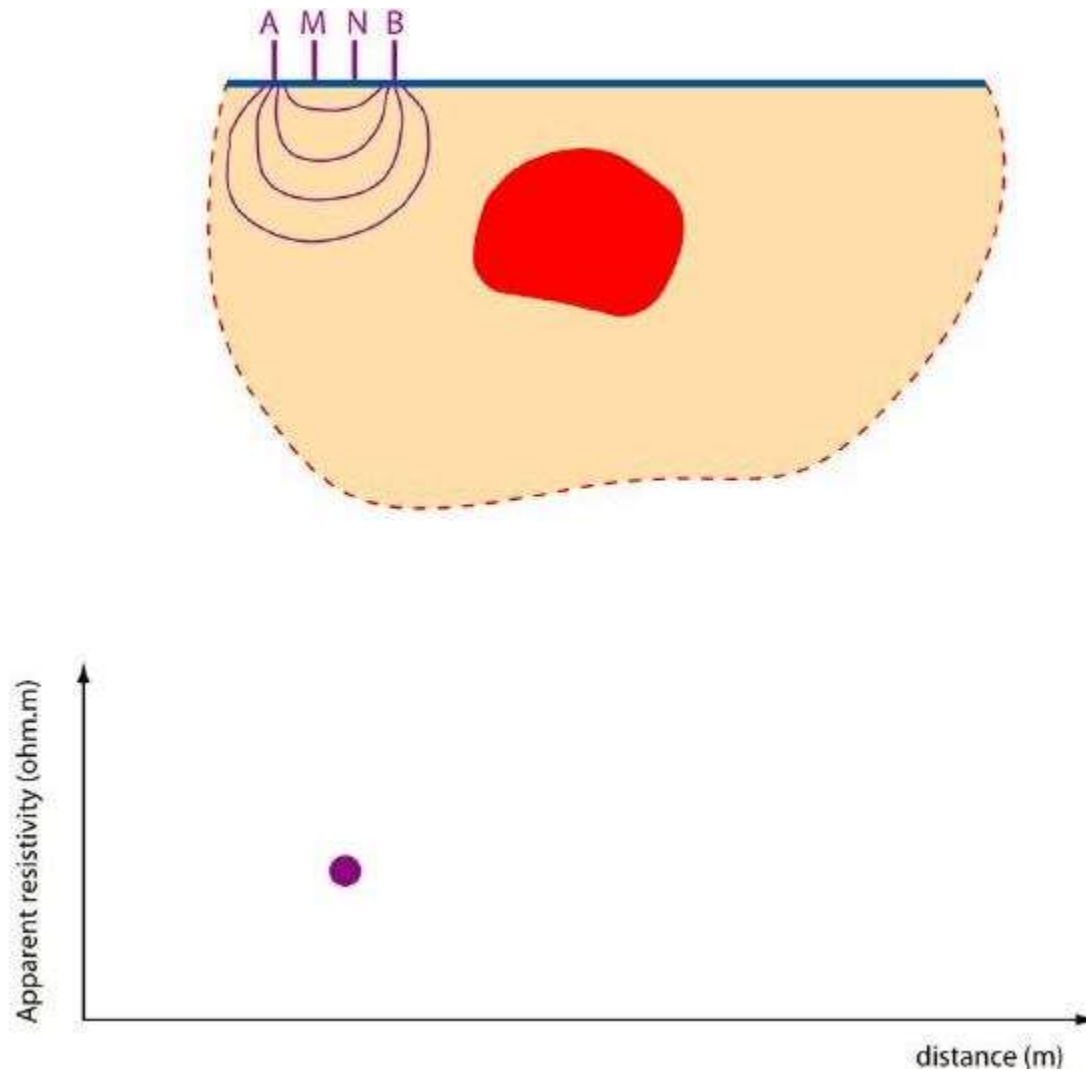


# Survey Types Overview: Profiles



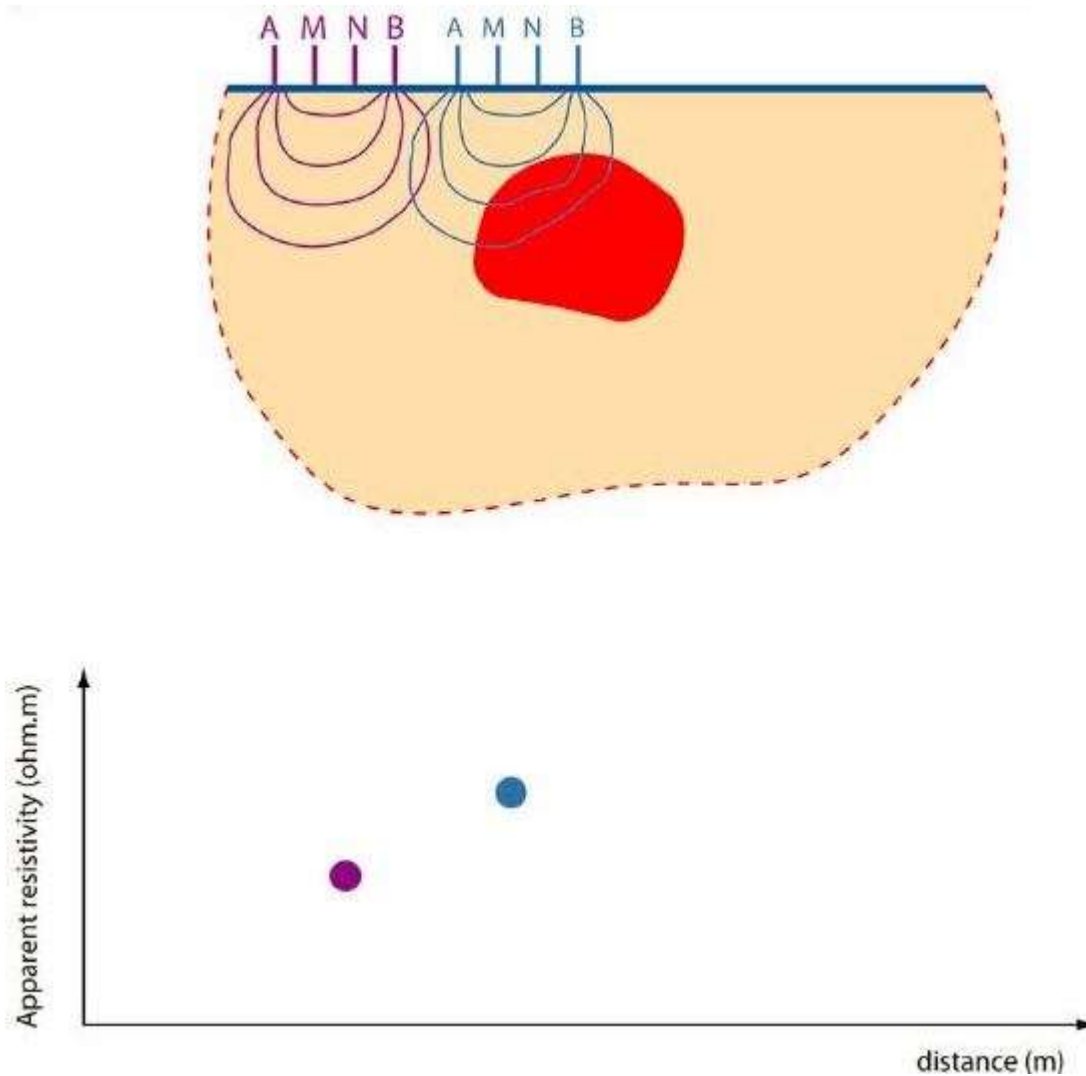


# Constant Separation Traversing (CST)



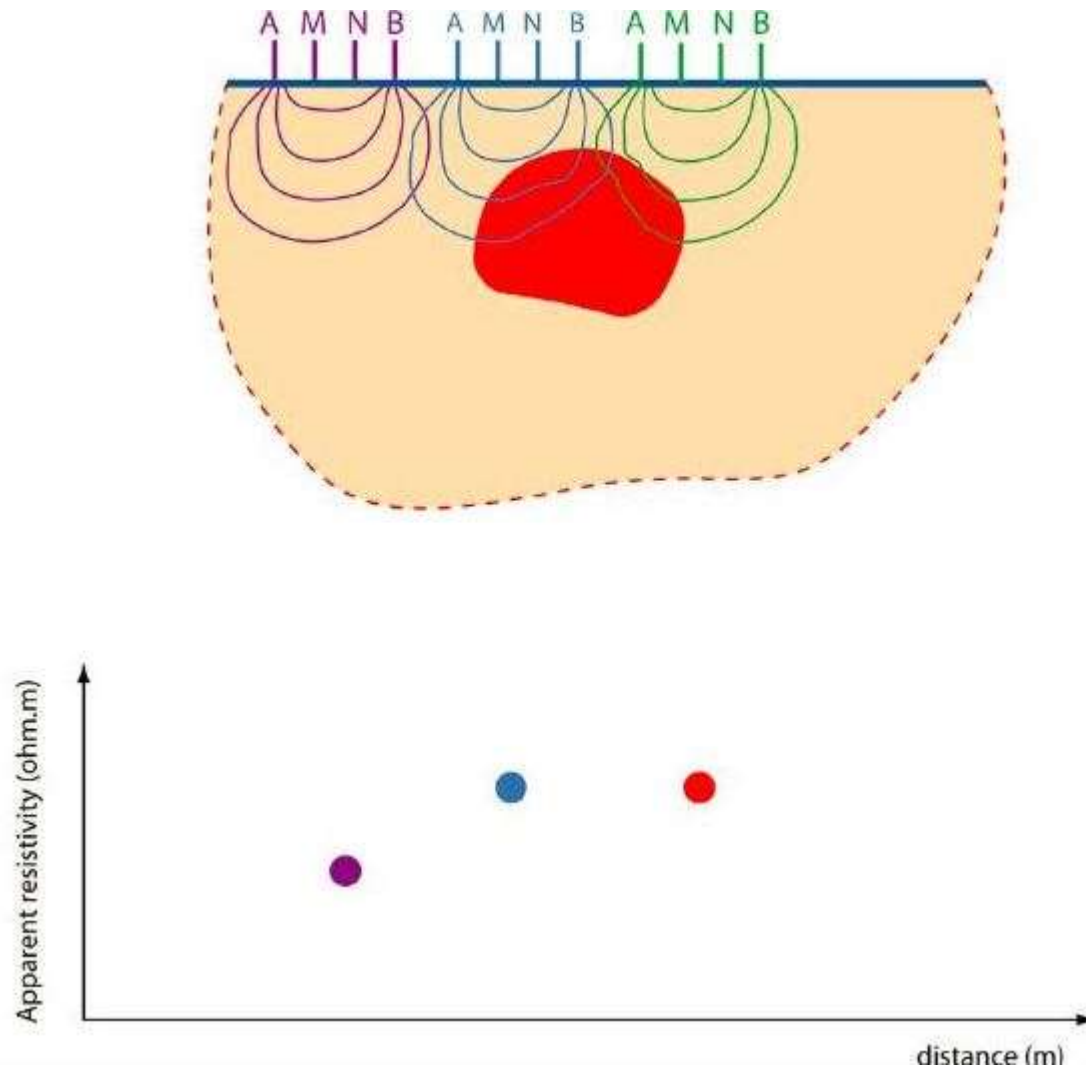
Source: [http://www.tomoquest.com/Lectures\\_in\\_Geophysics.php](http://www.tomoquest.com/Lectures_in_Geophysics.php)

# Constant Separation Traversing (CST)



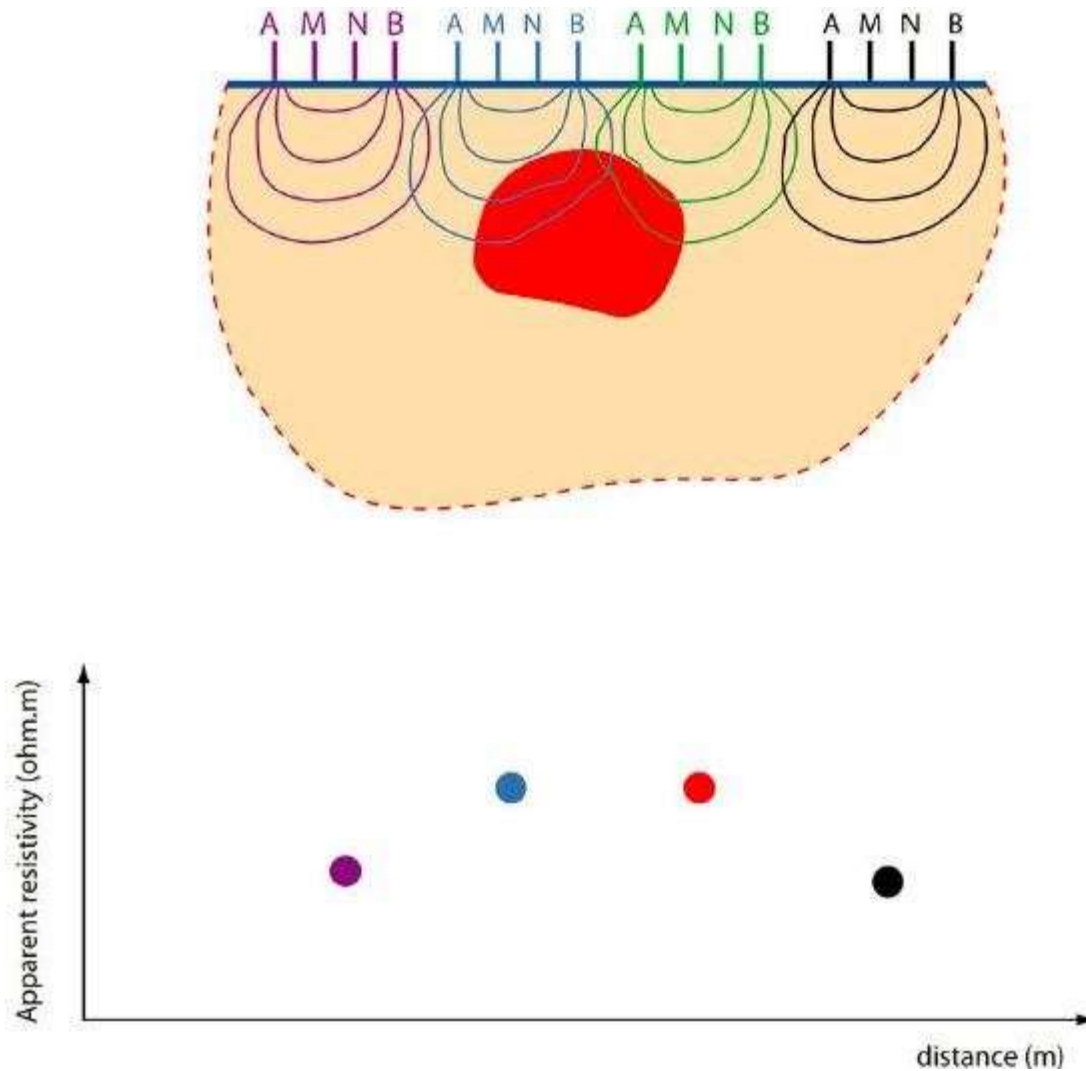
Source: [http://www.tomoquest.com/Lectures\\_in\\_Geophysics.php](http://www.tomoquest.com/Lectures_in_Geophysics.php)

# Constant Separation Traversing (CST)



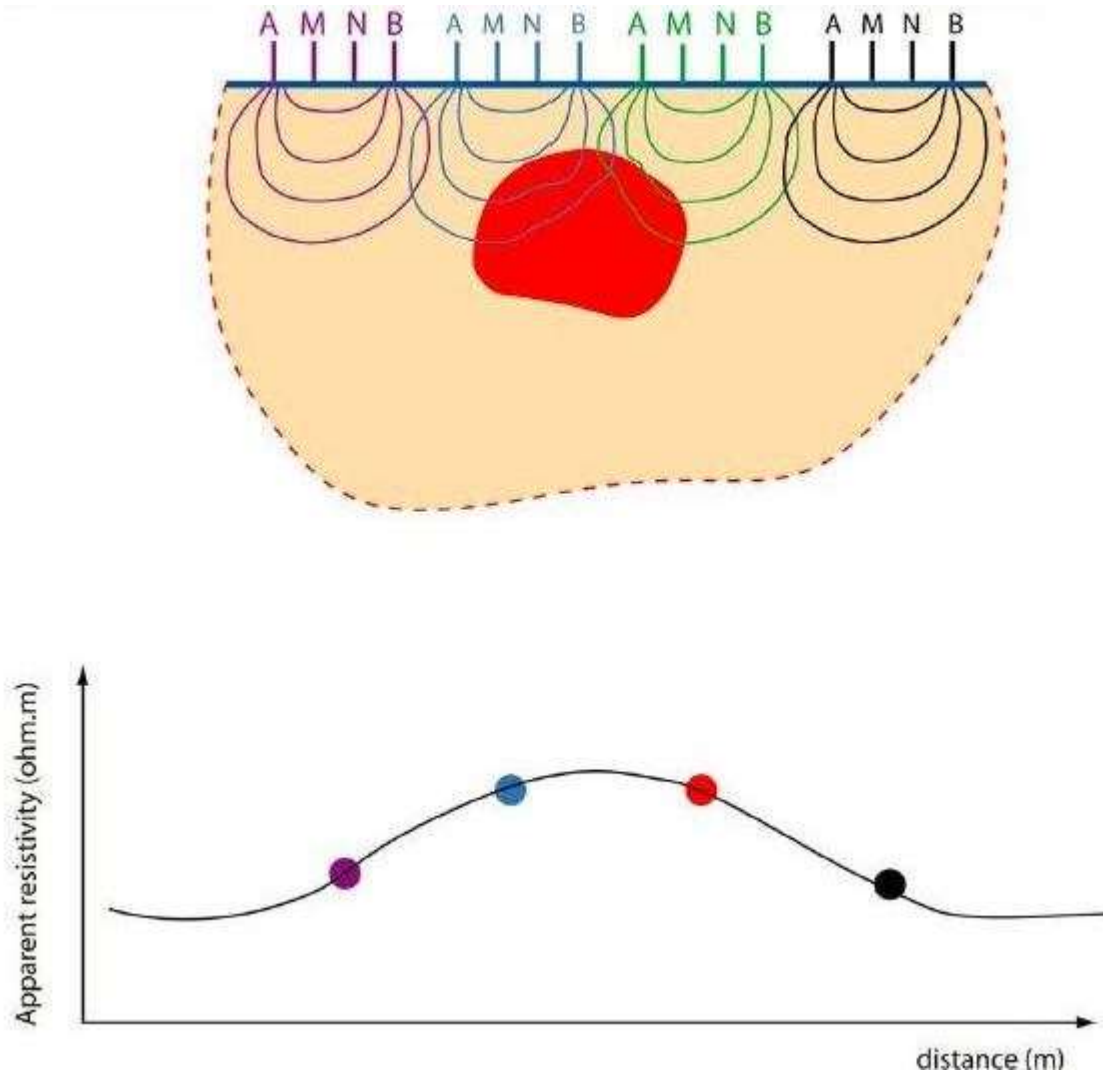
Source: [http://www.tomoquest.com/Lectures\\_in\\_Geophysics.php](http://www.tomoquest.com/Lectures_in_Geophysics.php)

# Constant Separation Traversing (CST)



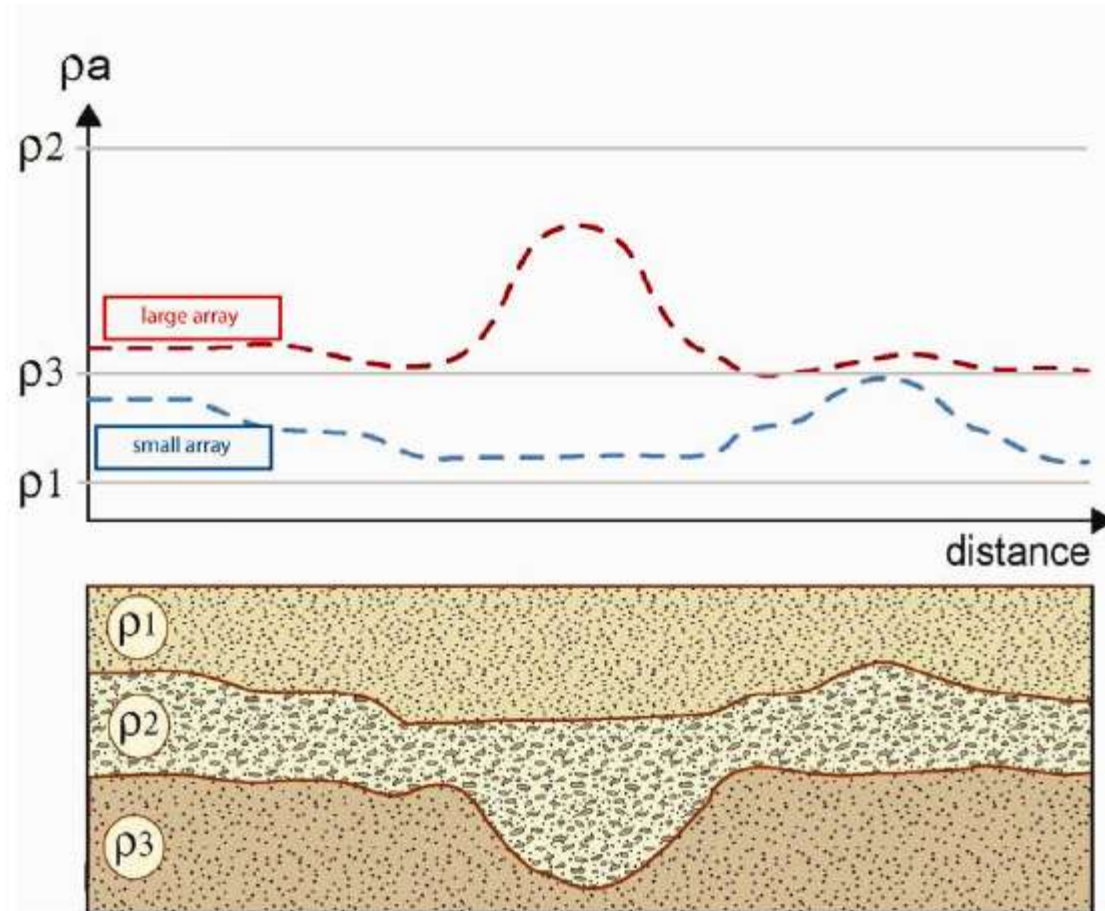
Source: [http://www.tomoquest.com/Lectures\\_in\\_Geophysics.php](http://www.tomoquest.com/Lectures_in_Geophysics.php)

# Constant Separation Traversing (CST)



Source: [http://www.tomoquest.com/Lectures\\_in\\_Geophysics.php](http://www.tomoquest.com/Lectures_in_Geophysics.php)

# Interpretation of CST





# Survey Types Overview: Profiles

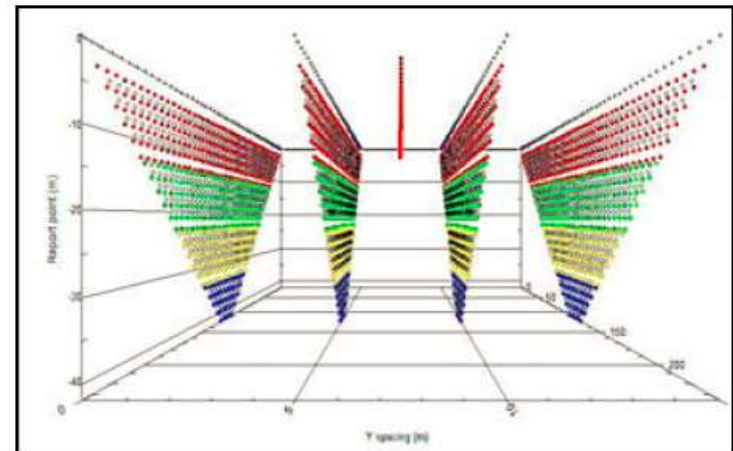
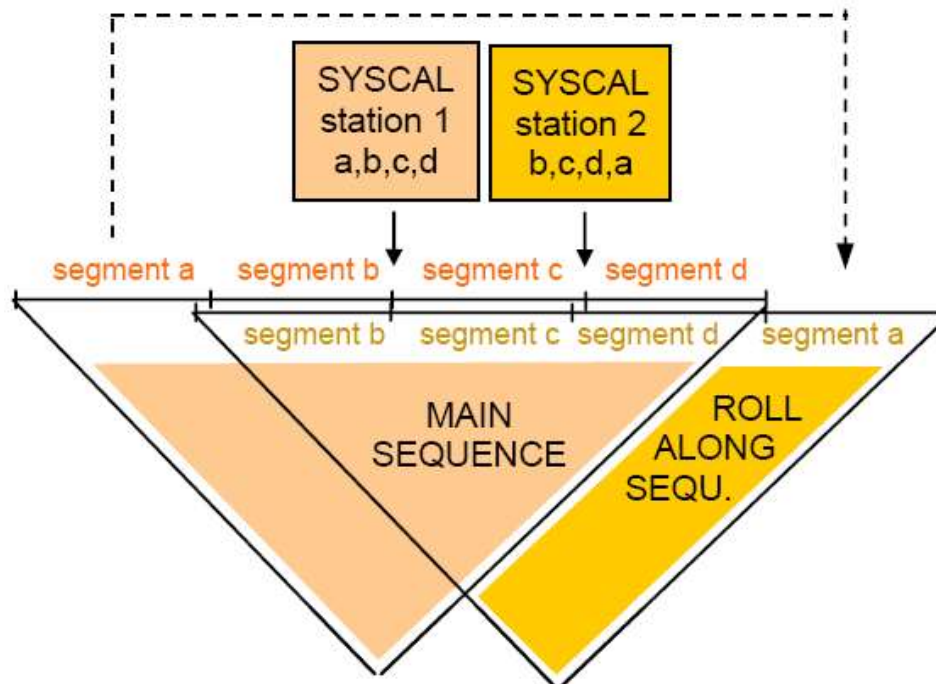
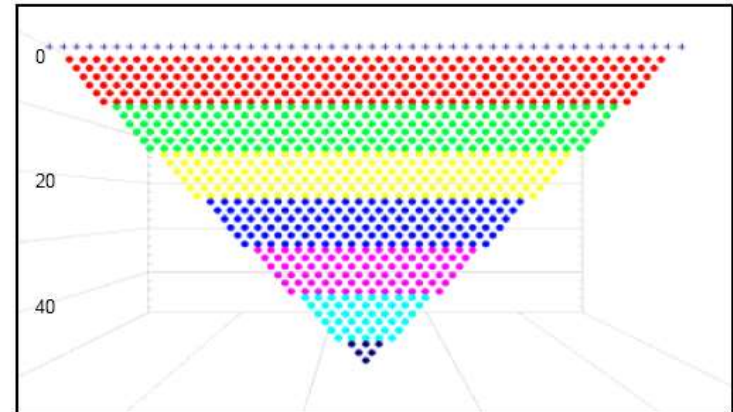


## Geometrics OhmMapper

*OhmMapper being towed over grass and pavement. Contact is made capacitively with the ground through insulated cables.*

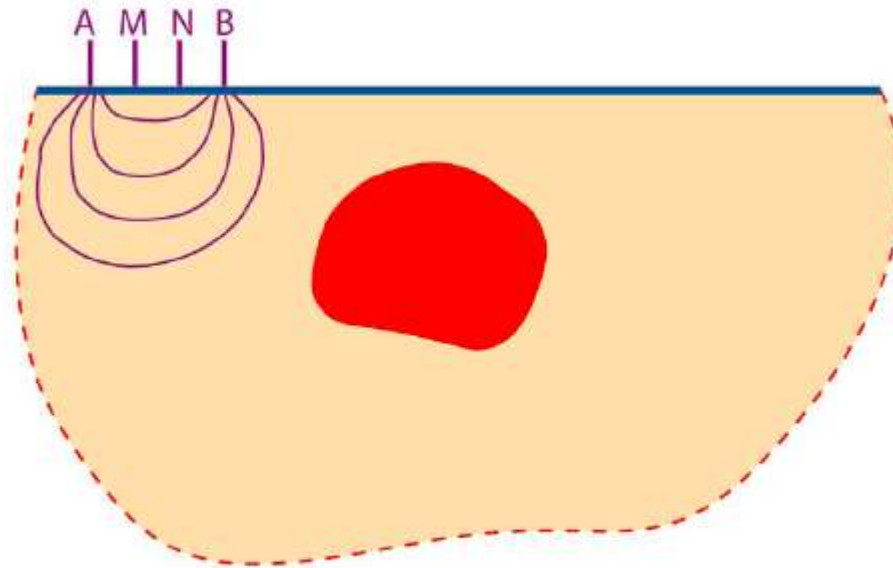
# Survey Types Overview: Resistivity Imaging

SYSCAL Pro  
Switch 48  
multi-electrode  
equipment  
10m spacing

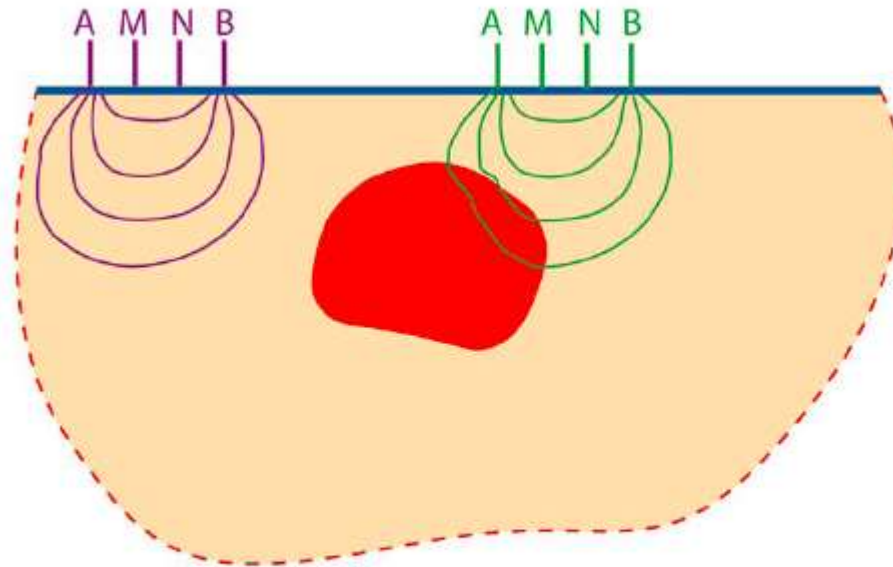


Source: <http://www.iris-instruments.com>

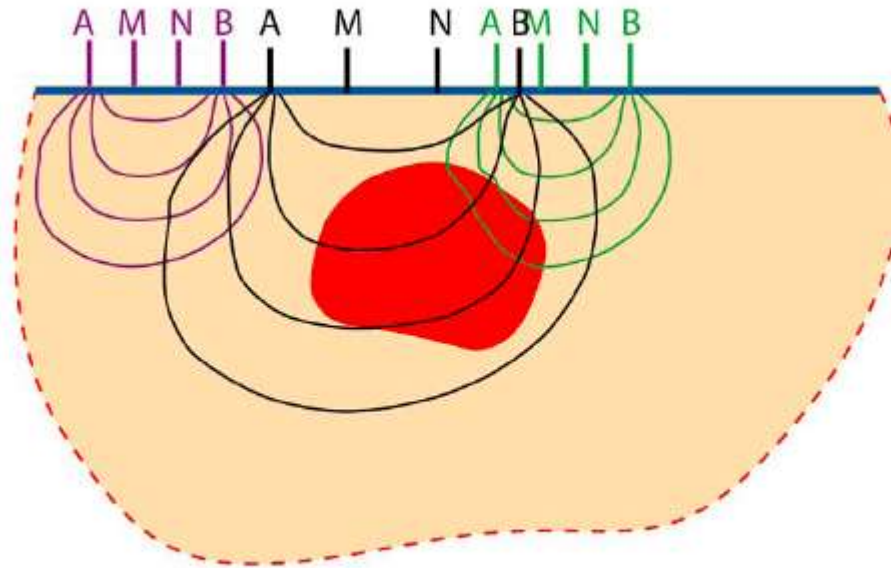
# Resistivity Imaging



# Resistivity Imaging

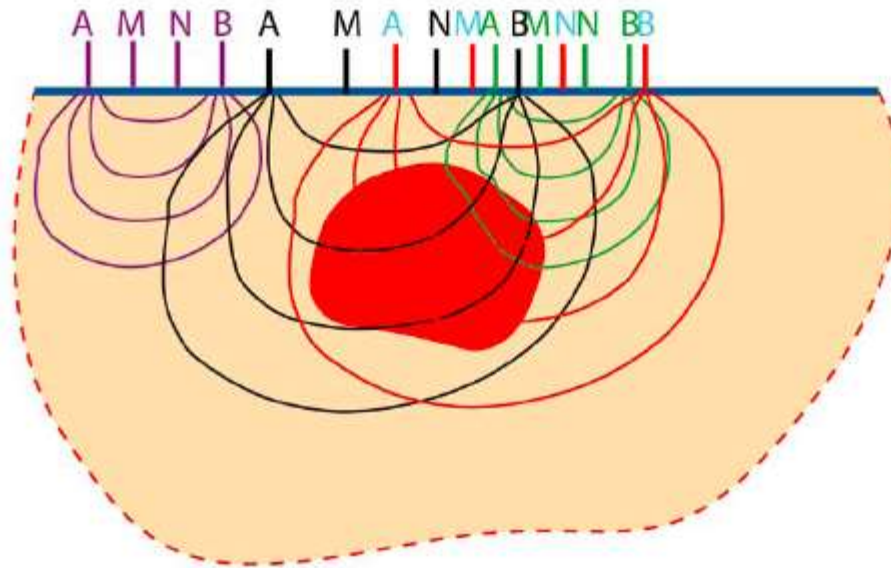


# Resistivity Imaging



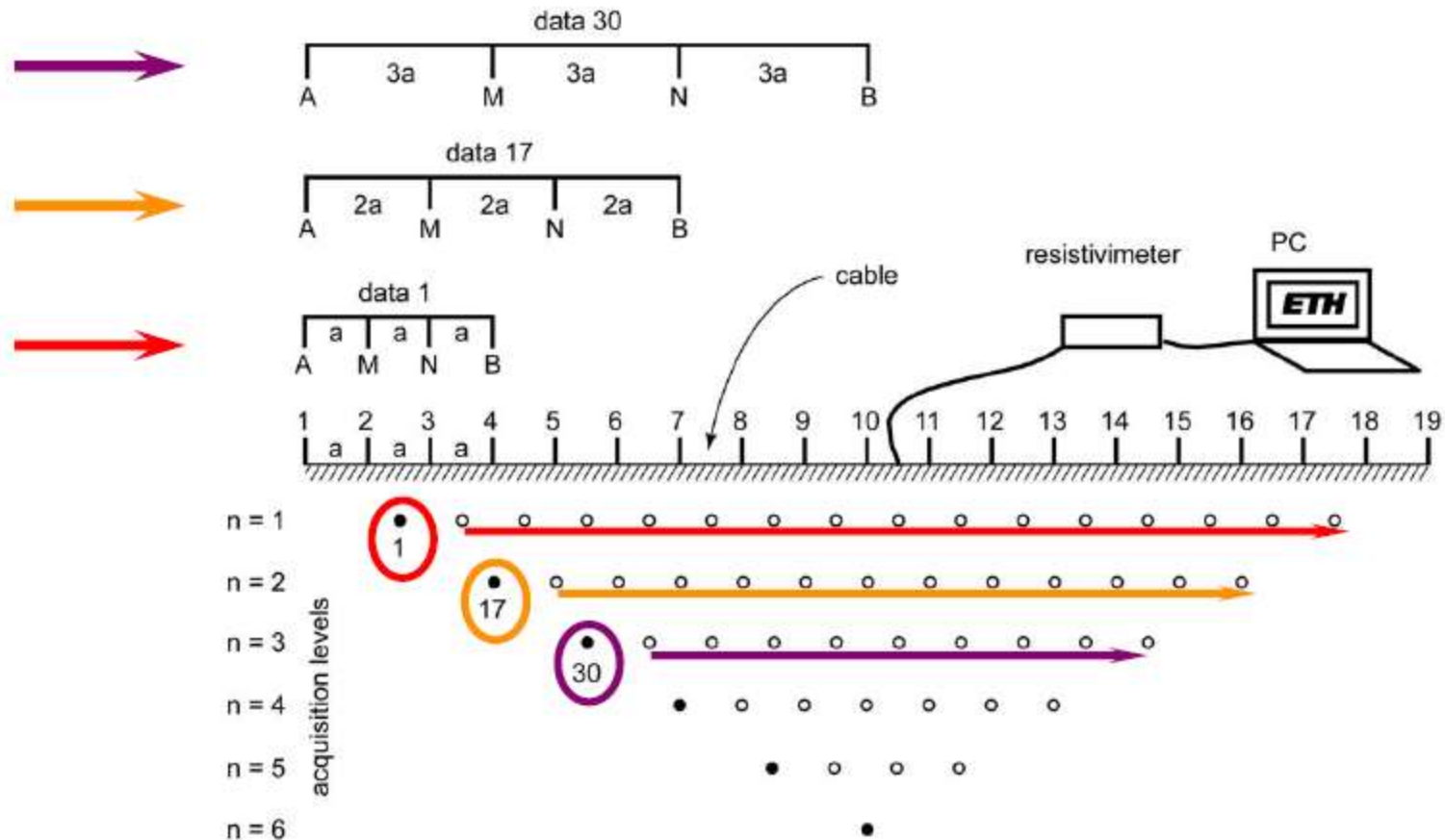


# Resistivity Imaging

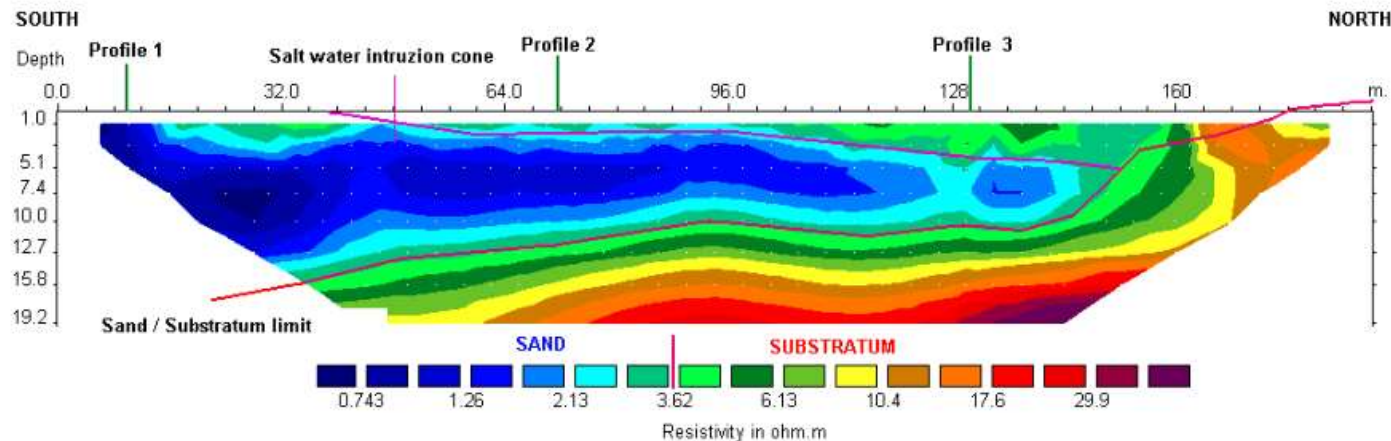
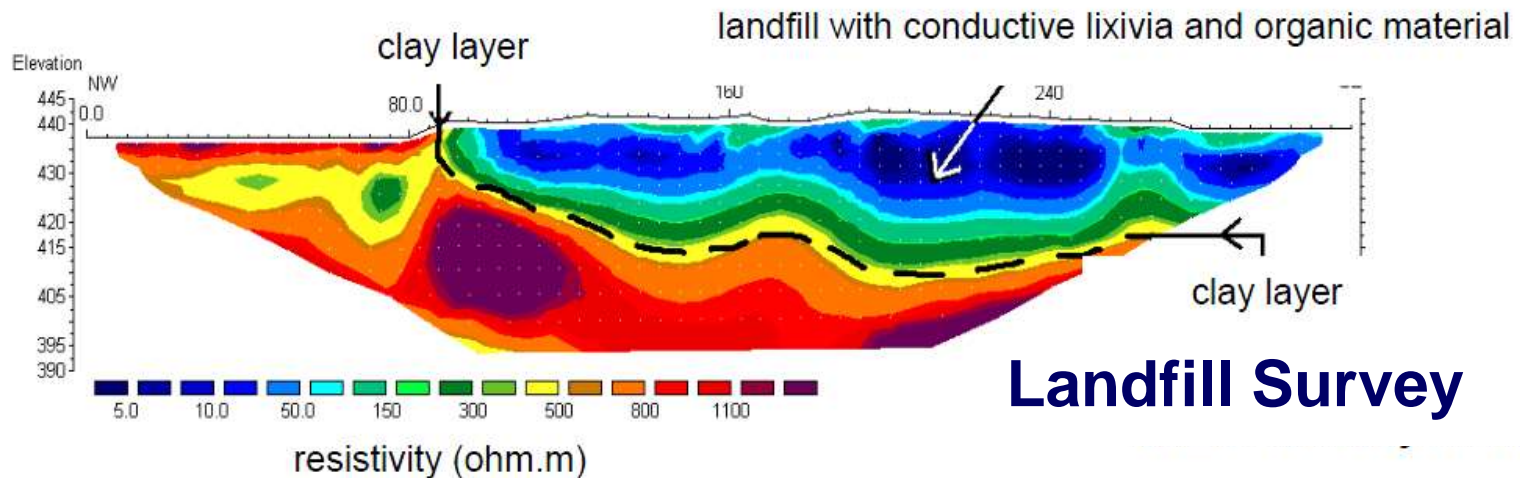




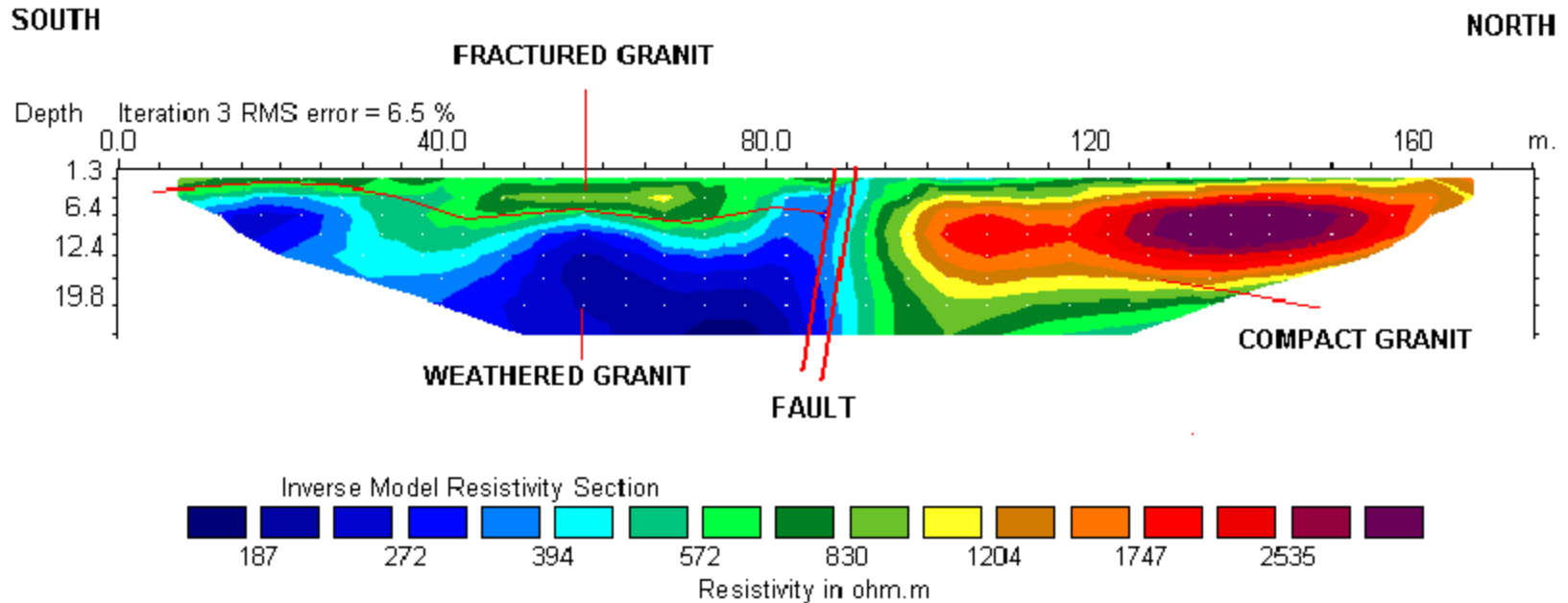
# Resistivity Imaging



# Applications of Resistivity Imaging – 1

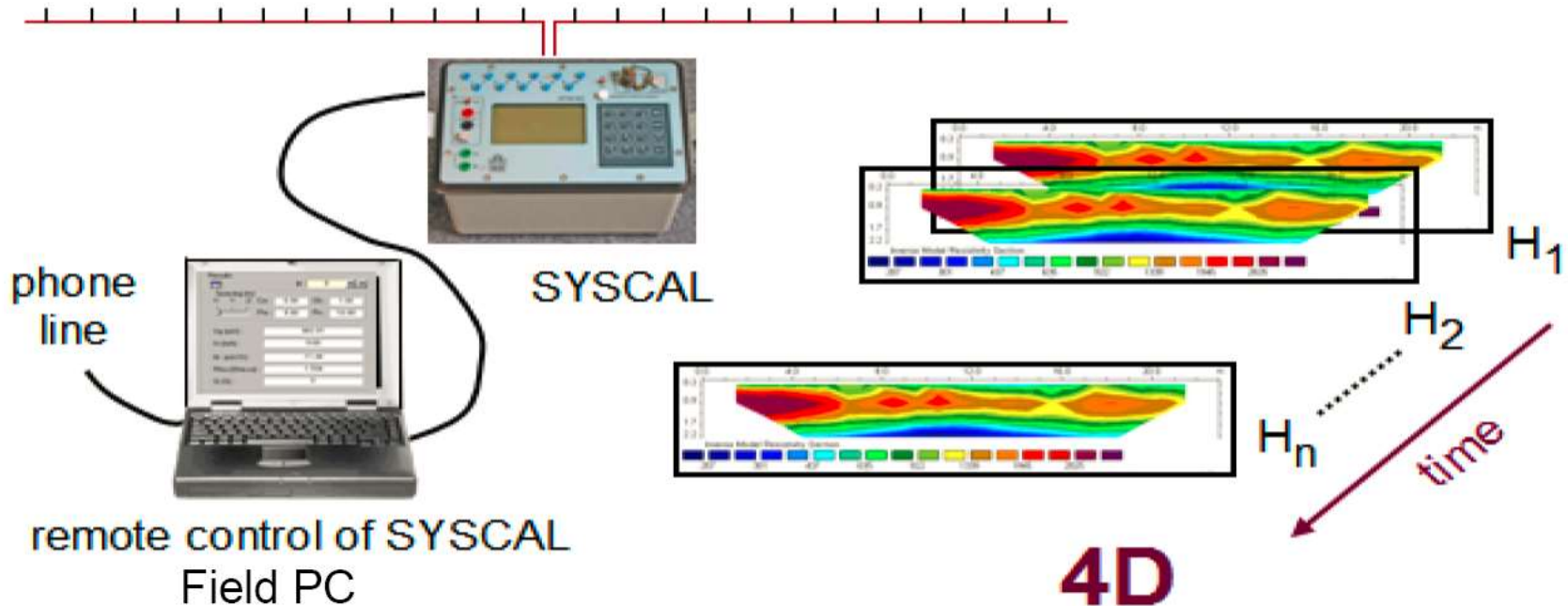


# Applications of Resistivity Imaging – 2



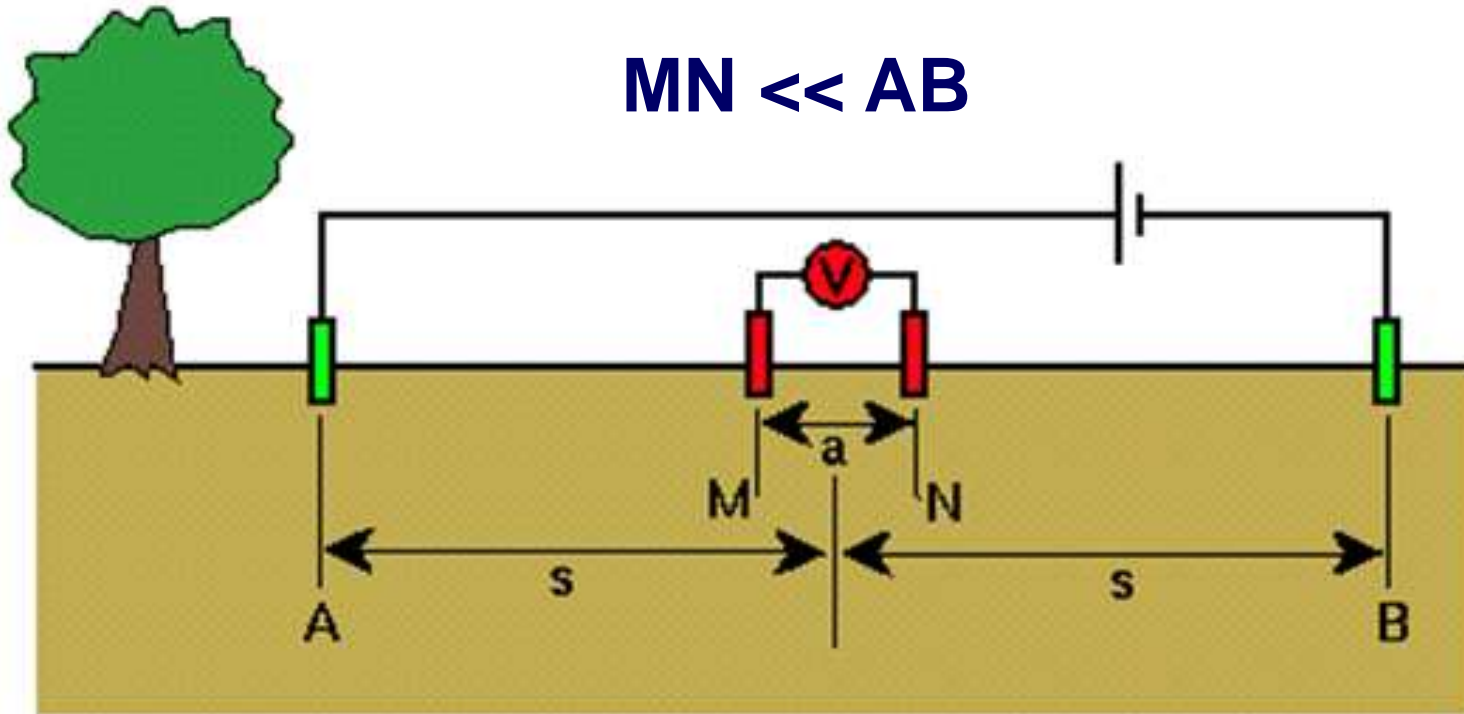
## Fracture Survey

# Survey Types Overview: Resistivity Monitoring



# Main Electrode Arrays: Schlumberger Array

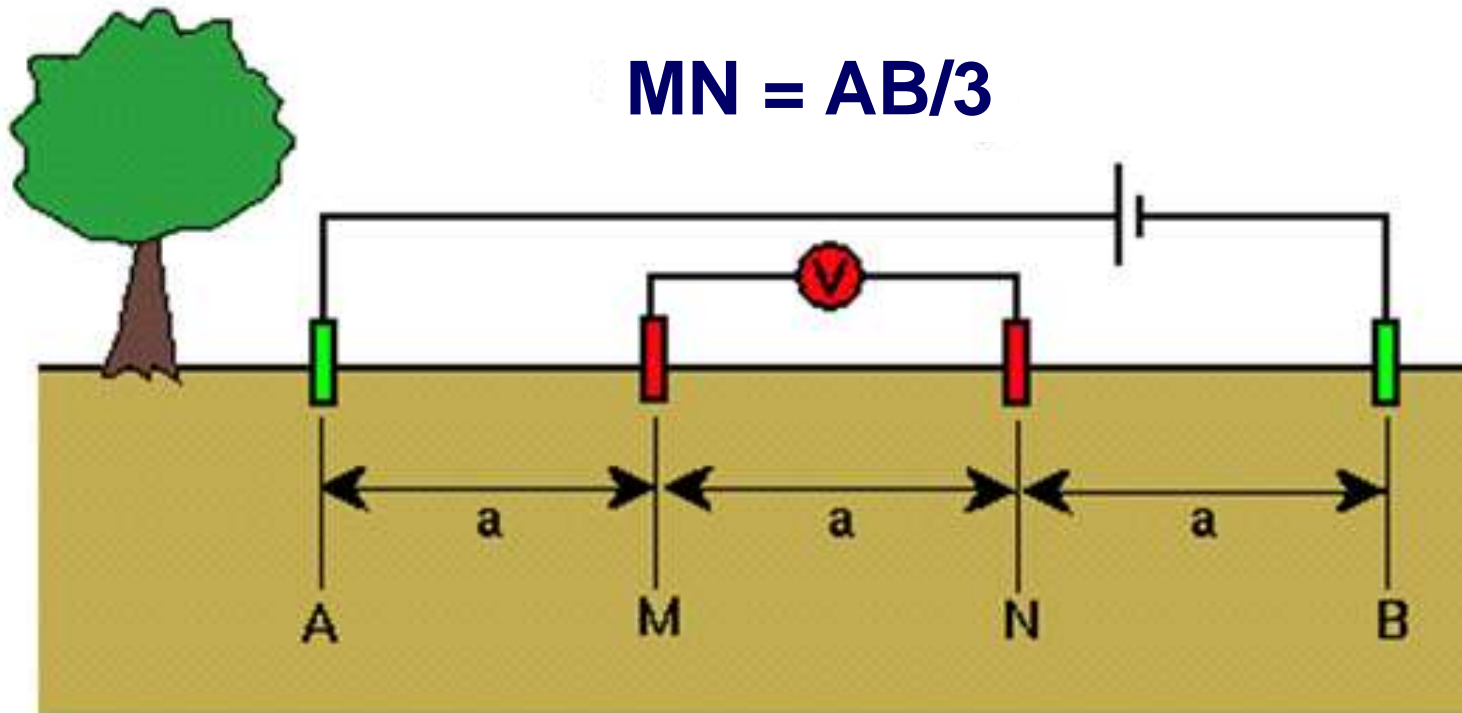
$$MN \ll AB$$



$$\rho_a = \frac{\pi(s^2 - a^2/4) \Delta V}{a i}$$

# Main Electrode Arrays: Wenner Array

$$MN = AB/3$$

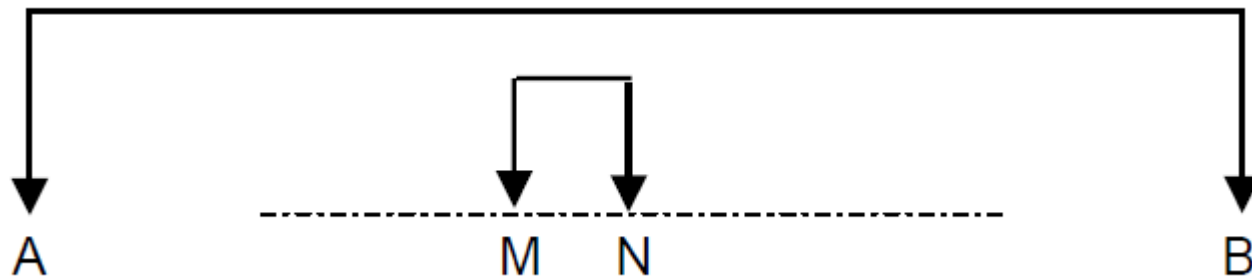


$$\rho_{\alpha} = 2\pi a \frac{\Delta V}{i}$$



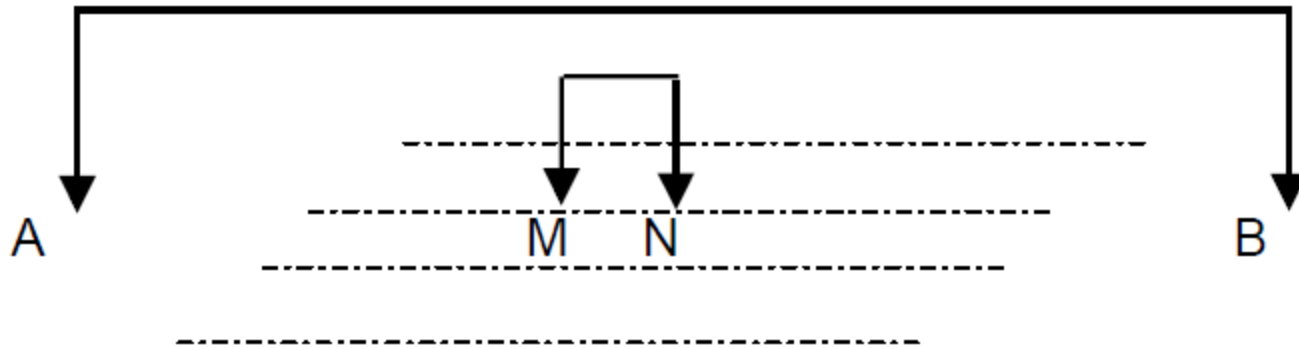
# Main Electrode Arrays: Gradient Array

MN is moved within the middle part of AB



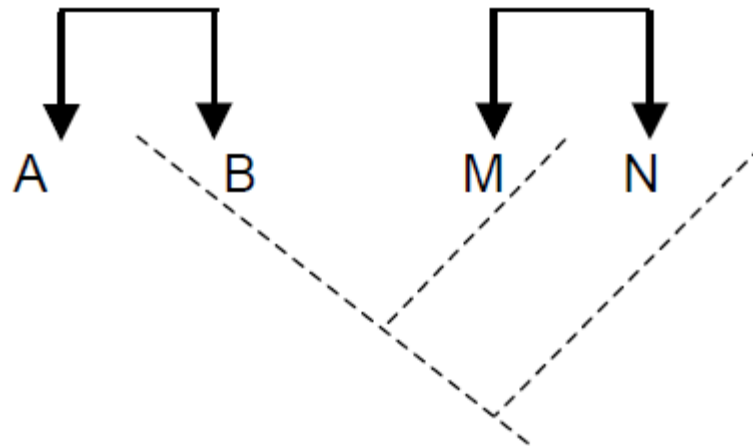
# Main Electrode Arrays: Rectangle Array

MN is moved along various lines parallel to AB

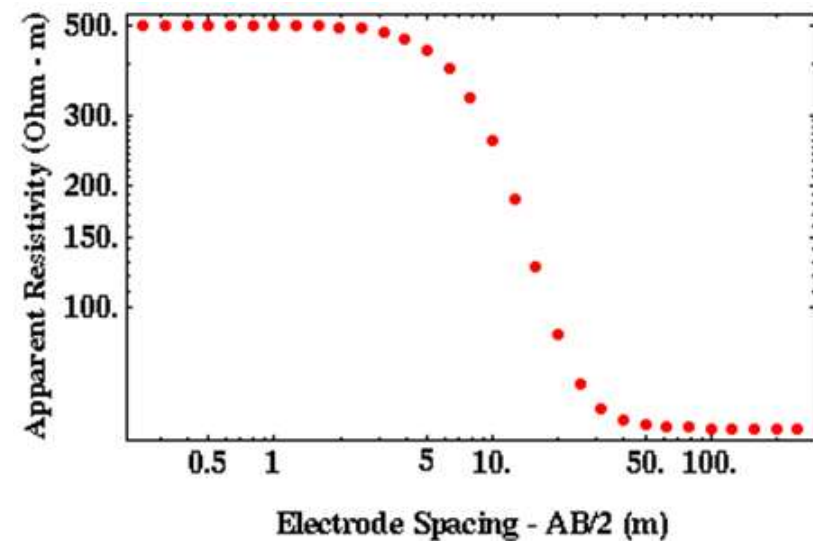
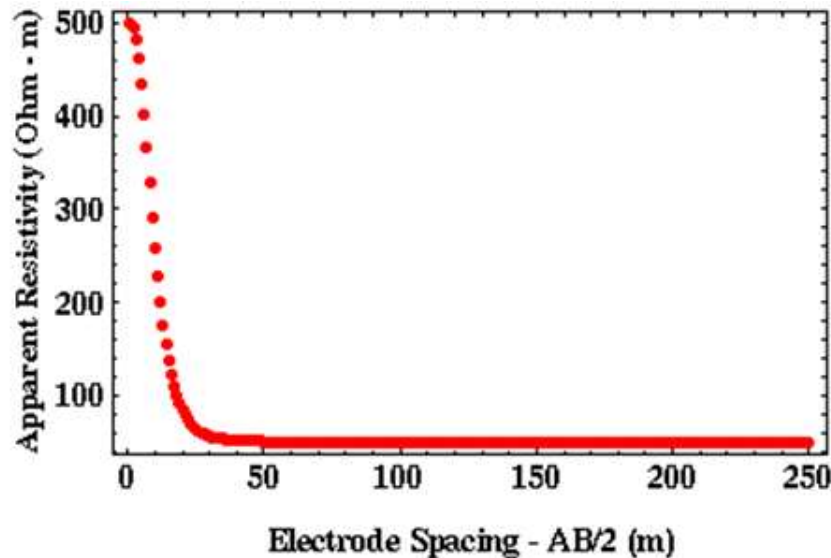
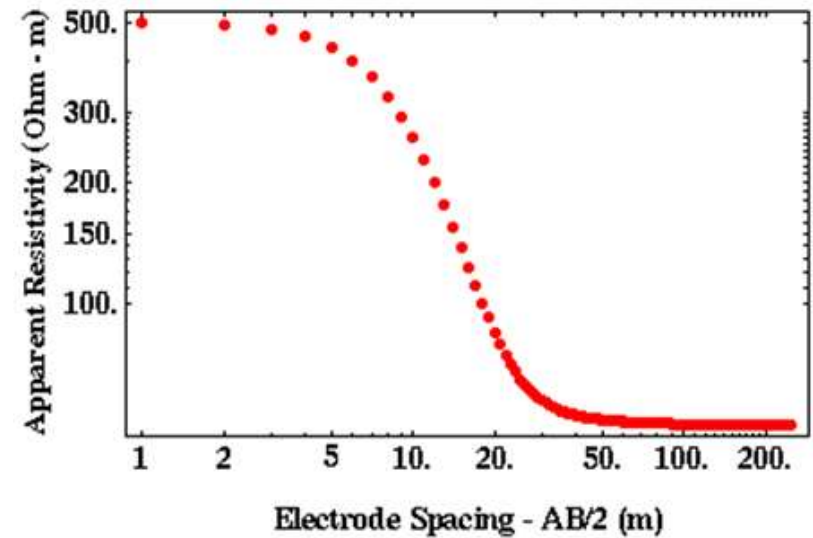
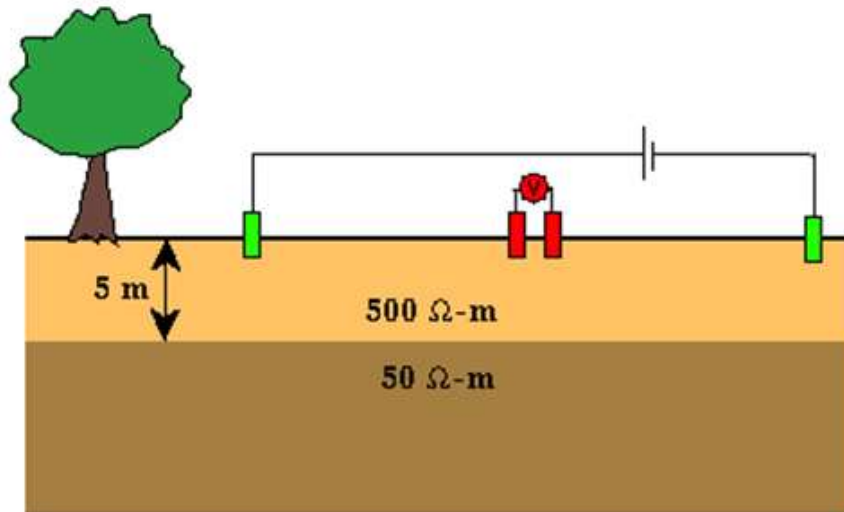


# Main Electrode Arrays: Dipole Dipole Array

MN is moved a certain number of times away from AB, then AB is shifted of one spacing and so on. A pseudo section is obtained, a combination of profiling and shallow sounding



# Electrode Spacings and Apparent Resistivity Plots



# Advantages and Disadvantages of Schlumberger Arrays

| Advantage  | Disadvantage  |
|--|---|
| Need to move the two current electrodes only for most readings. This can significantly decrease the time required to acquire a sounding. | Because the potential electrode spacing is small compared to the current electrode spacing, for large current electrode spacings, very sensitive voltmeters are required. |
| Because the potential electrodes remain in fixed locations, the effects of near-surface lateral variations in resistivity are reduced.   | In general, interpretations based on DC soundings will be limited to simple, horizontally layered structures.   |

# Advantages and Disadvantages of Wenner Arrays

| Advantage   | Disadvantage  |
|---|---|
| Potential electrode spacing increases as current electrode spacing increases. Less sensitive voltmeters are required. | All four electrodes, two current and two potential, must be moved to acquire each reading.  |
|   | Because all electrodes are moved for each reading, this method can be more susceptible to near-surface, lateral variations in resistivity. These near-surface lateral variations could potentially be misinterpreted in terms of depth variations in resistivity. |
|   | In general, interpretations based on DC soundings will be limited to simple, horizontally layered structures.   |

Source: <http://galitzin.mines.edu/INTROGP/>



# Choice of Array

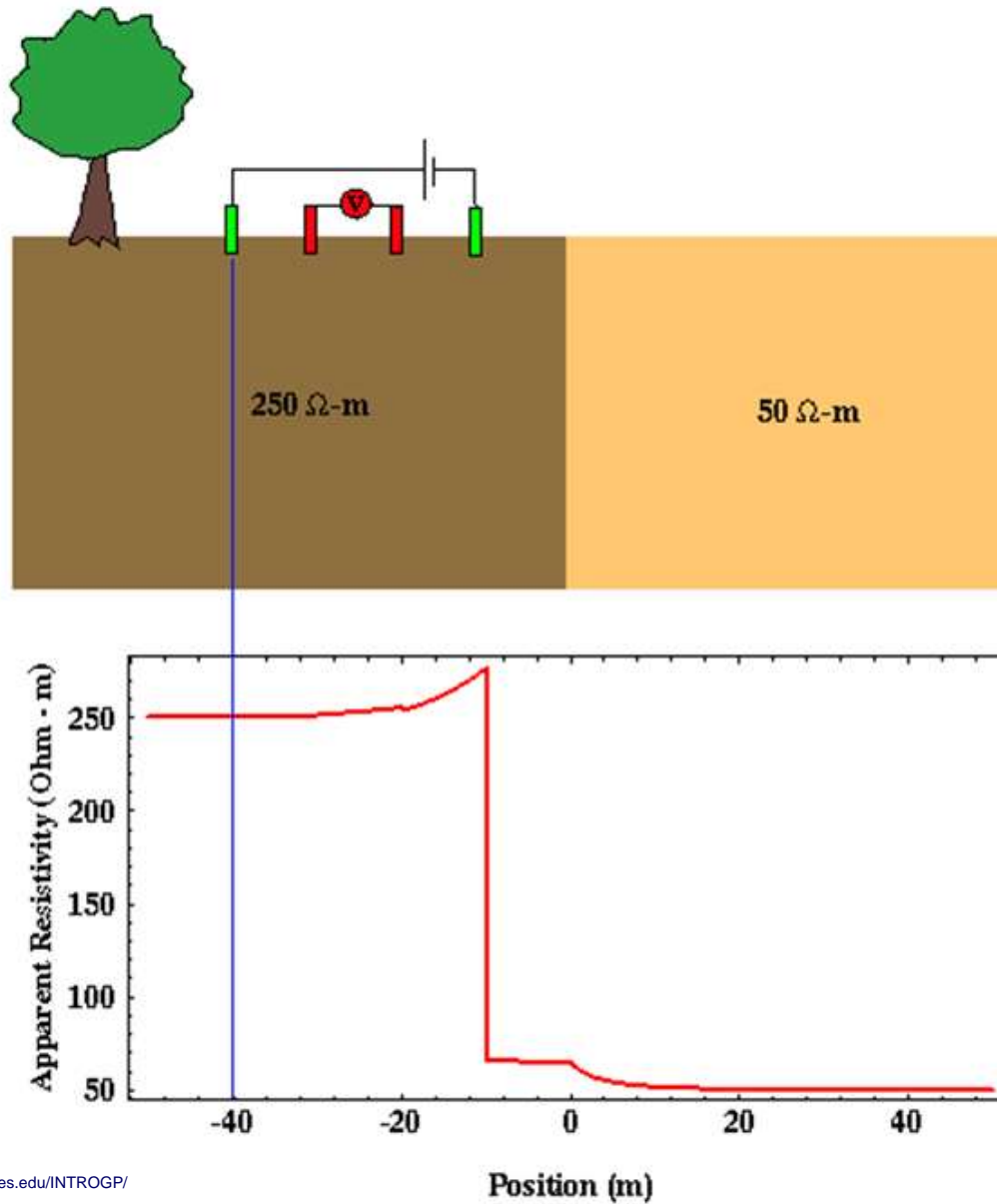
## Key Questions:

- Which type of structure needs to be mapped?
- How sensitive is the resistivity meter?
- What is the background noise level?

## Considerations

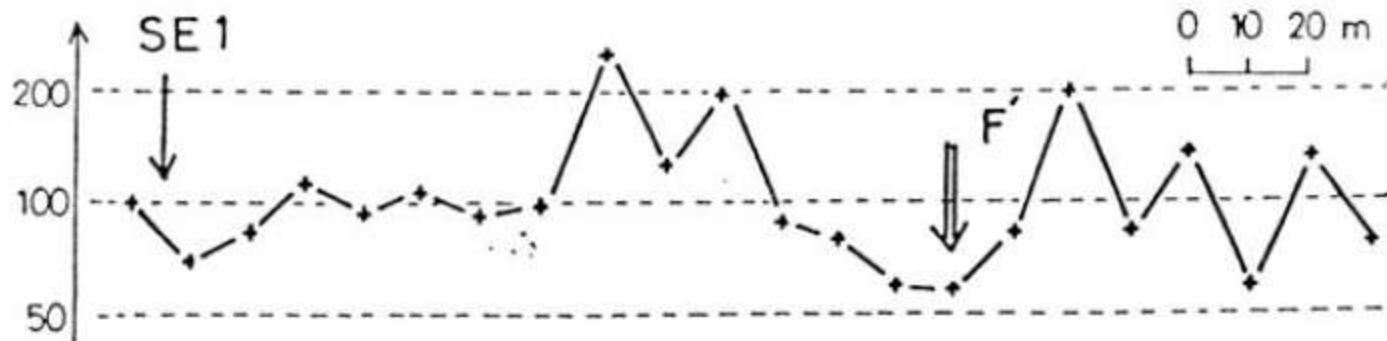
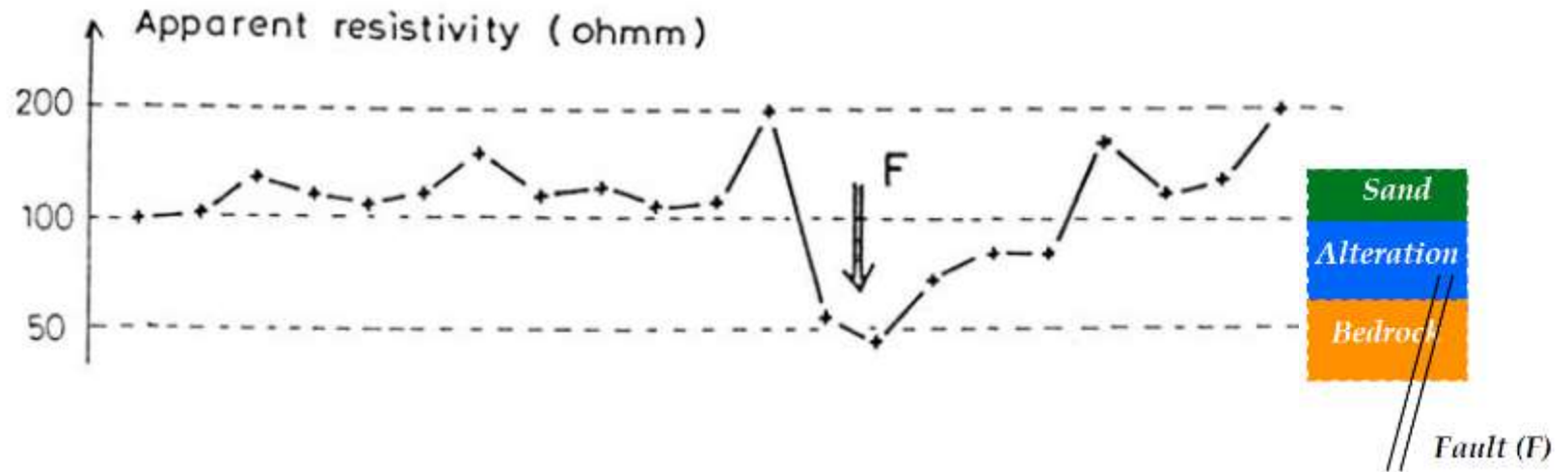
- Depth of investigation
- Sensitivity of the array to vertical and horizontal structures
- Horizontal data coverage
- Signal strength

# Resistivity Profiles



Source: <http://galitzin.mines.edu/INTROGP/>

# Profile Example: Niger Village Water Supply

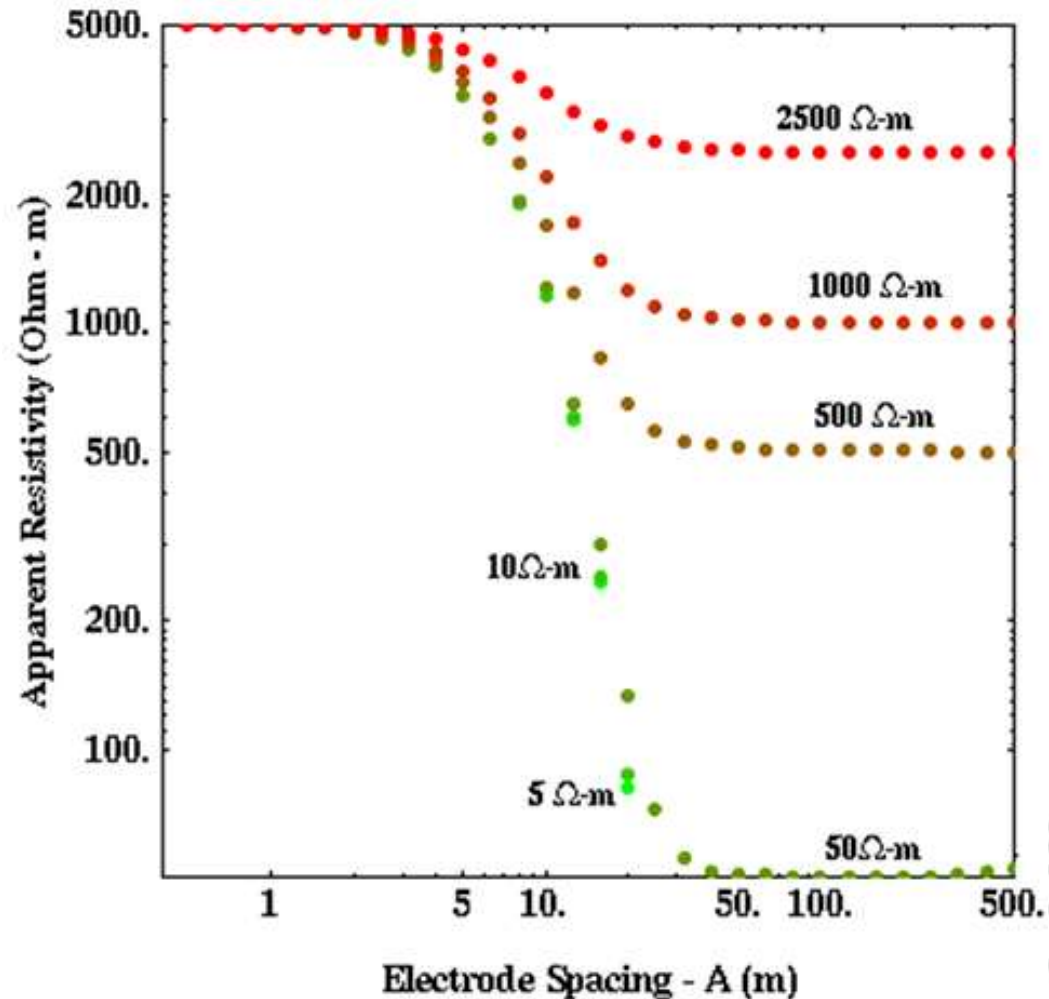
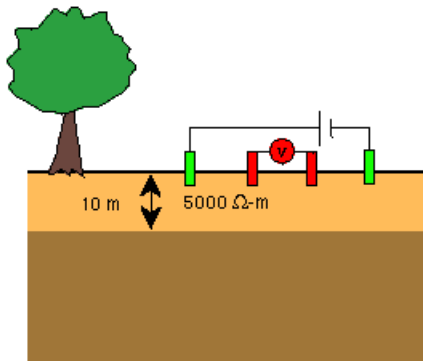


SCHLUMBERGER PROFILING ( AB = 300 m )

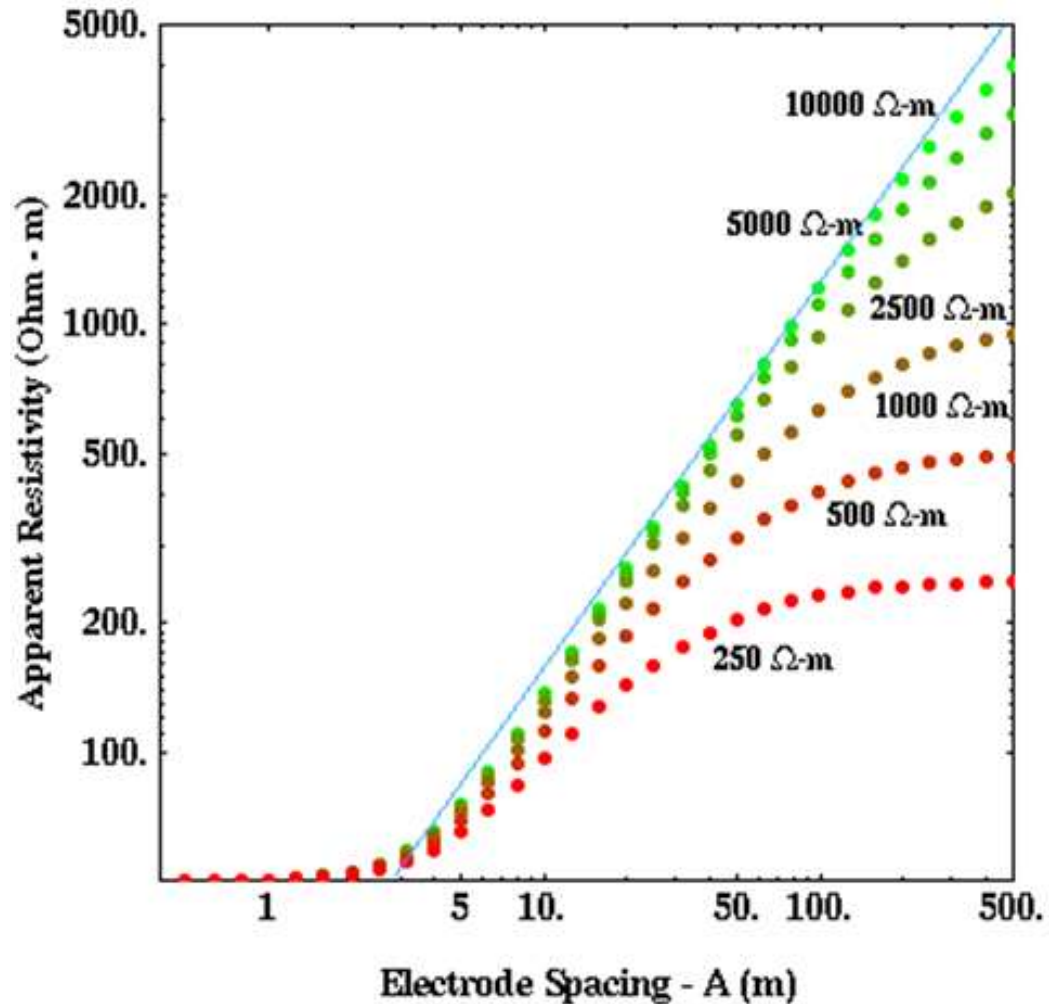
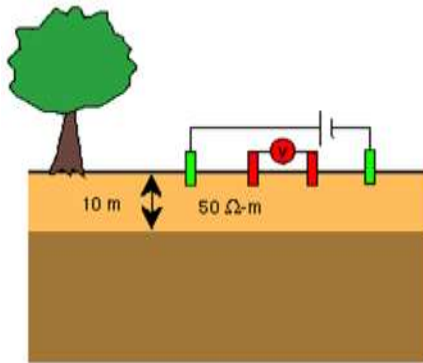
# **PART 5 – Interpretation of Resistivity Measurements**

1. Apparent Resistivity Curves for Soundings Over One-Layered Media
2. Apparent Resistivity Curves in Two-Layered Media
3. Resistivity Modelling and Inversion

# Apparent Resistivity Curves for Soundings Over One-Layered Media: Case 1

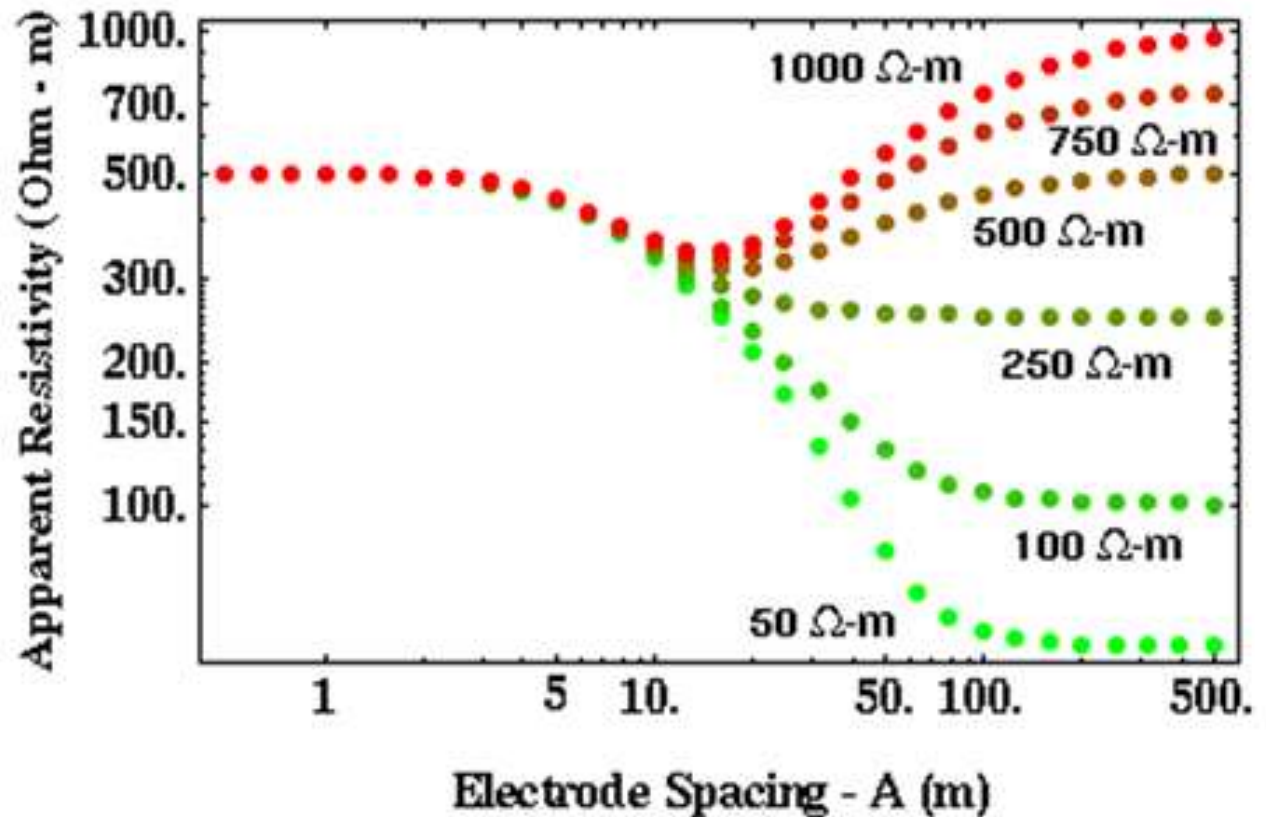
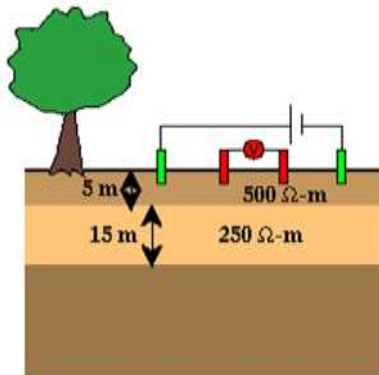


# Apparent Resistivity Curves for Soundings Over One-Layered Media: Case 2

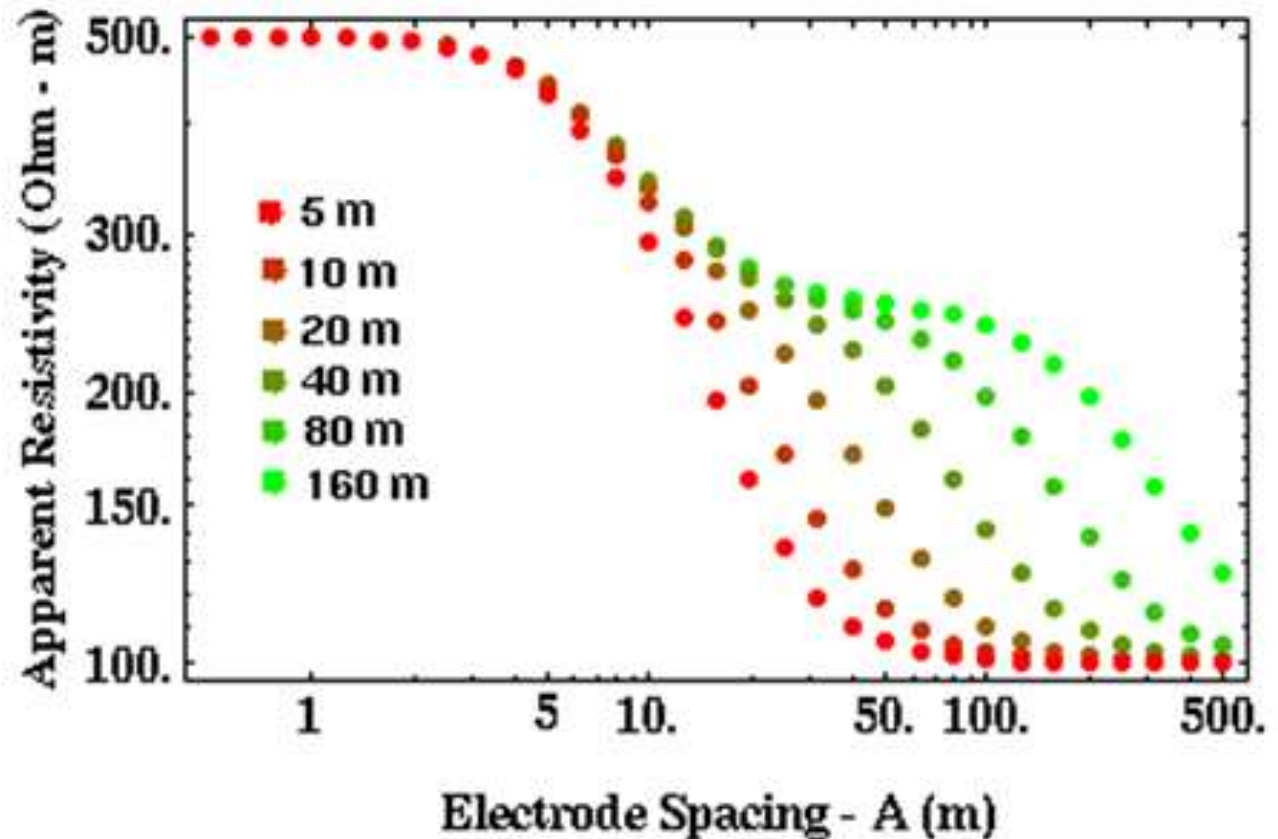
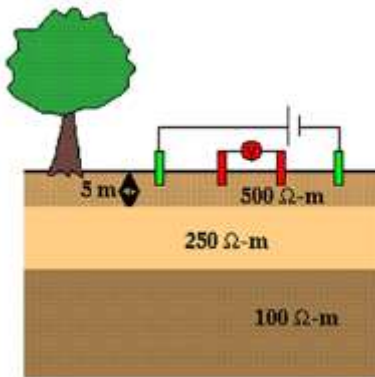




# Apparent Resistivity Curves in Two-Layered Media: Case 1

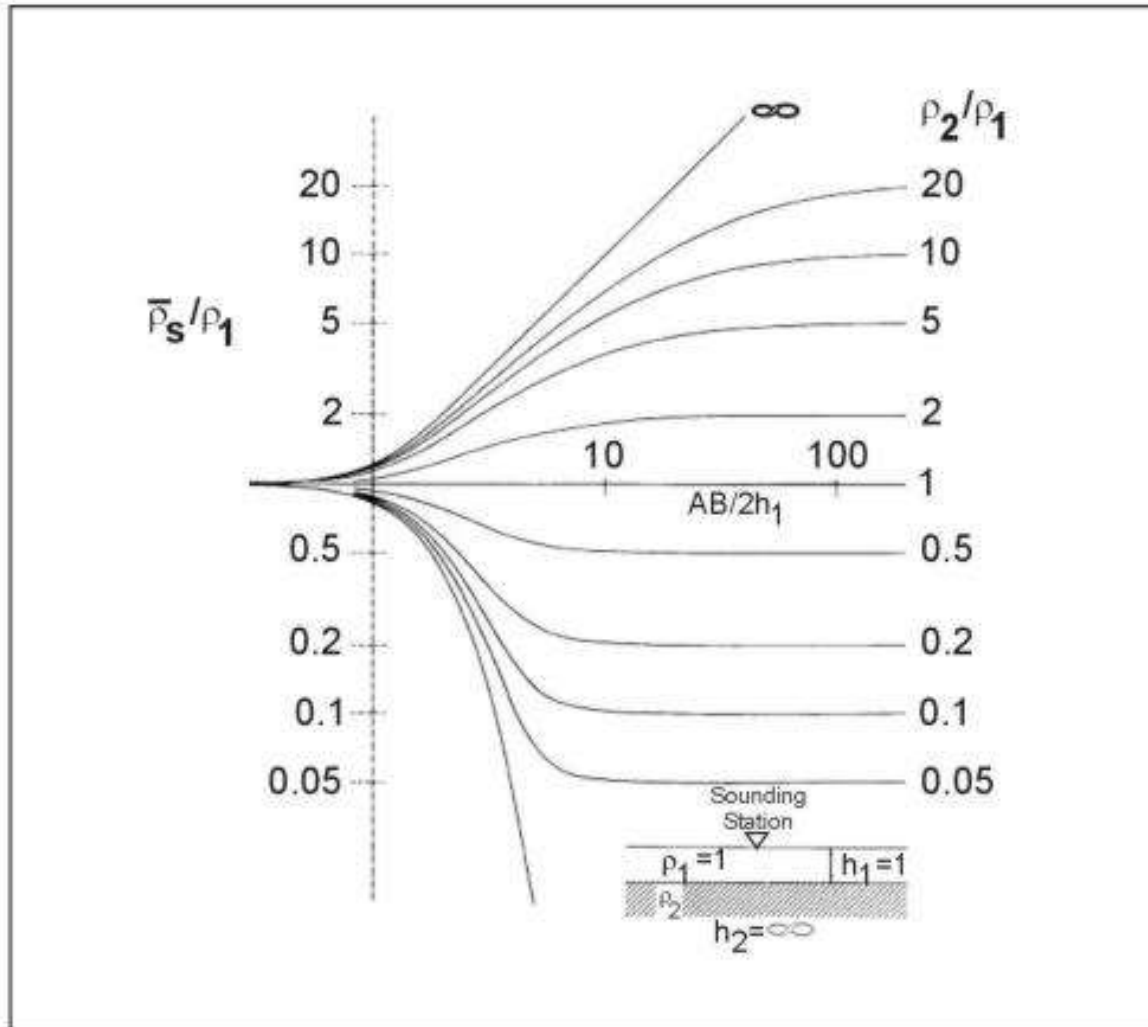


# Apparent Resistivity Curves in Two-Layered Media: Case 2



# Apparent Resistivity Curves in Two-Layered Media

Two-layer master set of sounding curves for the Schlumberger array. (Zohdy, 1974)

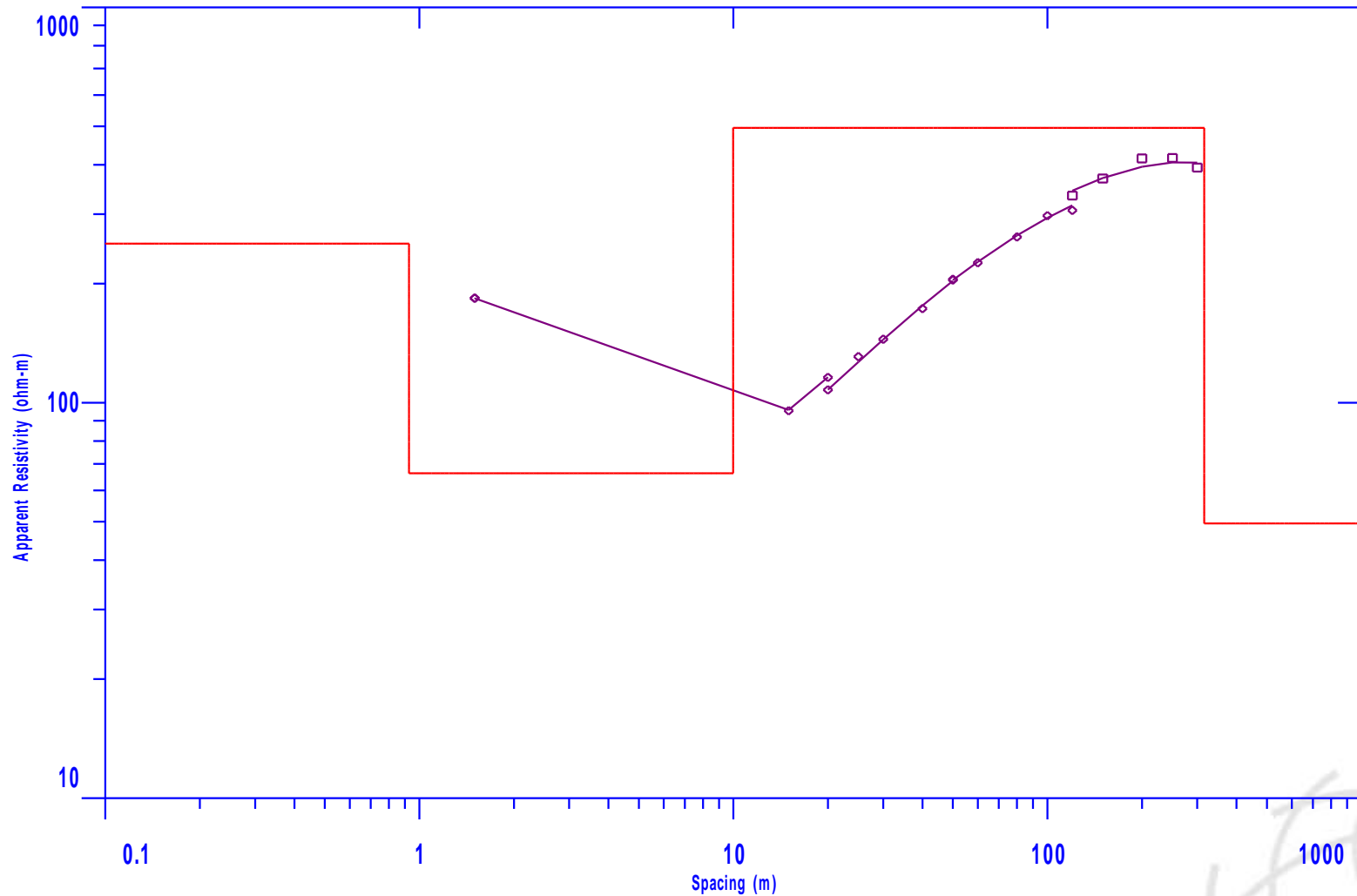


Source: [http://www.epa.gov/esd/cmb/GeophysicsWebsite/pages/reference/methods/Surface\\_Geophysical\\_Methods/Electrical\\_Methods/Resistivity\\_Methods.htm](http://www.epa.gov/esd/cmb/GeophysicsWebsite/pages/reference/methods/Surface_Geophysical_Methods/Electrical_Methods/Resistivity_Methods.htm)

# 1D Inversion – 1X1D (Interpex Limited)

Balkh\_1

Unregistered Version



# 1D Inversion – GeoVES 1.4

Client : Irrigation Department  
Project : Balkh  
District :  
Date : 2013  
Field Operator : Ahmad Jawid  
Interpreted by : AdJ

Community : Balkh  
Sounding Number : S-01  
Coordinates East : E XX.XXXXX  
Coordinates North : N XX.XXXXX  
GPS Datum : WGS84  
Azimuth : XX°

**Balkh - S-01**

**GeoVES 1.4**

MS Excel based modelling of Vertical Electrical Soundings in the Schlumberger Array using Gosh linear filters

### Geoelectrical Model

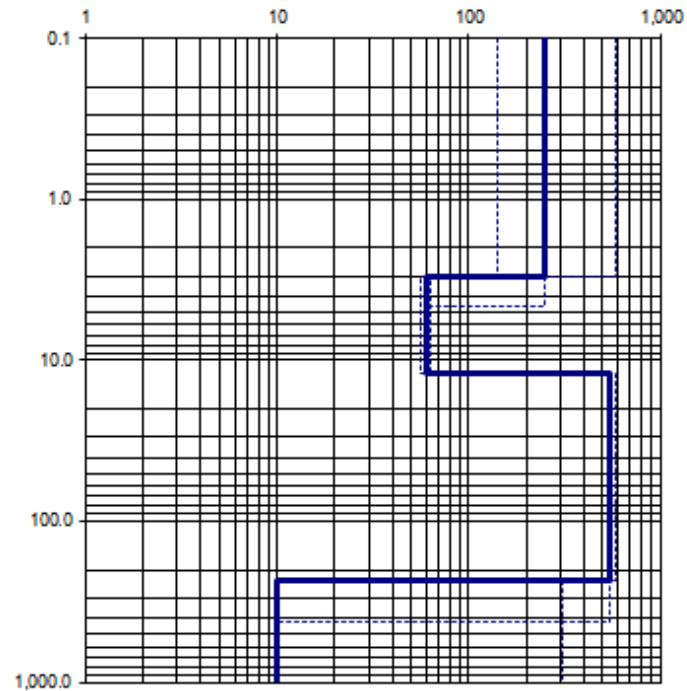
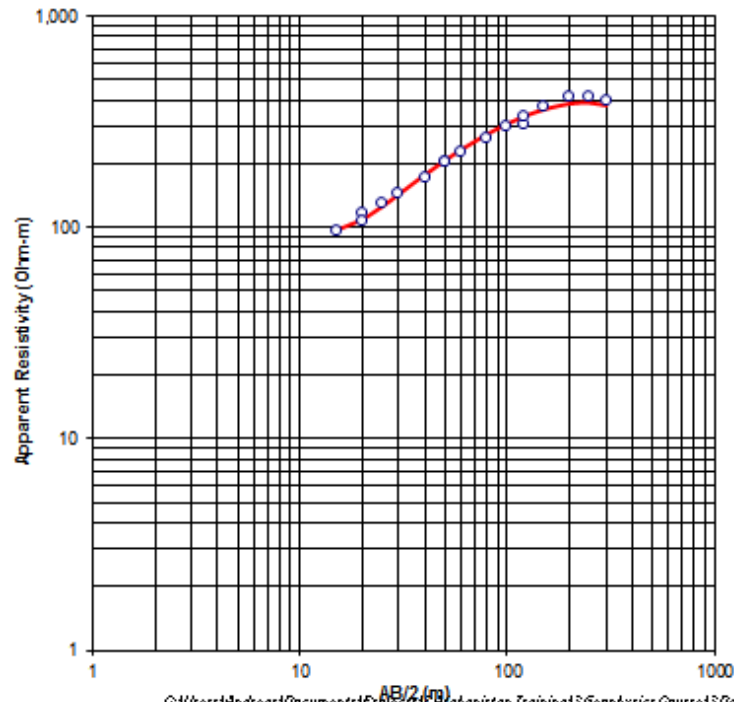
**RMS Error : 14**

|                            |          |          |          |          |          |          |          |          |
|----------------------------|----------|----------|----------|----------|----------|----------|----------|----------|
| <b>Layer Number</b>        | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b> | <b>7</b> | <b>8</b> |
| <b>Resistivity (Ohm-m)</b> | 250      | 60       | 540      | 10       |          |          |          |          |
| <b>Thickness (m)</b>       | 3.0      | 9.0      | 220.0    |          |          |          |          |          |
| <b>Depth (m)</b>           | 3.0      | 12.0     | 232.0    |          |          |          |          |          |

### Sensitivity Analysis

### Remove Error Bars

### Geoelectrical Model



# 2D Inversion

